

Magnetic Resonance Imaging



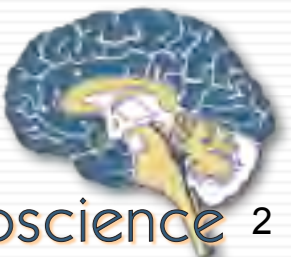
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Biomedical Physics. Biomedical Engineering

The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
- The “Pulse Sequence” Rules Everything (3)
Seventh Inning Stretch
- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)
- Image Quality and Artifacts (48)



Metaphor

['metə,fôr; -fər]

noun

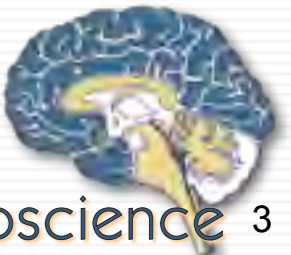
1. a figure of speech in which a word or phrase is applied to an object or action to which it is not literally applicable :

“I had fallen through a trapdoor of depression,” said Mark, who was fond of theatrical metaphors | her poetry depends on suggestion and metaphor.

a thing regarded as representative or symbolic of something else, esp. something abstract :

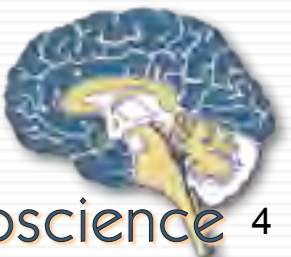
*the amounts of money being lost by the company were enough to make it a **metaphor for** an industry that was teetering.*

2. Little white lie



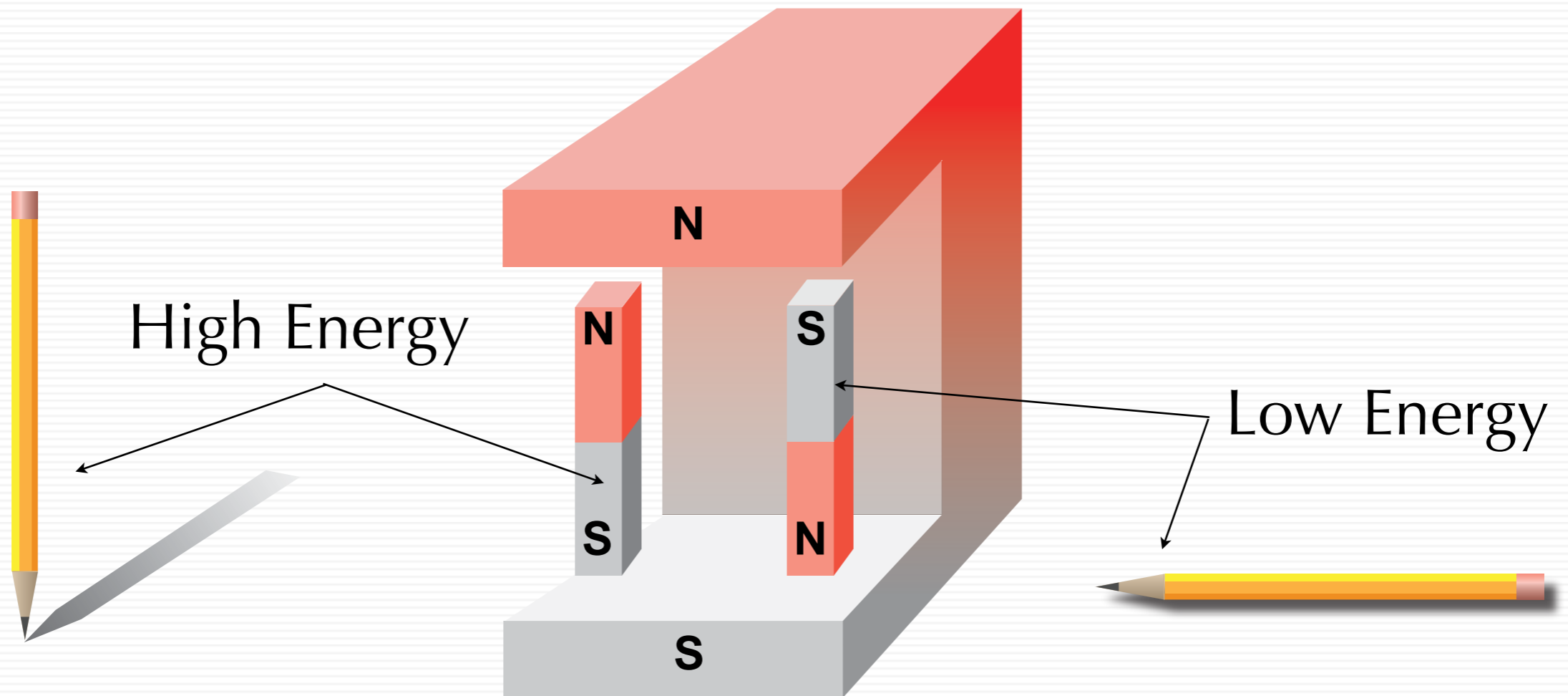
Spin

- Similar to Angular Momentum
- Intrinsic Property of Matter (rotation *not* required)
- Spin takes half-integer (0, 1/2, 1, 1-1/2) quantum values
 - Particles with integer spin are ***Bosons***
 - Particles with half integer spins are ***Fermions***
- Atoms with odd Mass Numbers (^1H , ^{13}C , ^{19}F , ^{23}Na) have half-integer spin.
- Electrons, Neutrons, Protons have spin = 1/2

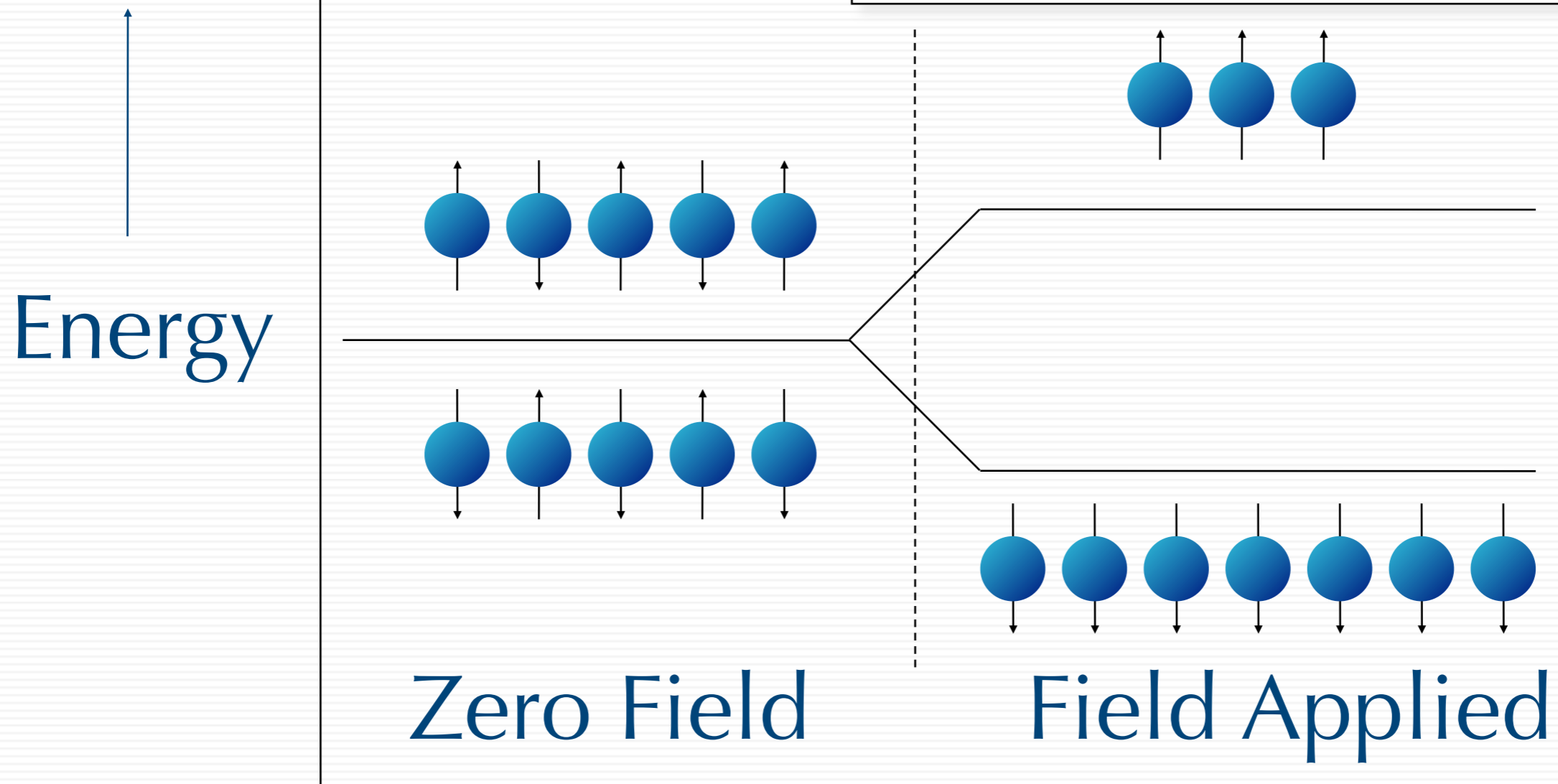


Spin States

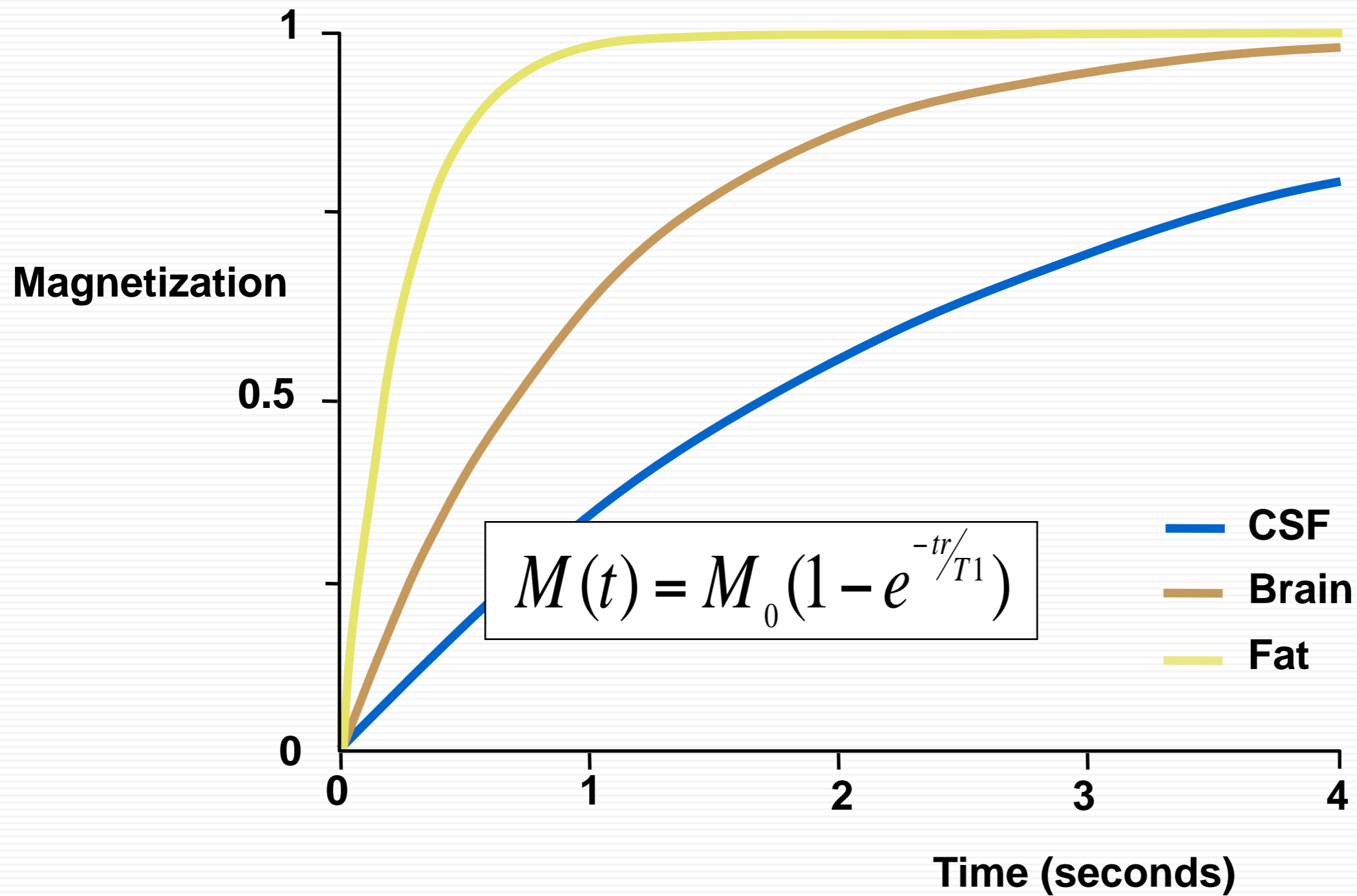
- A Spin 1/2 particle has two states: up and down
- In a magnetic field, B_0 , the two states have different energies



Transition to Equilibrium

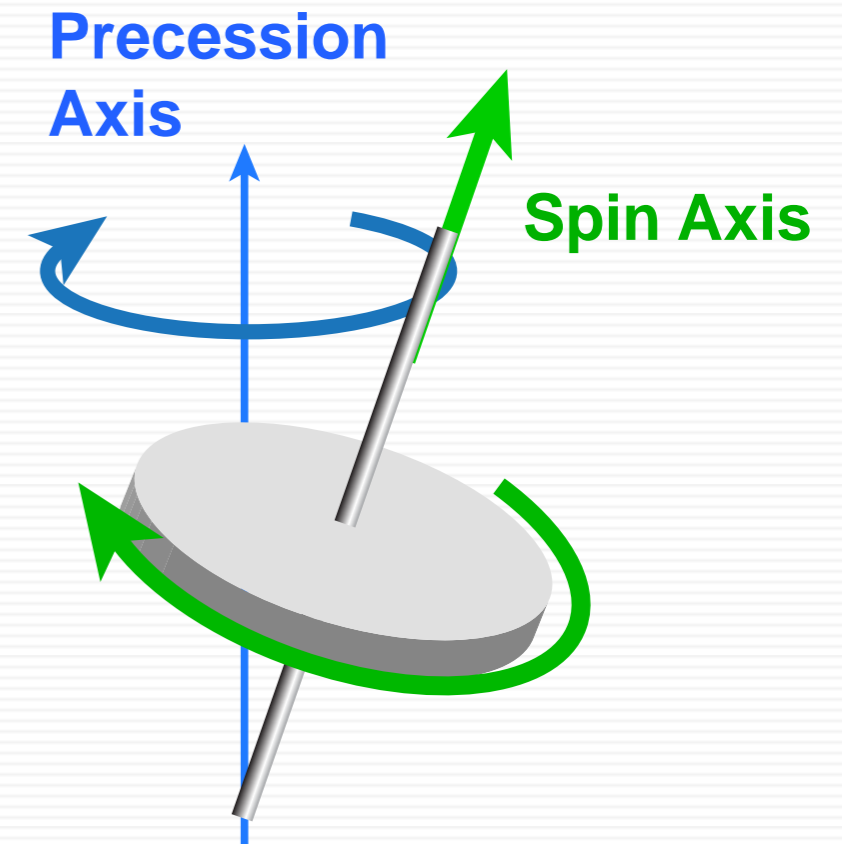


T1



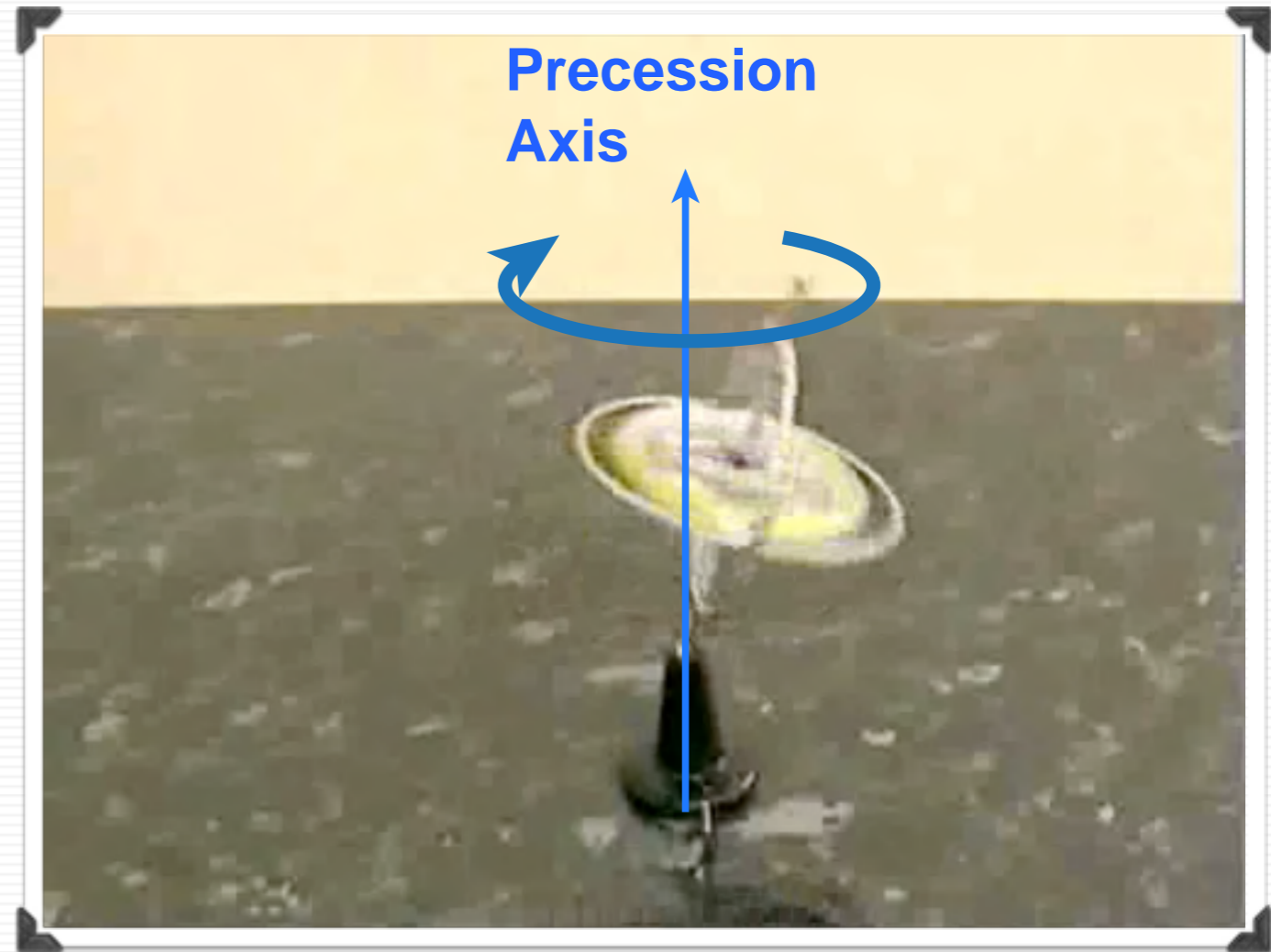
Nuclear Spin

- Angular momentum is a vector quantity having *magnitude & direction*.
- Angular Momentum is *Conserved*, causing precession to occur



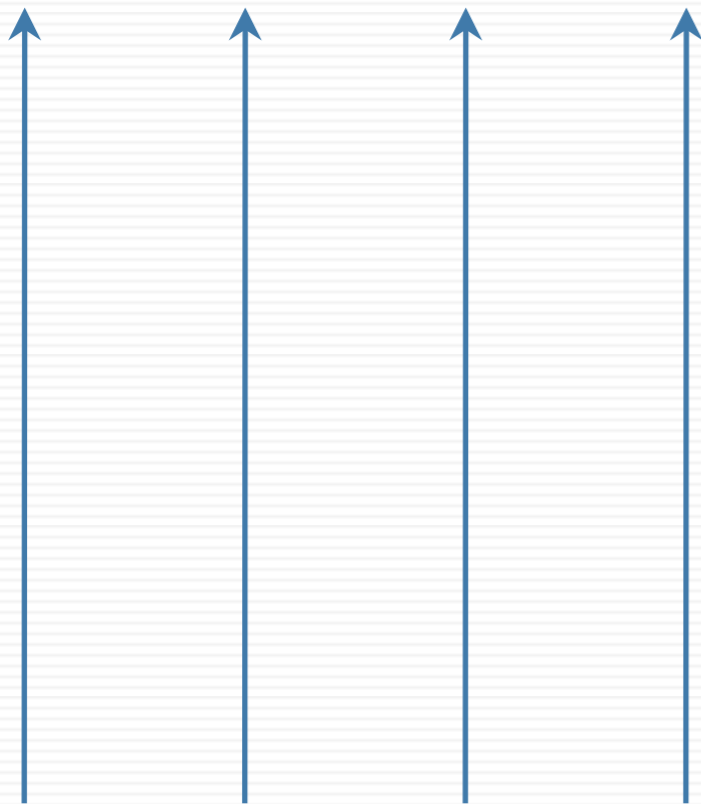
Nuclear Spin

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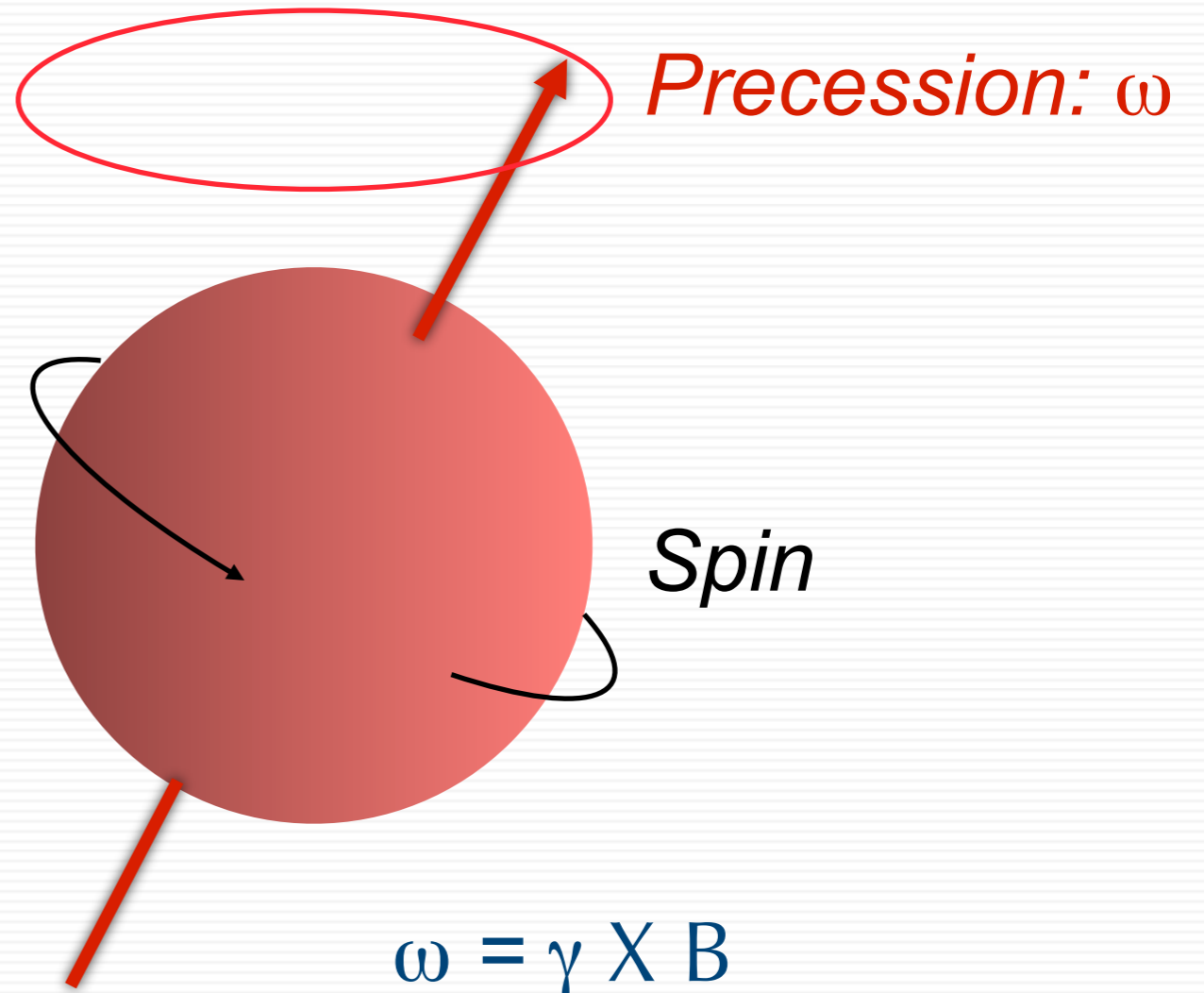


Proton Precession

Due to their angular momentum, Protons precess in the magnetic field.



Applied Magnetic Field: **B**



$$\omega = \gamma \times B$$

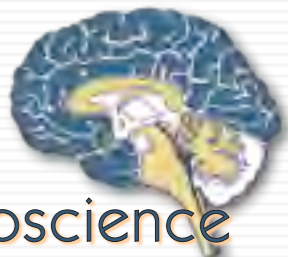
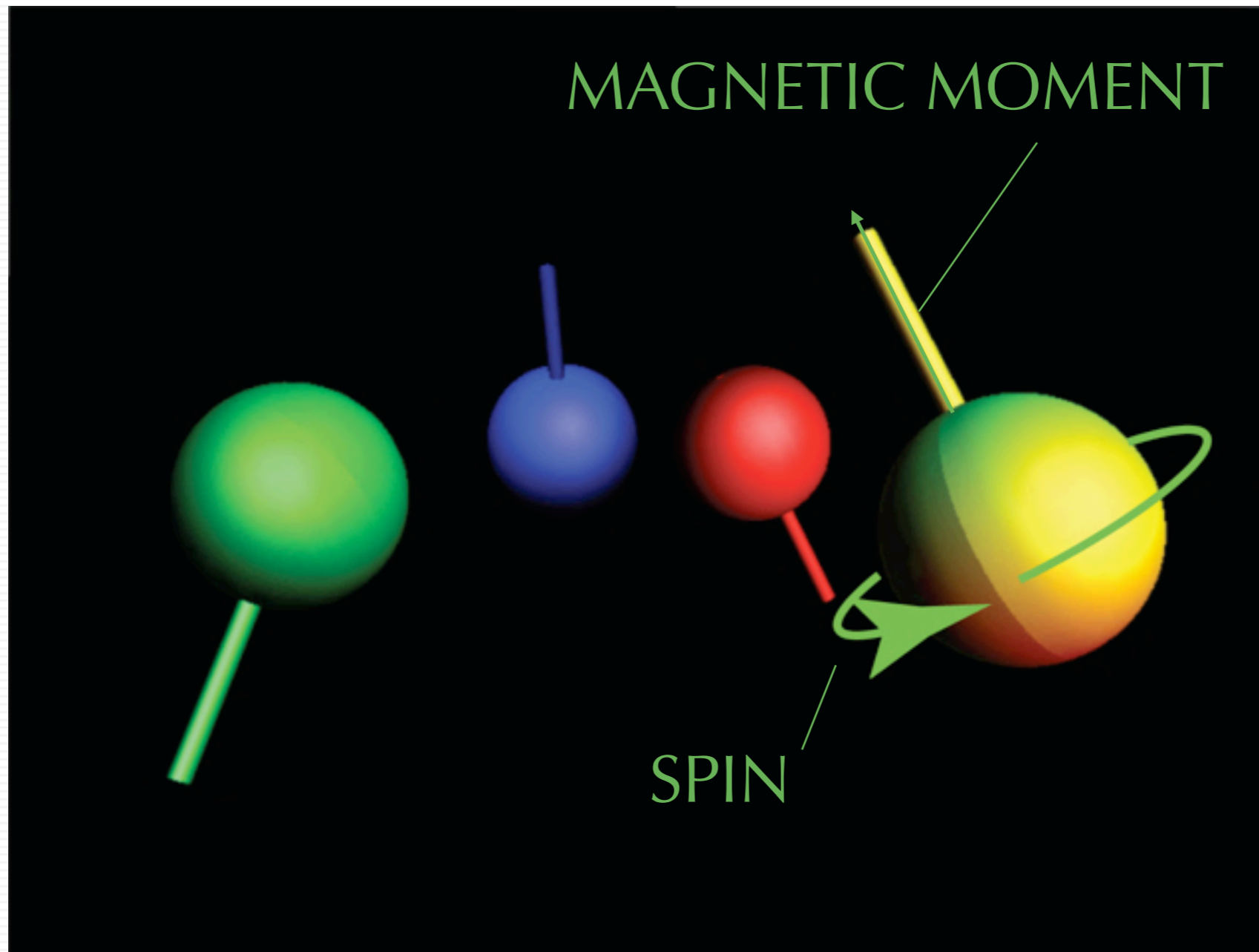
$$\gamma_H \approx 267.52 \text{ Rad/sec/Tesla}$$

$$\approx 42.577 \text{ MHz/Tesla}$$



MRI 101a

Protons, the Nucleus of Hydrogen, Have a Magnetic Moment



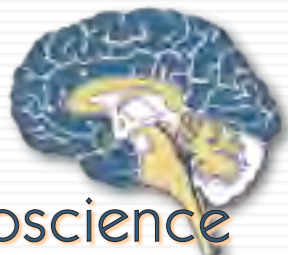
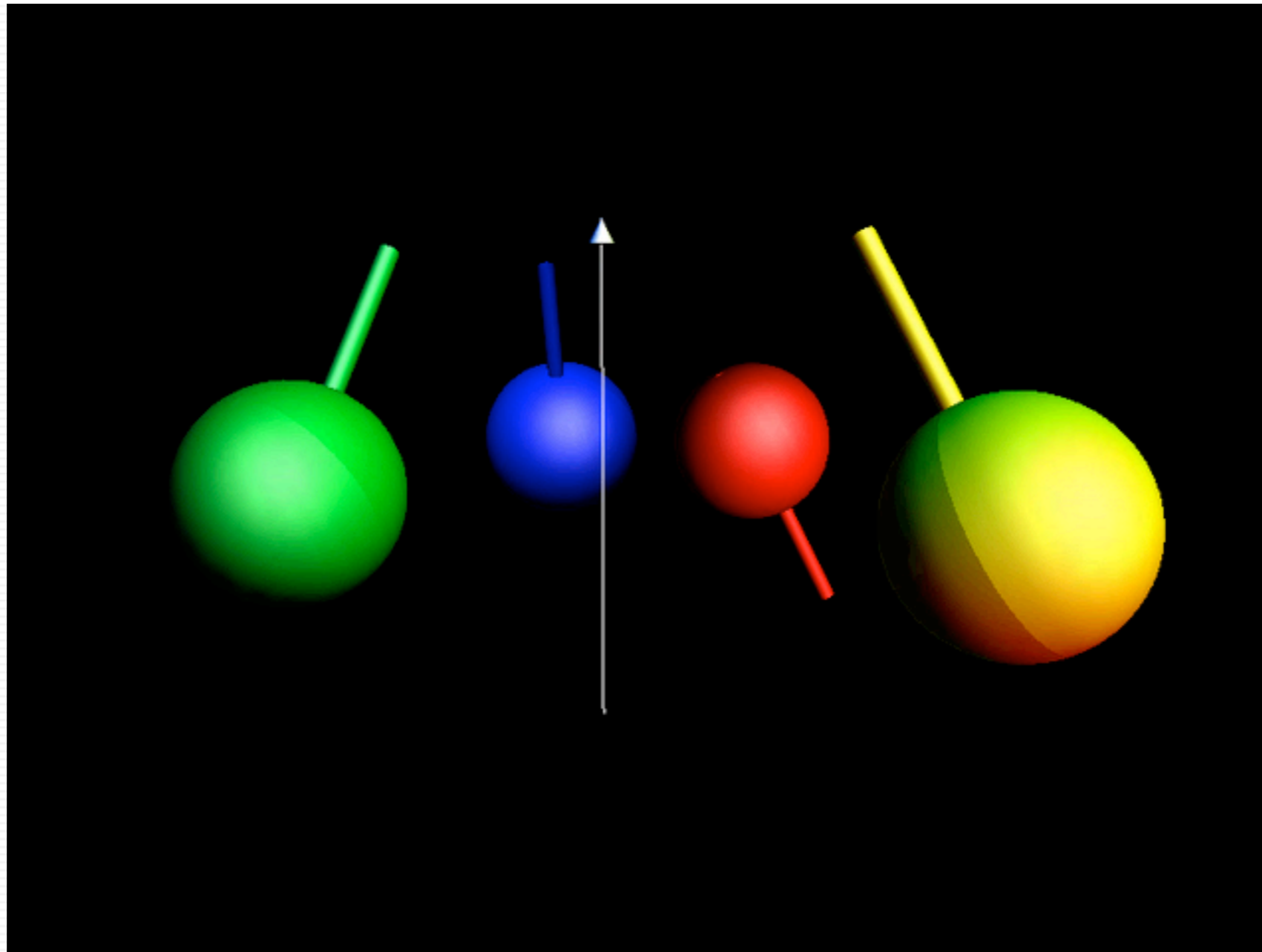
MRI 101b

Protons Align (polarize) and Precess in Magnetic Fields



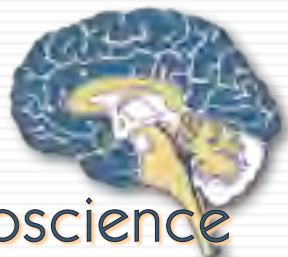
MRI 101b

Protons Align (polarize) and Precess in Magnetic Fields



Proton Responses to Magnetic Field

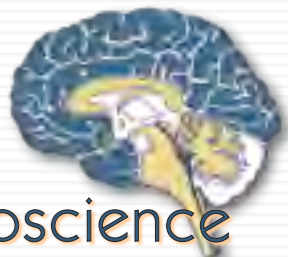
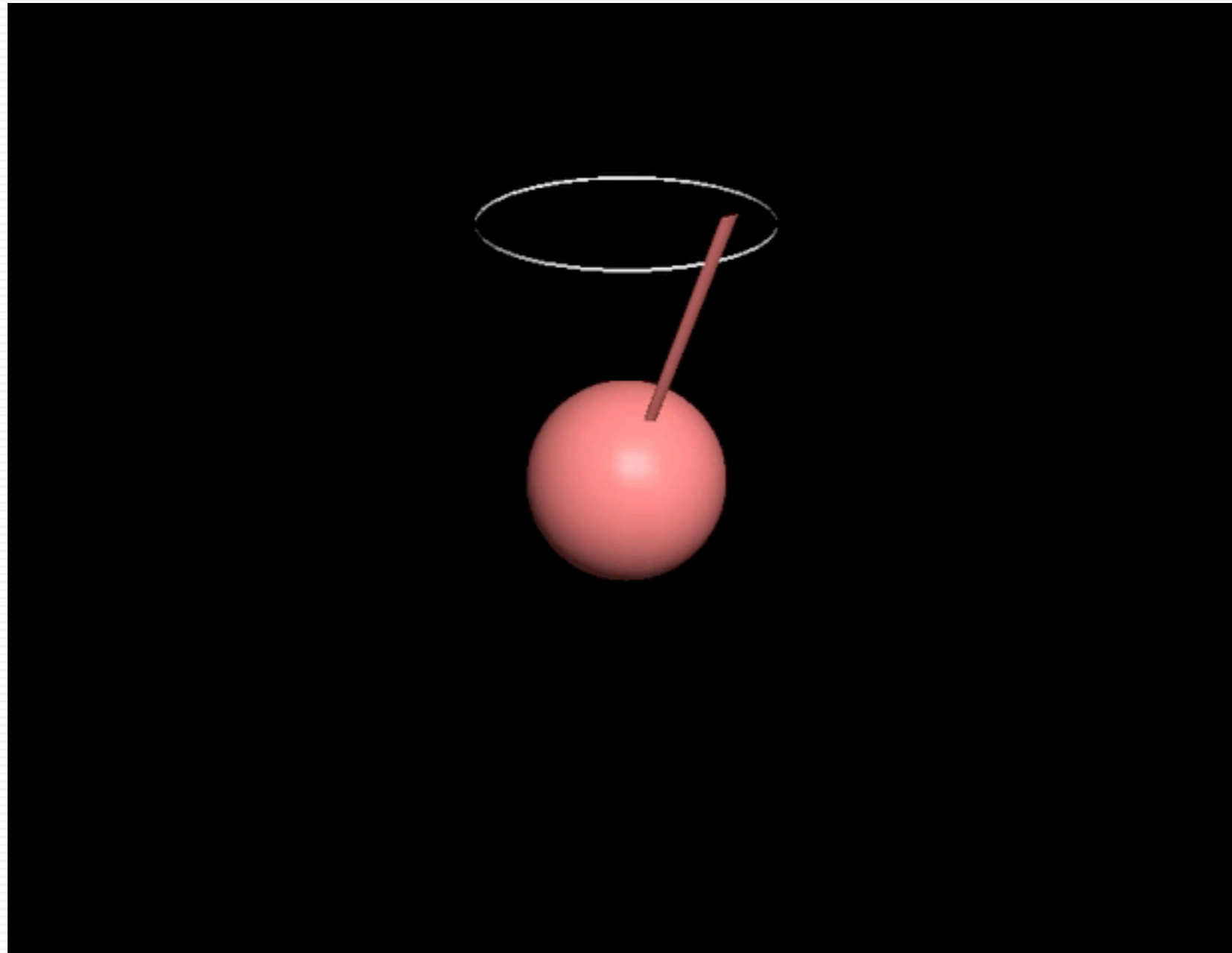
- Spin Alignment Along Net Applied Field
spins align parallel or anti-parallel to the applied field
- Precession About the Magnetic Field
at a precession frequency of: $\gamma \times B$, known as the Larmor frequency
- Spin Alignment Occurs at the Rate, T1



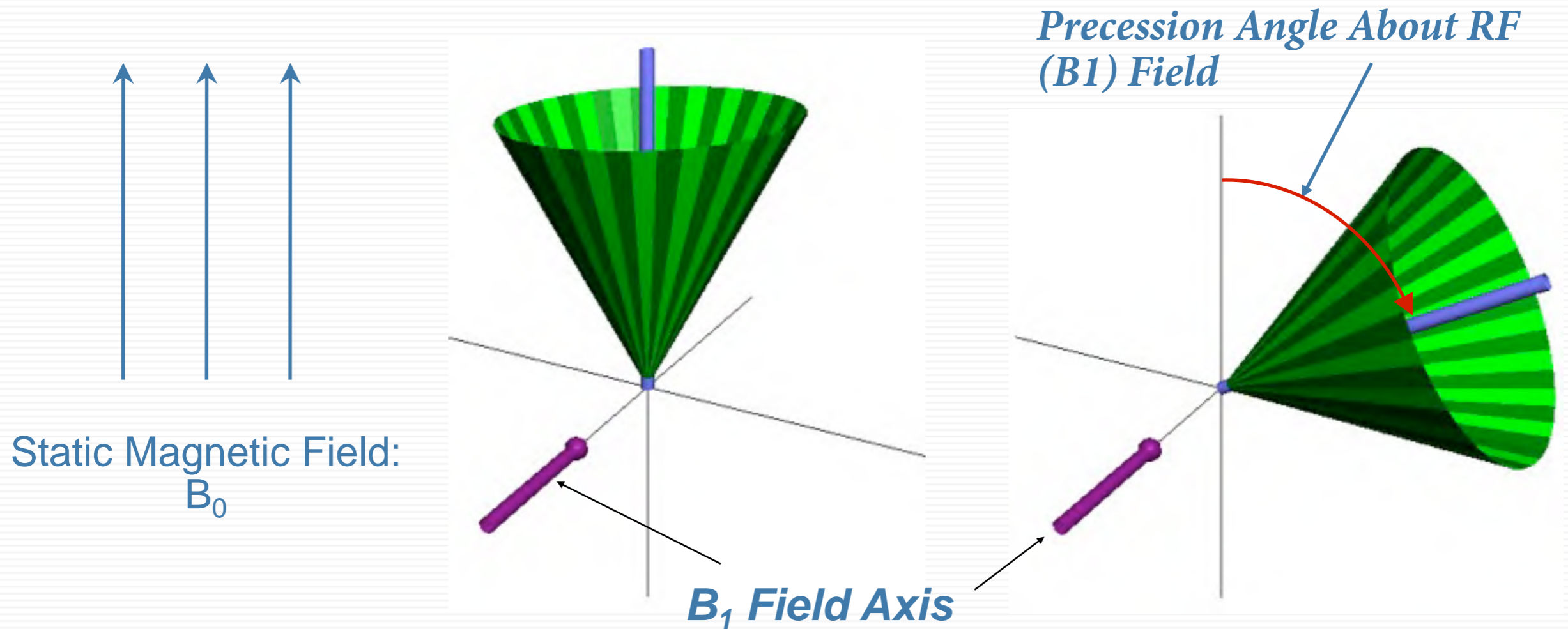
Vector Addition of Spins



Vector Addition of Spins



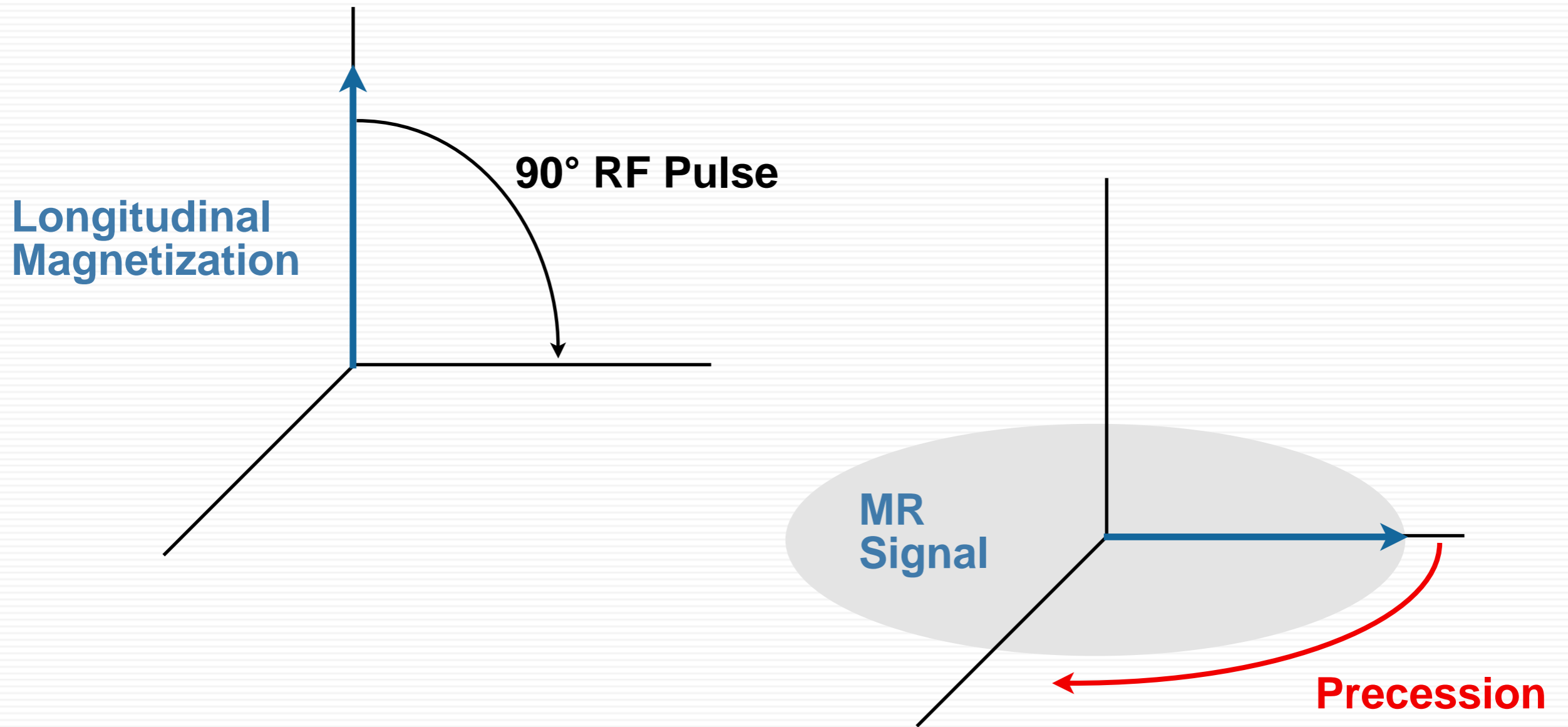
the Resonance Phenomenon



- When a second magnetic field (B_1) is applied, rotating at the Larmor rate, the proton will precess about it.
- The duration and amplitude of B_1 determine rotation angle



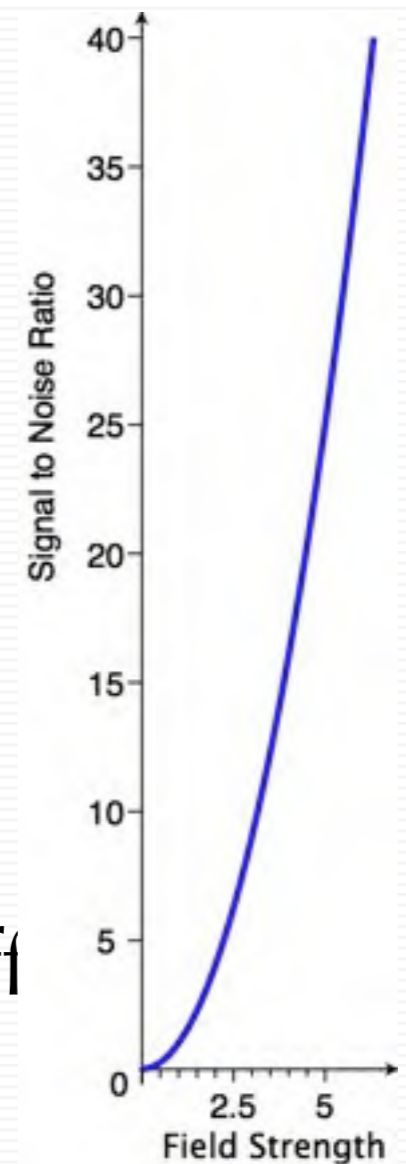
RF Pulses Convert Longitudinal Magnetization to MR Signal



Inductive Detection

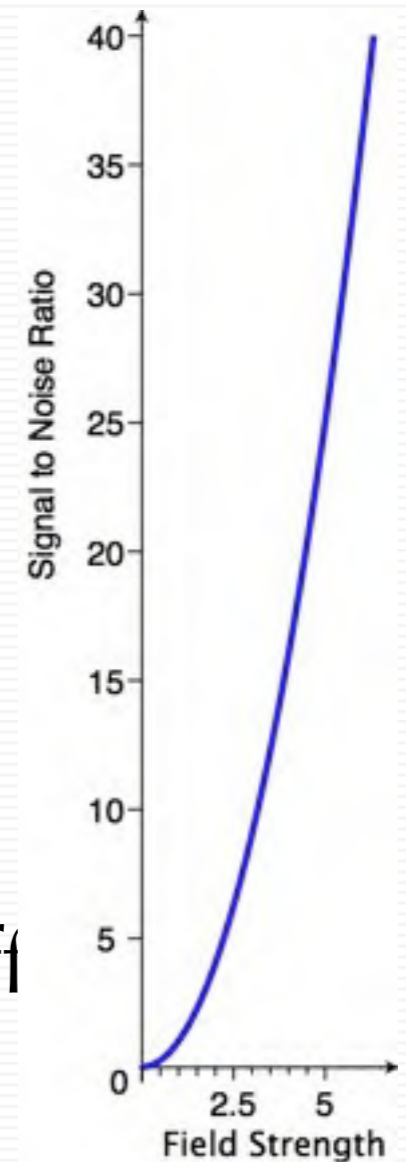
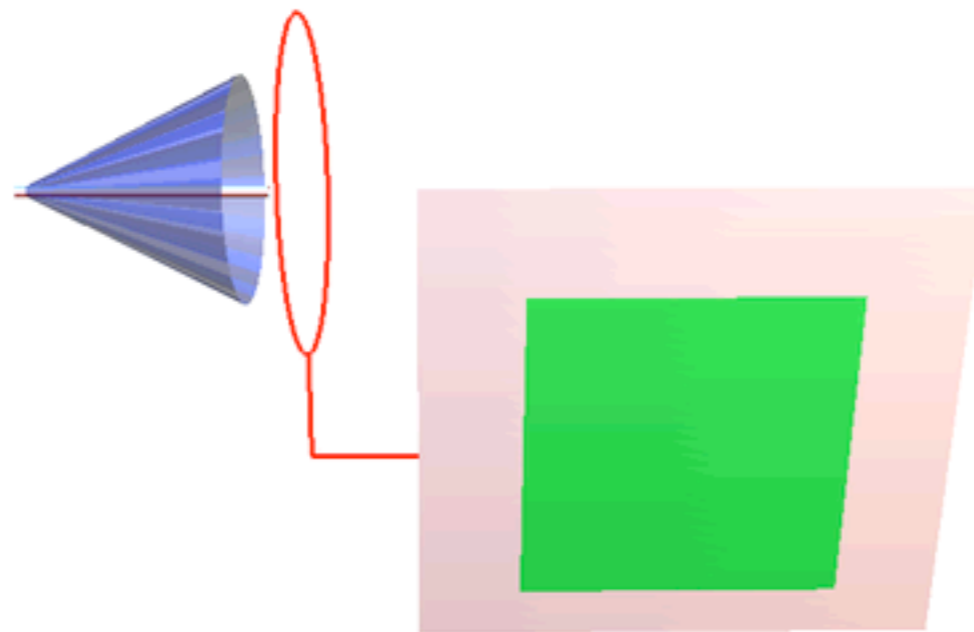
With Conventional MRI, the Signal is Detected Inductively.
Therefore the Intensity is Proportional to Frequency

In This Mode, Signal to Noise Ratio Falls off
Rapidly With Field Strength



Inductive Detection

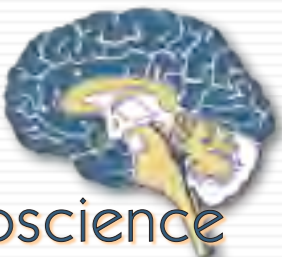
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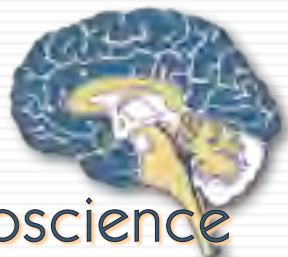
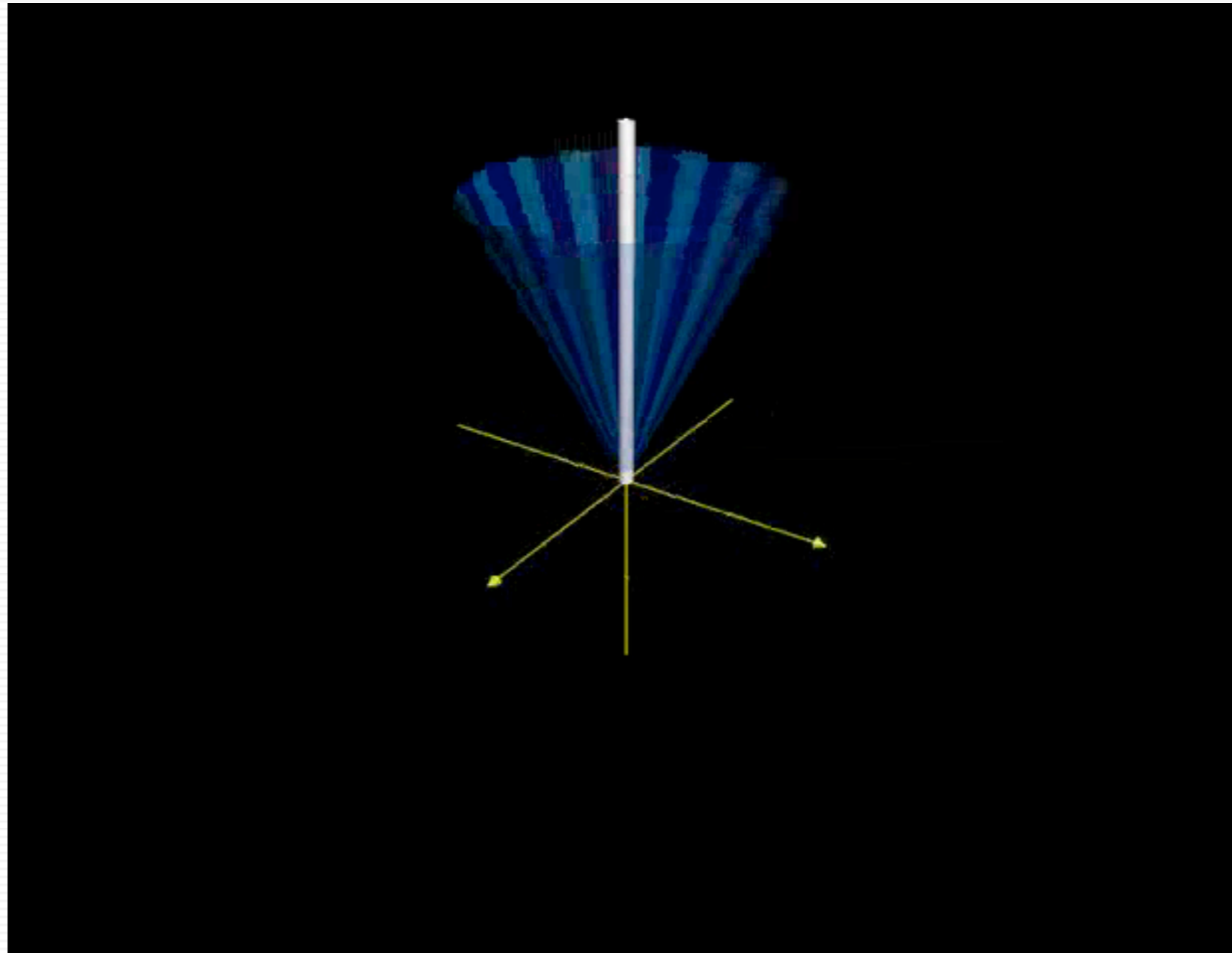
In This Mode, Signal to Noise Ratio Falls off Rapidly With Field Strength



From Magnetization to Signal

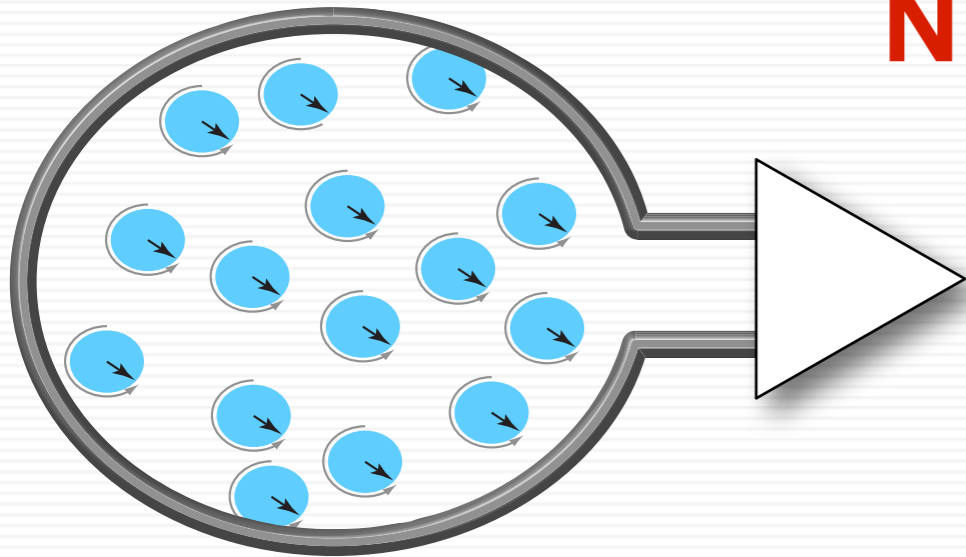


From Magnetization to Signal

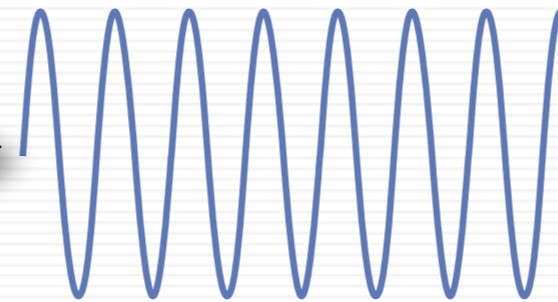


Spin Dephasing

N

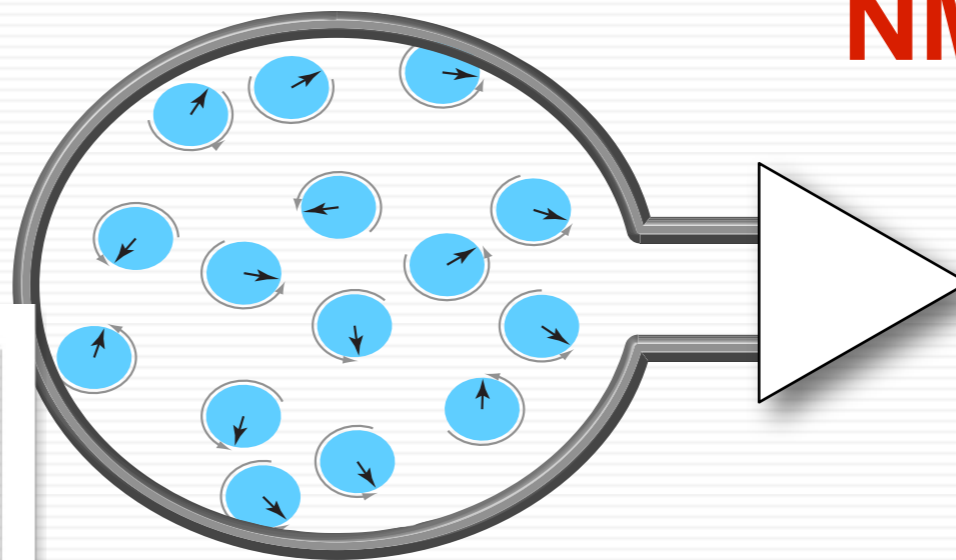


NMR Signal

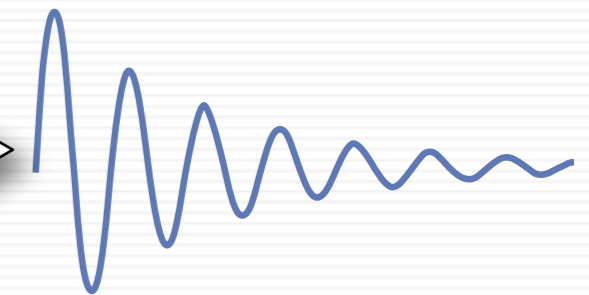


S

N



NMR Signal

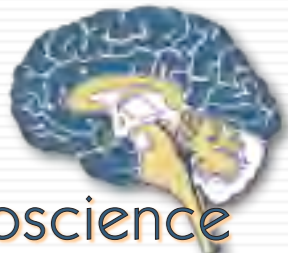
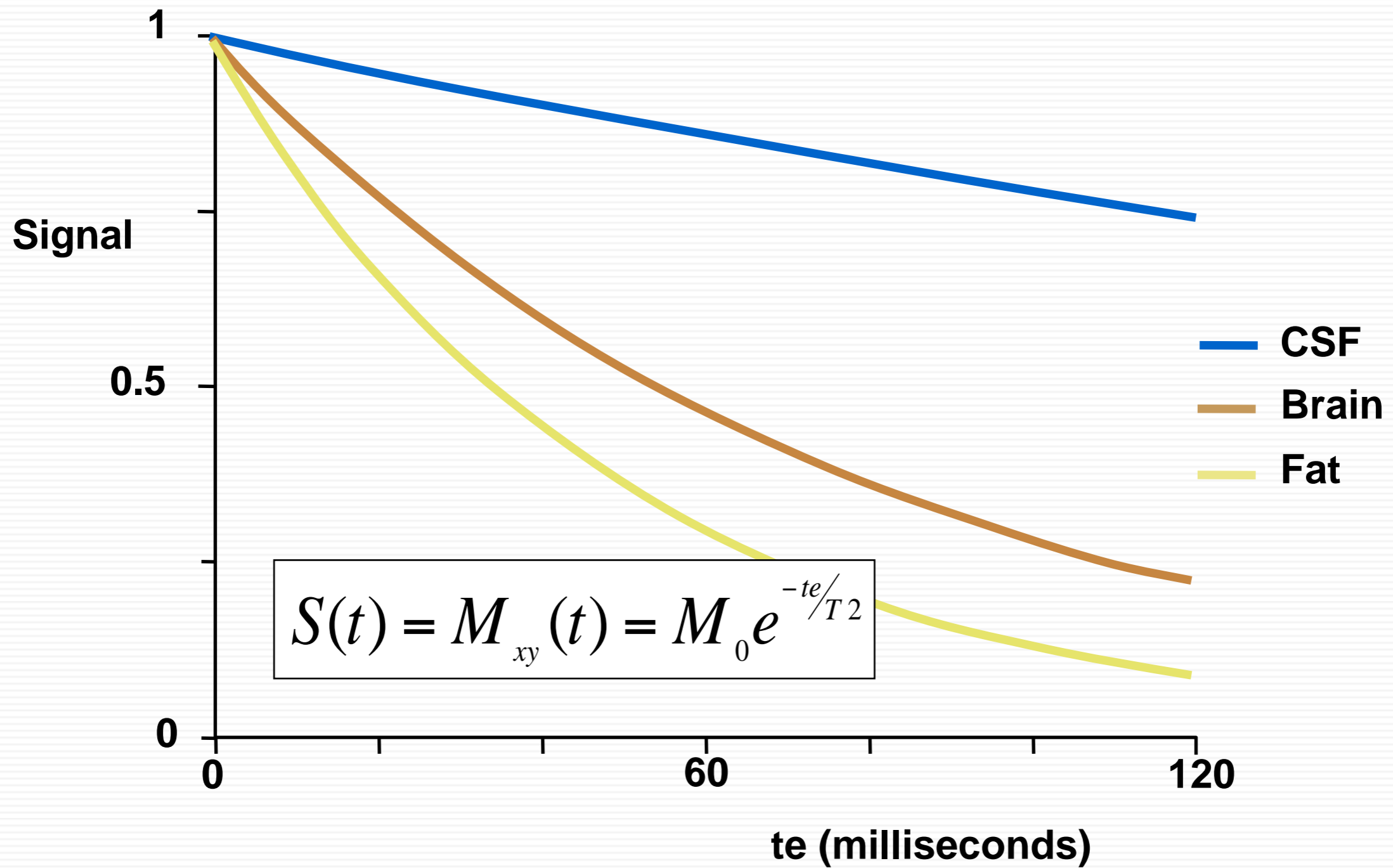


Dephasing results in no change in energy.

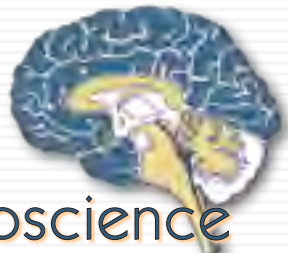
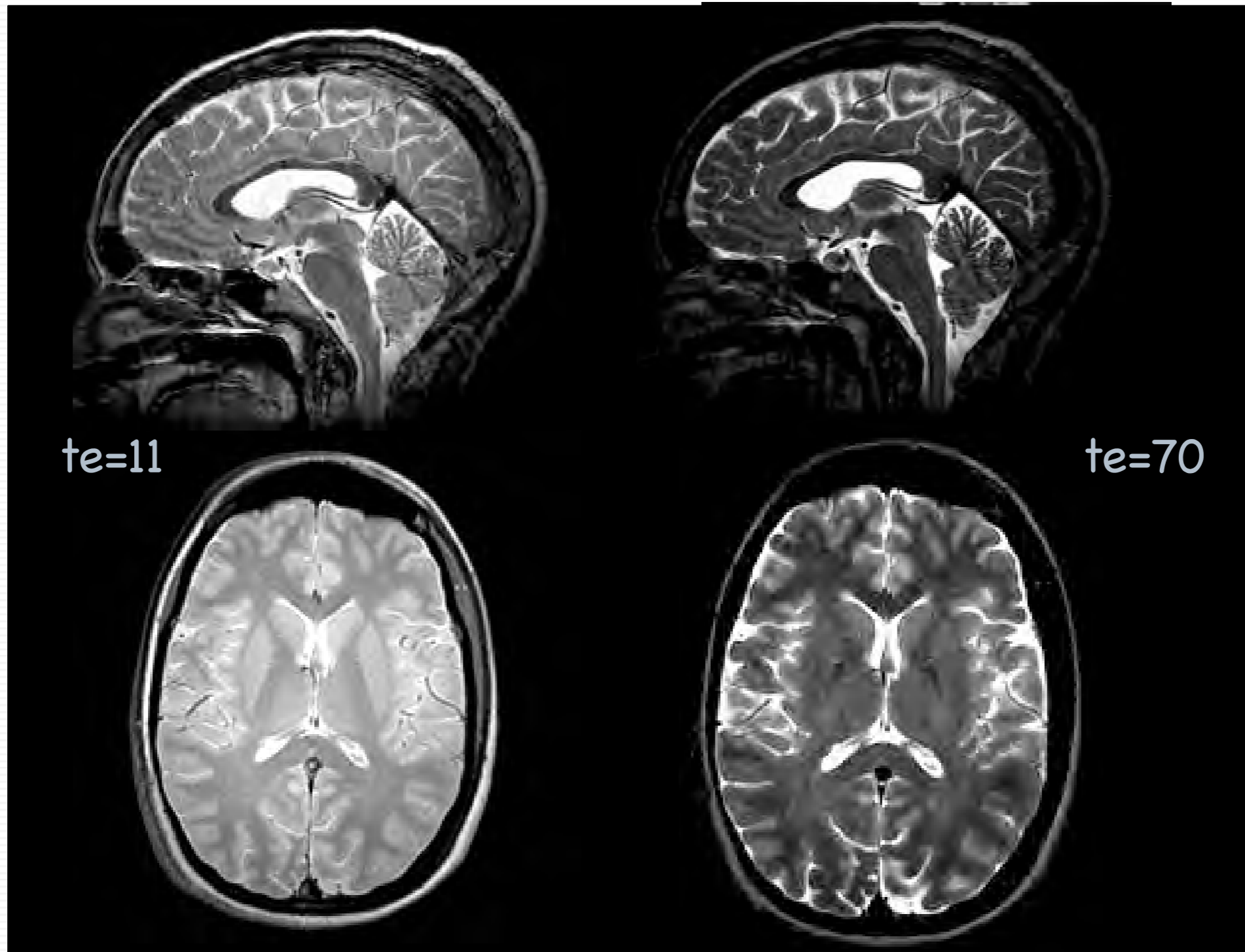
S



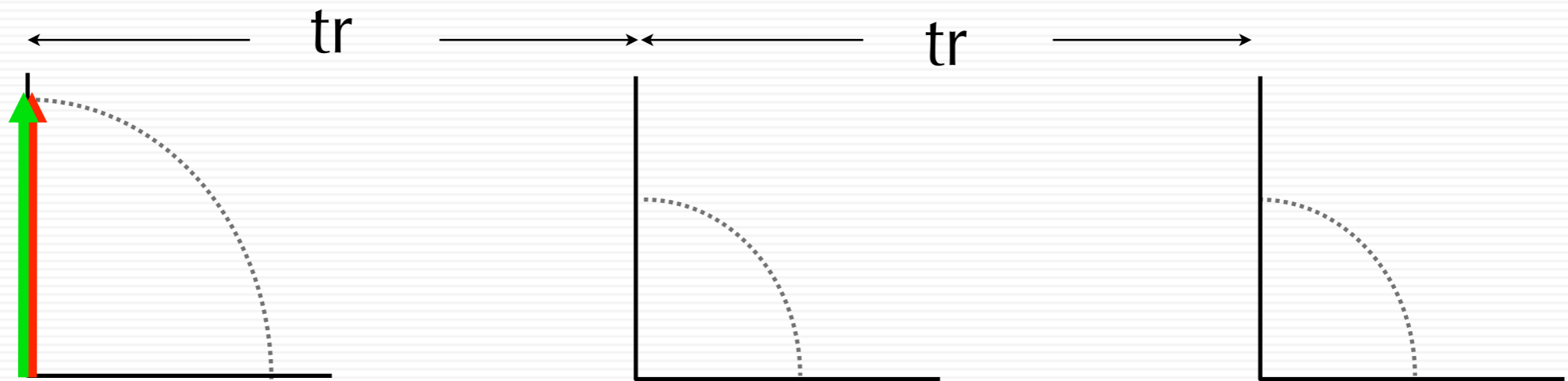
T2 and te



Effects of TE at long TR



Partial Saturation Sequence

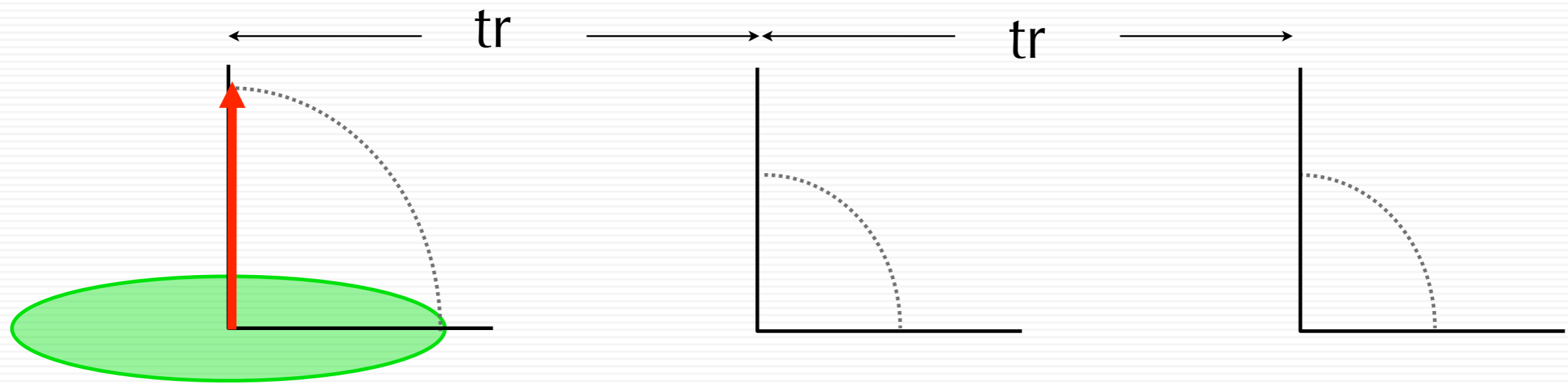


Sequence of 90° Pulses

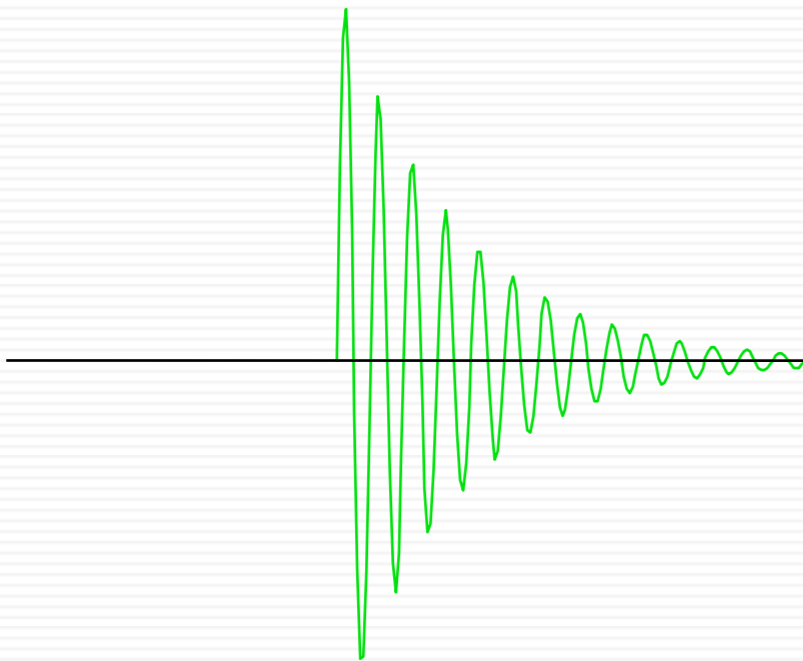
NMR Signal



Partial Saturation Sequence



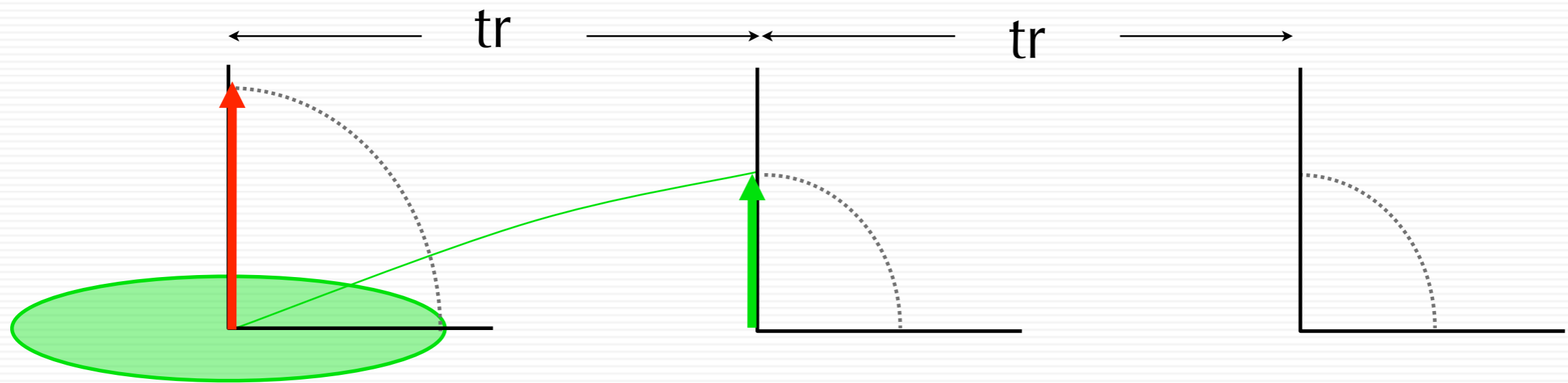
Sequence of 90° Pulses



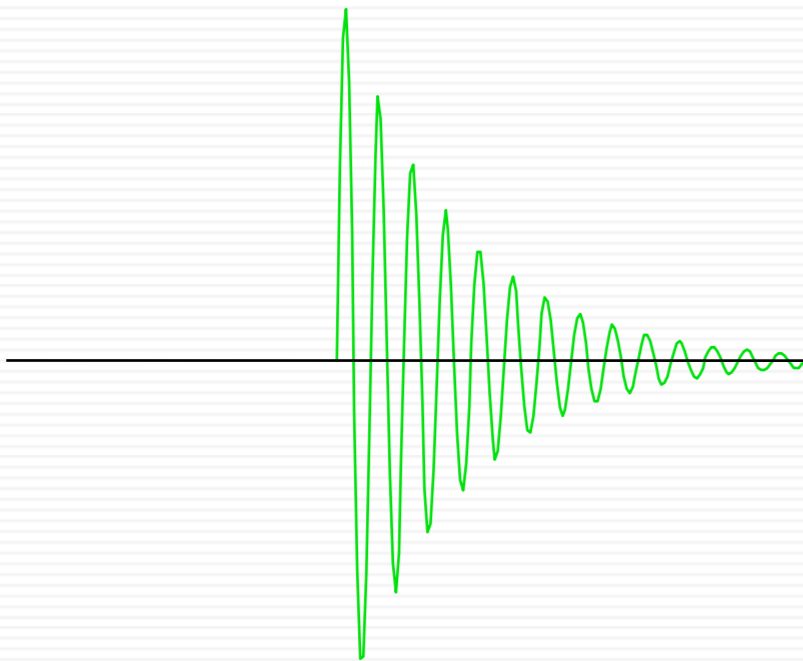
NMR Signal



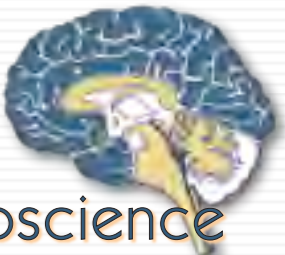
Partial Saturation Sequence



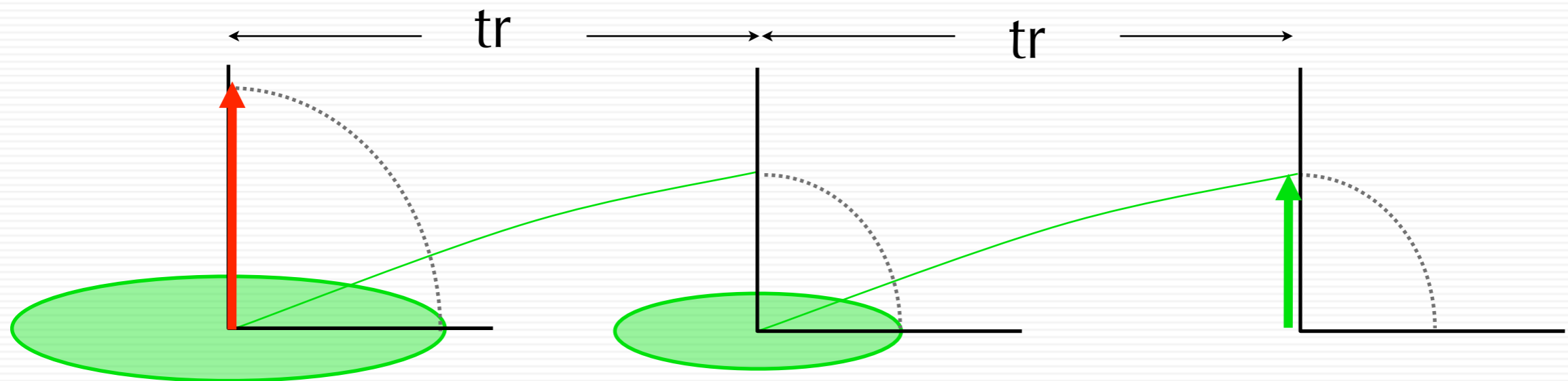
Sequence of 90° Pulses



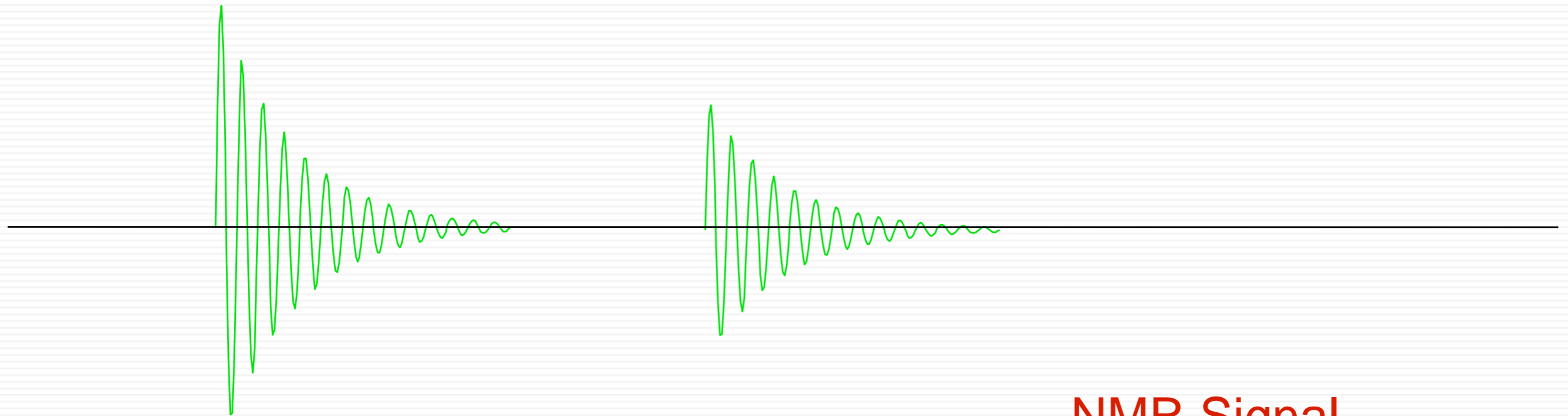
NMR Signal



Partial Saturation Sequence



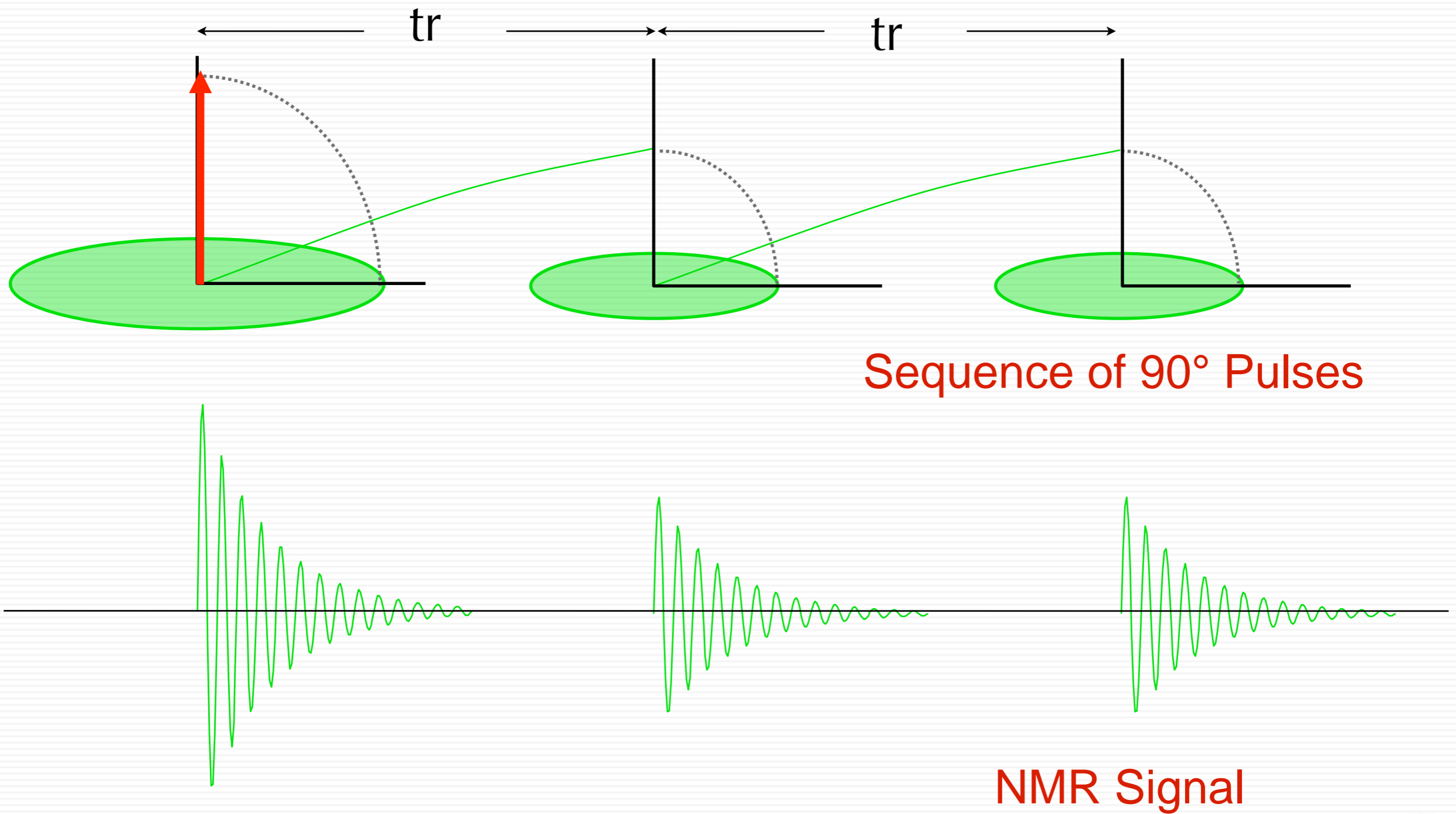
Sequence of 90° Pulses



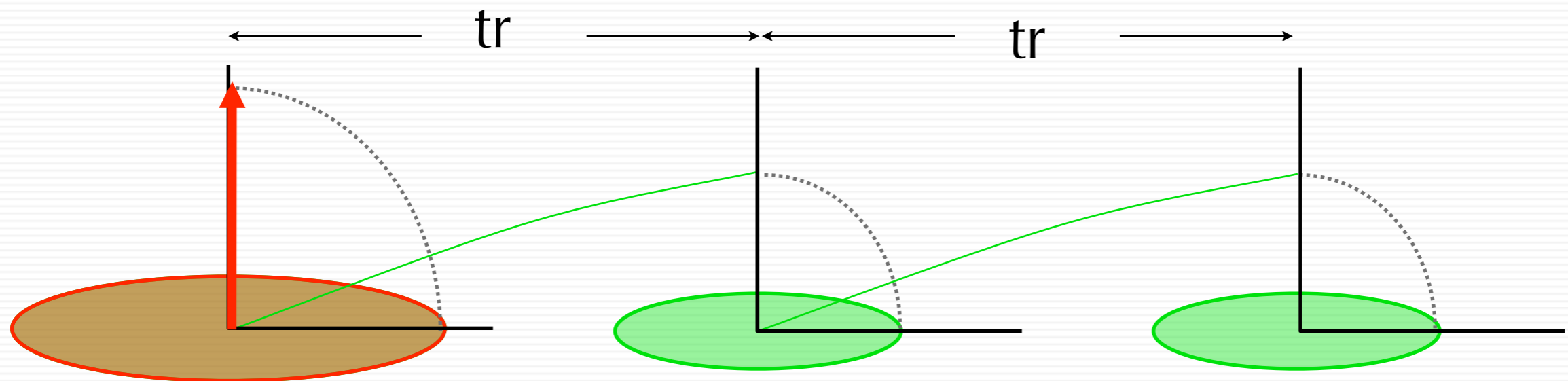
NMR Signal



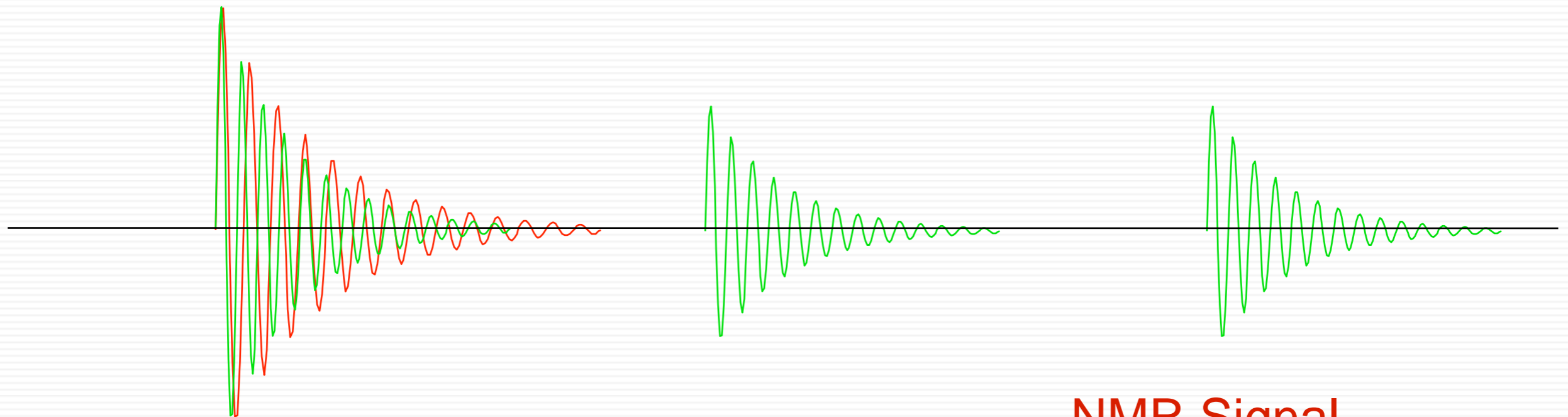
Partial Saturation Sequence



Partial Saturation Sequence



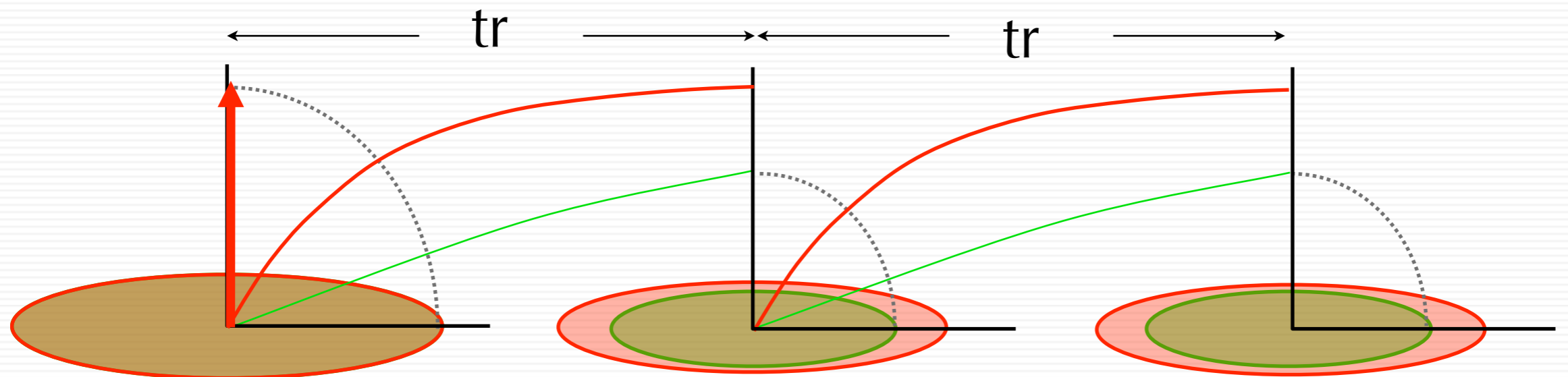
Sequence of 90° Pulses



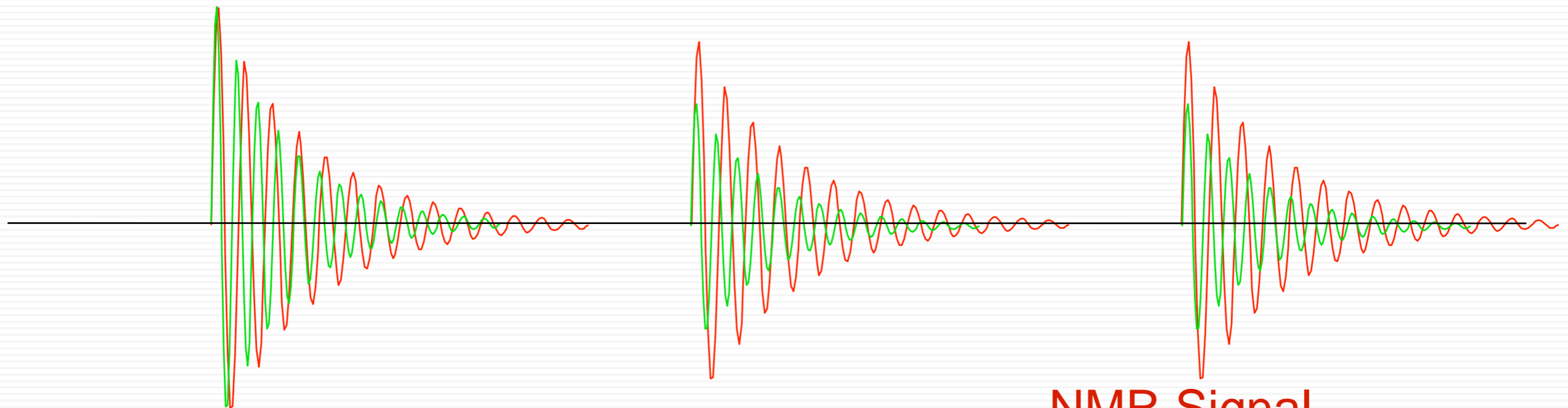
NMR Signal



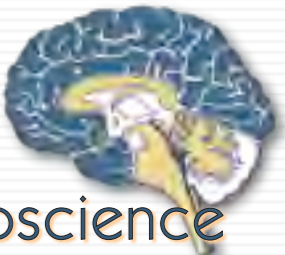
Partial Saturation Sequence



Sequence of 90° Pulses

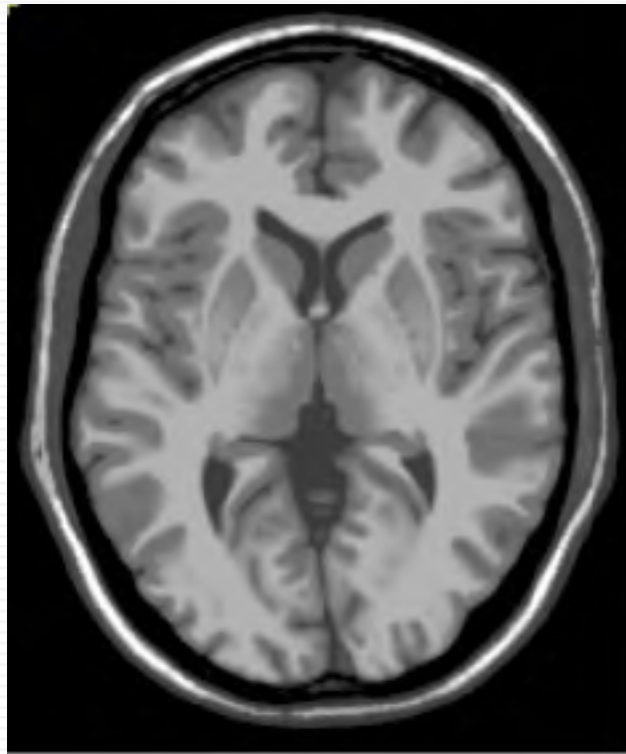


NMR Signal

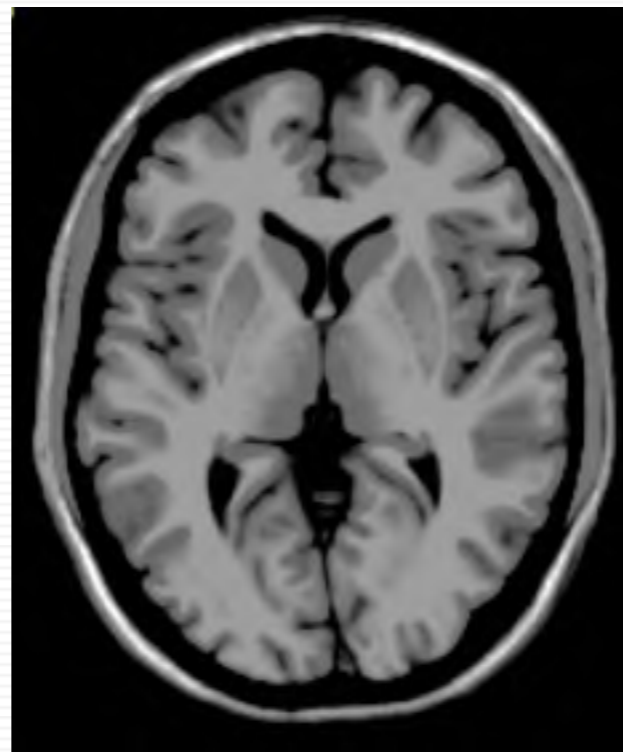


tr and contrast (simulations)

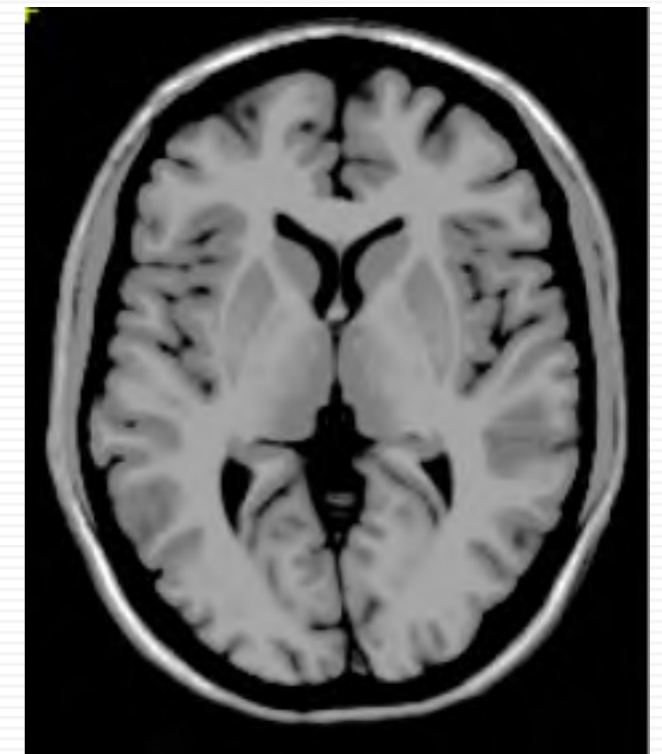
te=4



tr=100

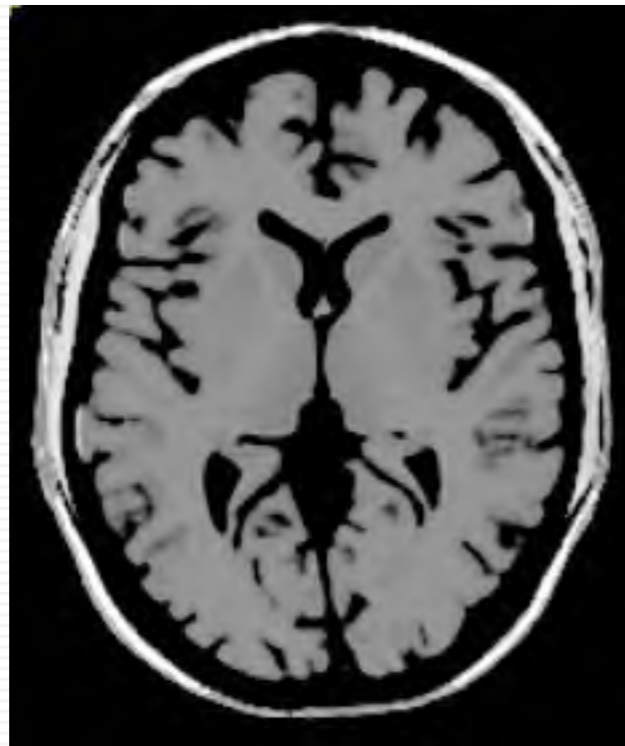


tr=400

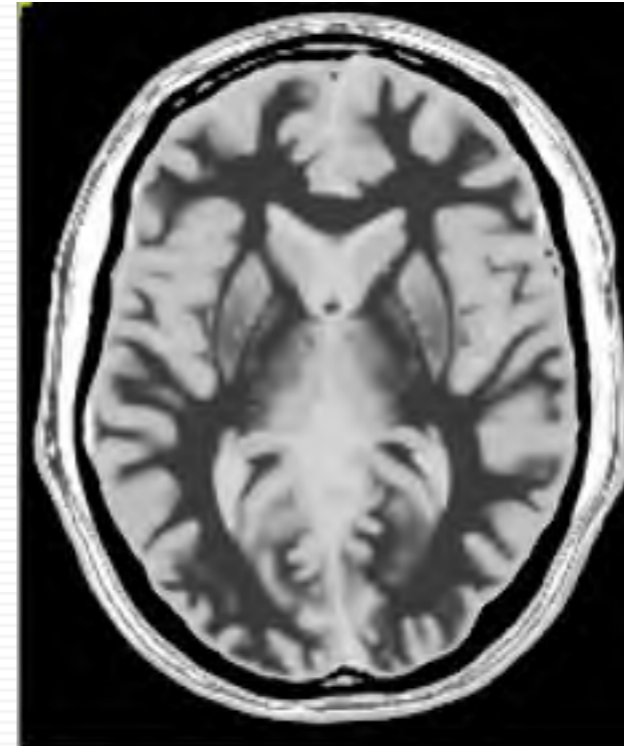


tr=700

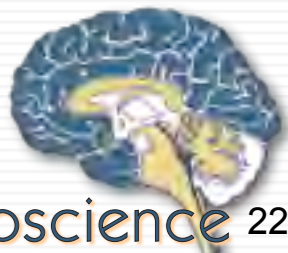
tr=1500



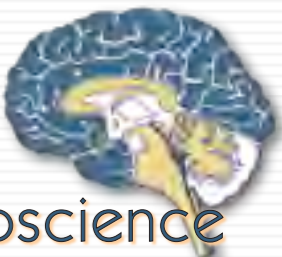
tr=400



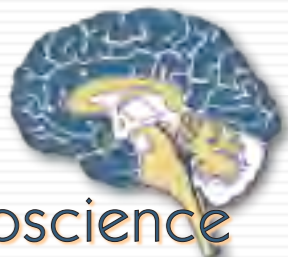
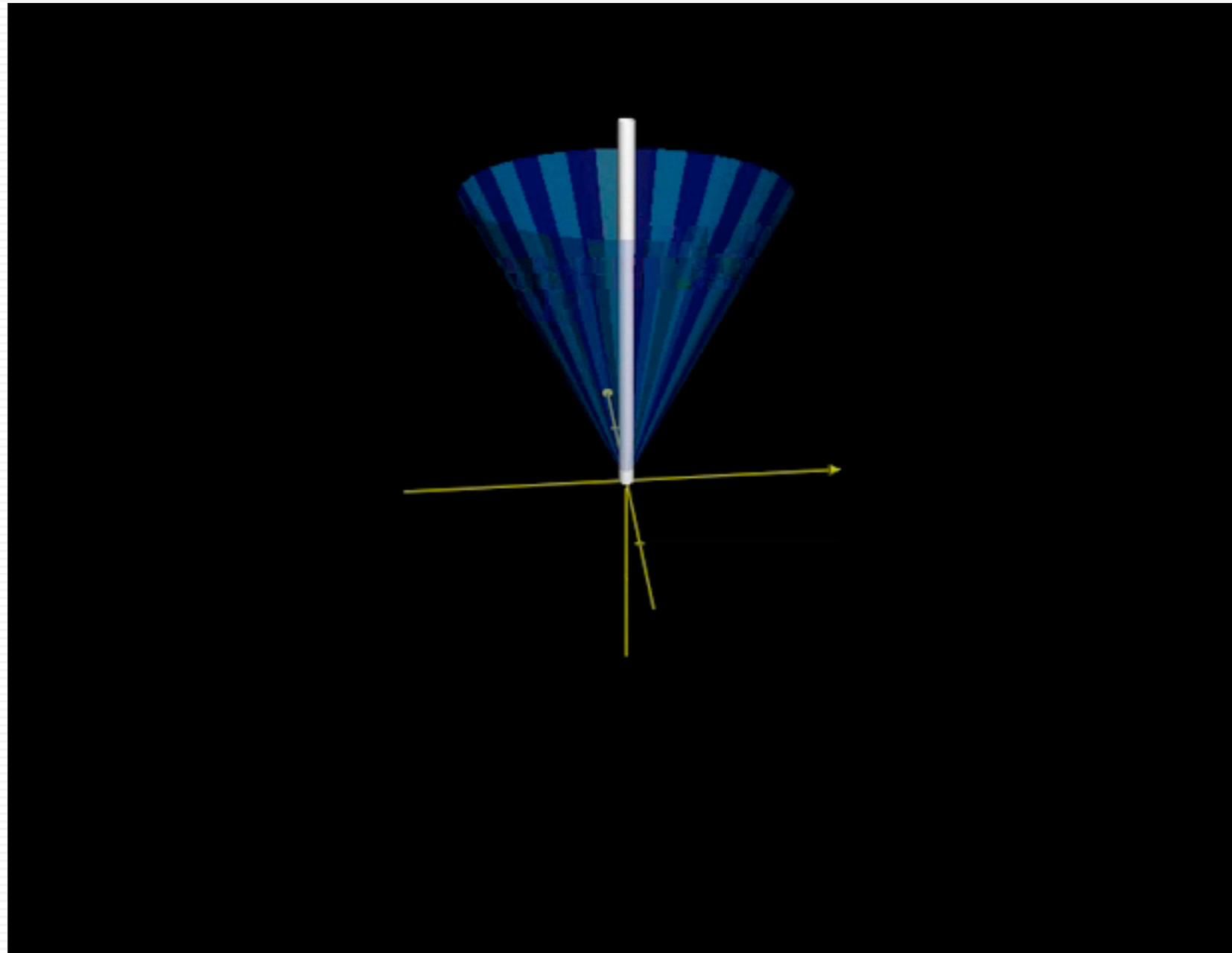
tr=5000



Signal Decay from Dephasing



Signal Decay from Dephasing



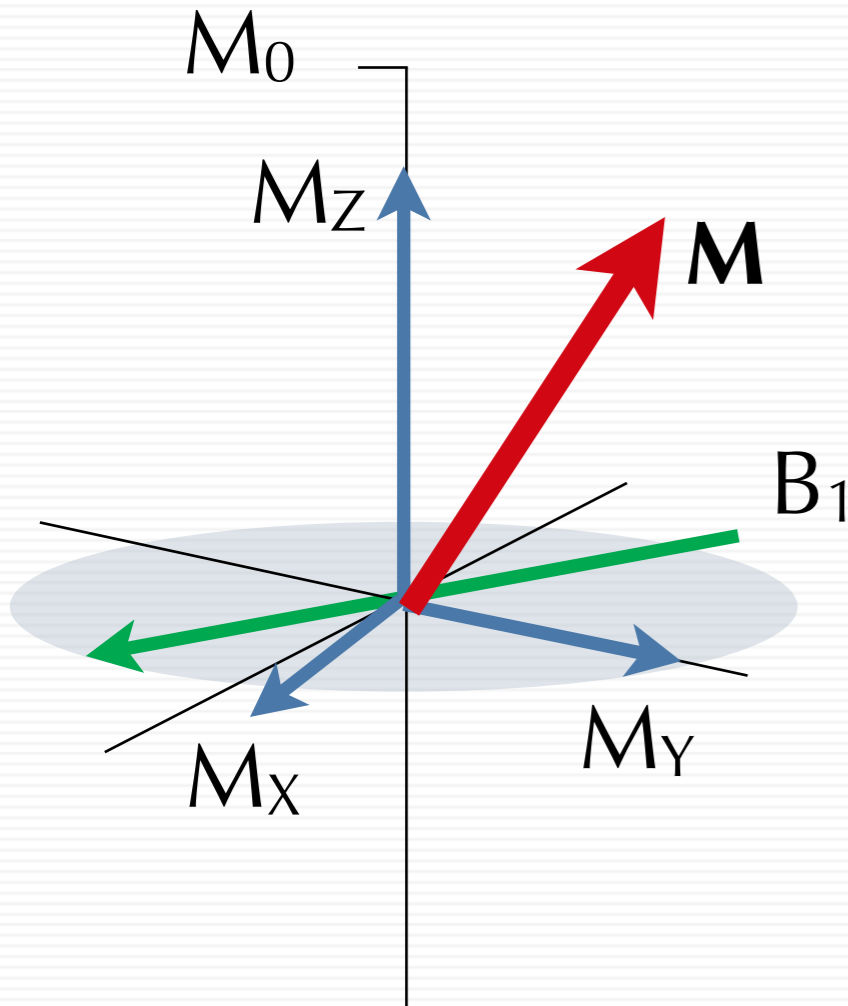
Bloch Equation

$$\blacksquare \frac{d\mathbf{M}}{dt} = \gamma \mathbf{M} \times \mathbf{B}_1 + (\mathbf{M}_0 - \mathbf{M}_z)/T_1 - (\mathbf{M}_x + \mathbf{M}_y)/T_2$$

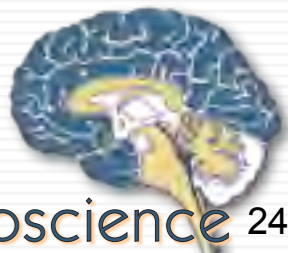
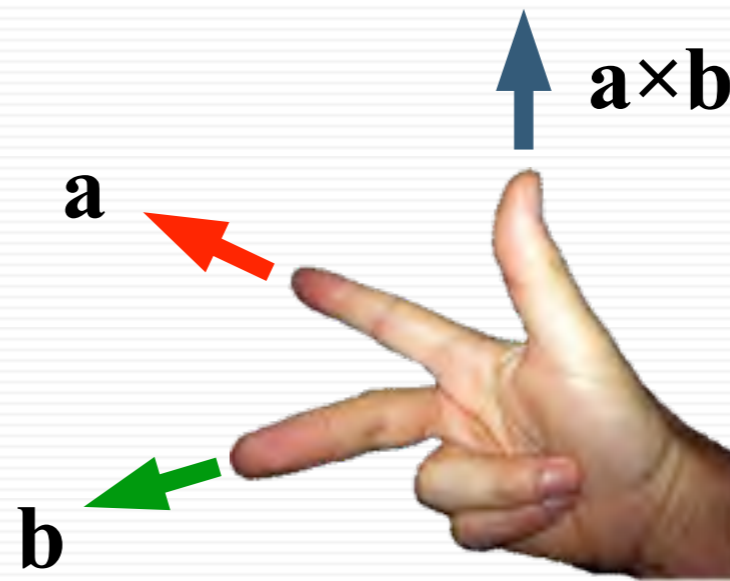
*Nutation &
precession*

*Longitudinal
relaxation*

*Transverse
relaxation*

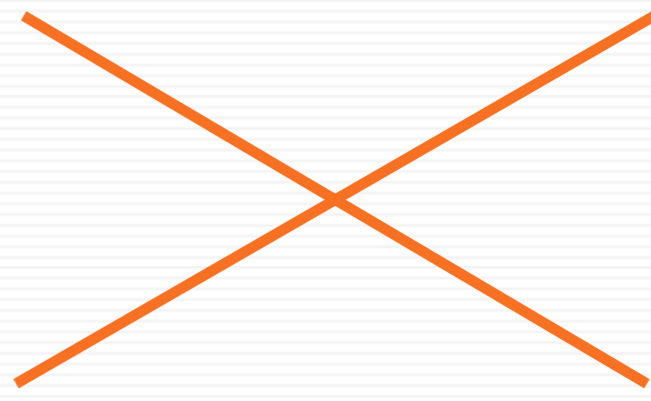


$$\mathbf{a} \times \mathbf{b} = ab \sin \theta \hat{\mathbf{n}}$$

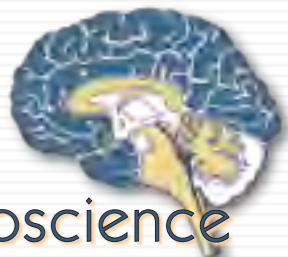


Contrast, TR and TE

$$S = k\rho M_0 (1 - e^{-tr/T_1})e^{-te/T_2}$$

tr	Long	Proton Density	T2-Weighted
	Short	T1-Weighted	
		Short	Long

te

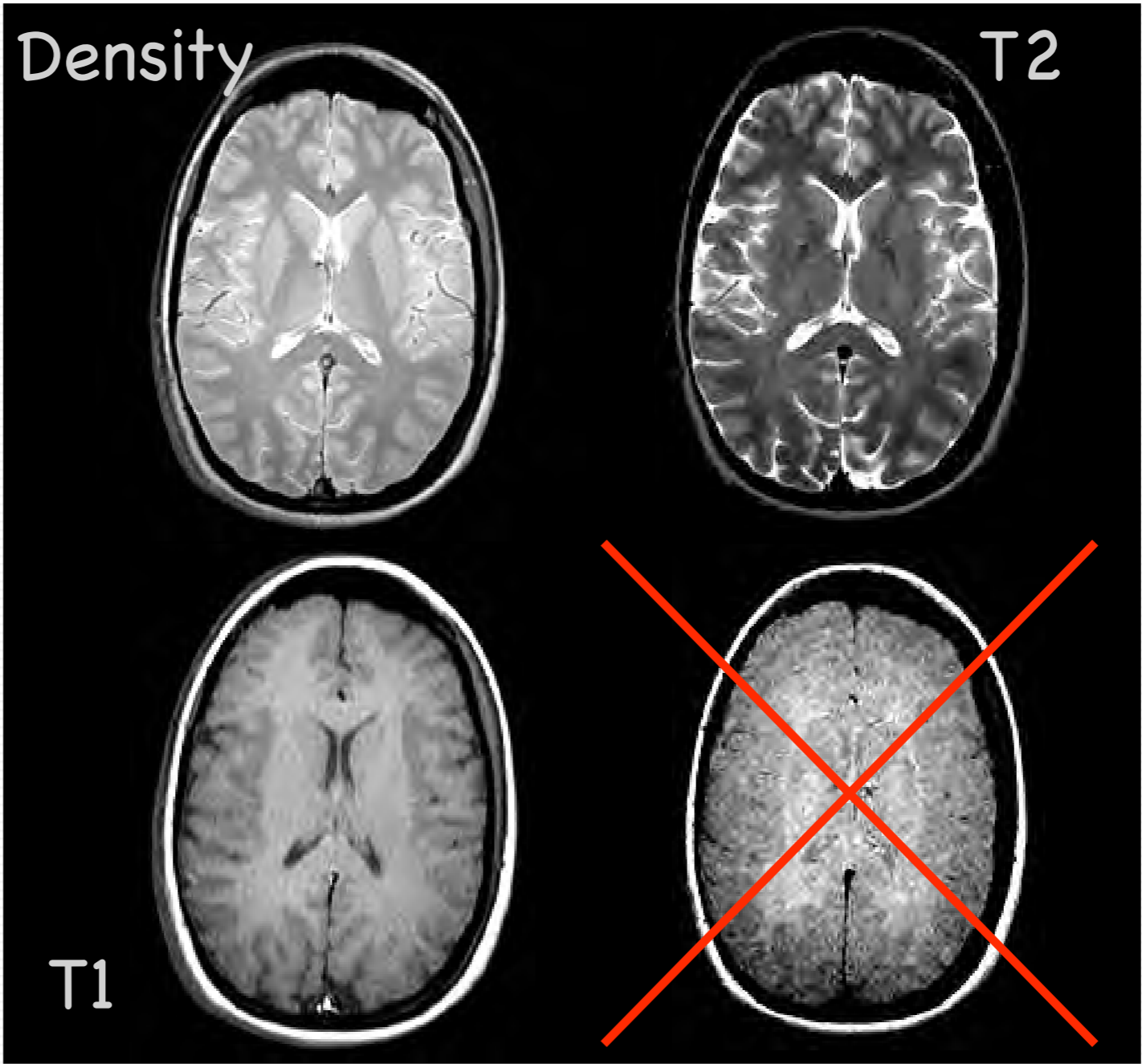


Contrast, TR and TE

Long

TR

Short



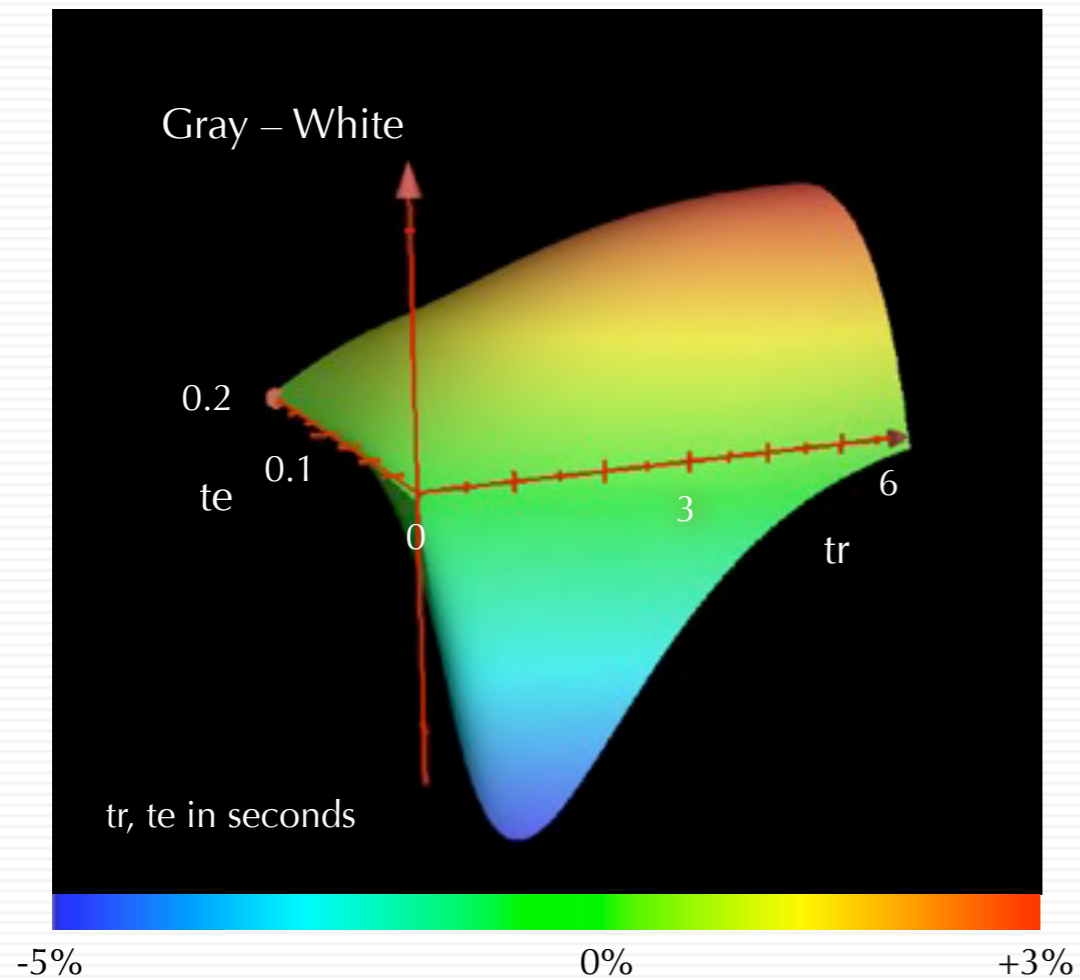
Short

TE

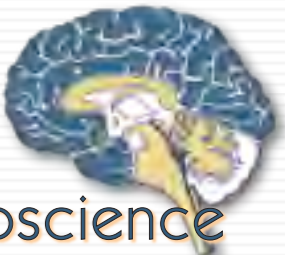
Long



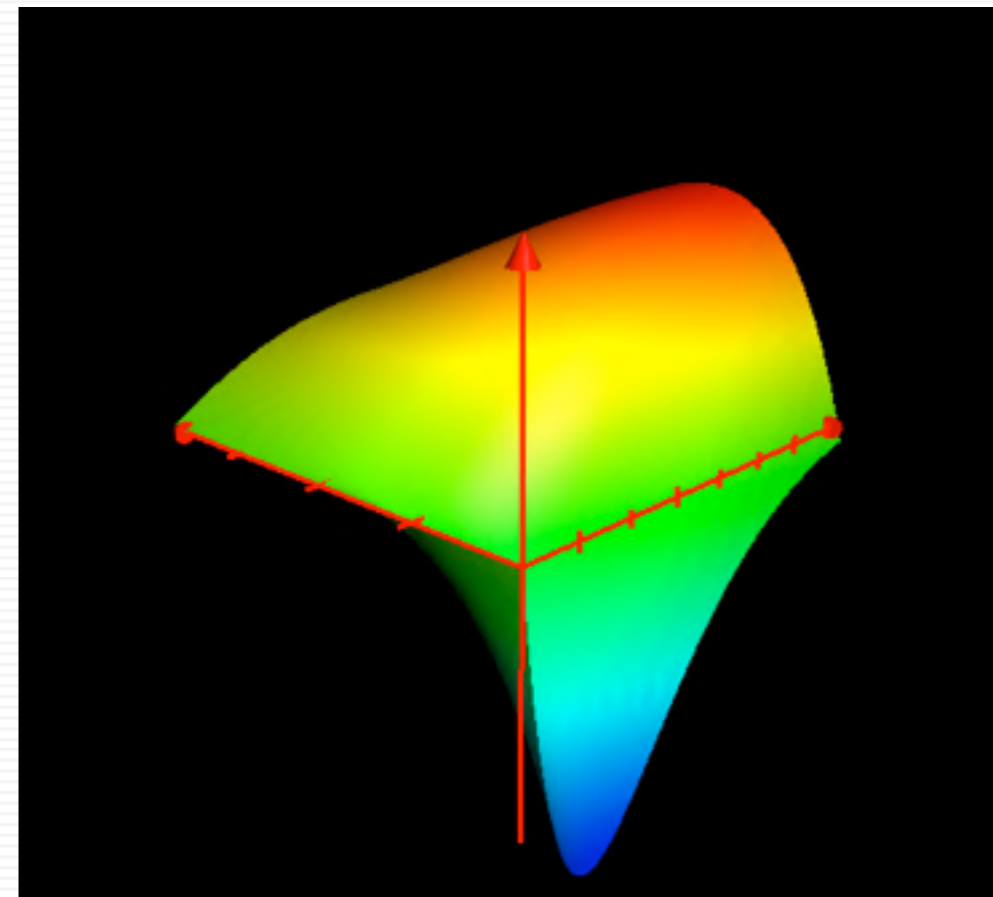
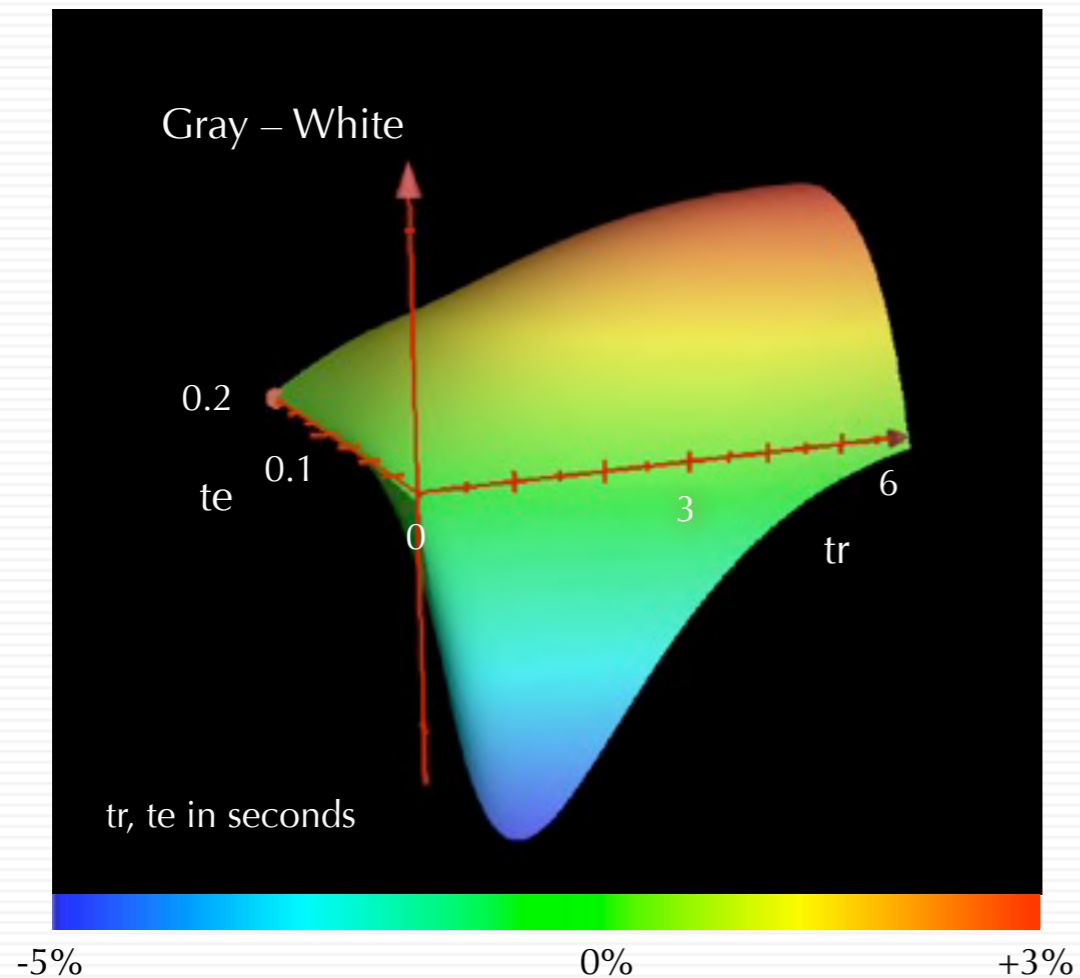
Contrast to Noise Ratio (Gray-White)



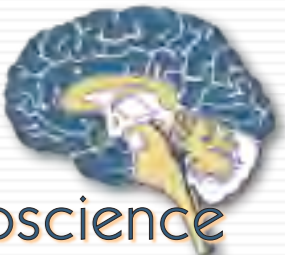
$$\text{Contrast} = [(1 - e^{-tr/1.2})e^{-te/.08}], \text{ gray matter}$$
$$- [(1 - e^{-tr/1.0})e^{-te/.07}], \text{ white matter}$$



Contrast to Noise Ratio (Gray-White)



$$\text{Contrast} = [(1 - e^{-tr/1.2})e^{-te/.08}], \text{ gray matter}$$
$$- [(1 - e^{-tr/1.0})e^{-te/.07}], \text{ white matter}$$



T2*

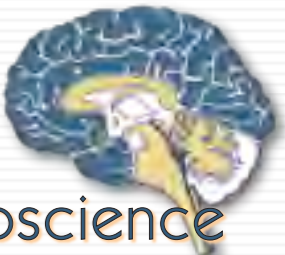
the Observed Transverse Relaxation Rate, $T2^*$, is the sum of several components:

$$\frac{1}{T2^*} = \frac{1}{T2} + \frac{1}{T2'} + \frac{1}{T2_D} + \dots$$

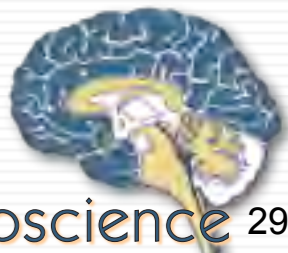
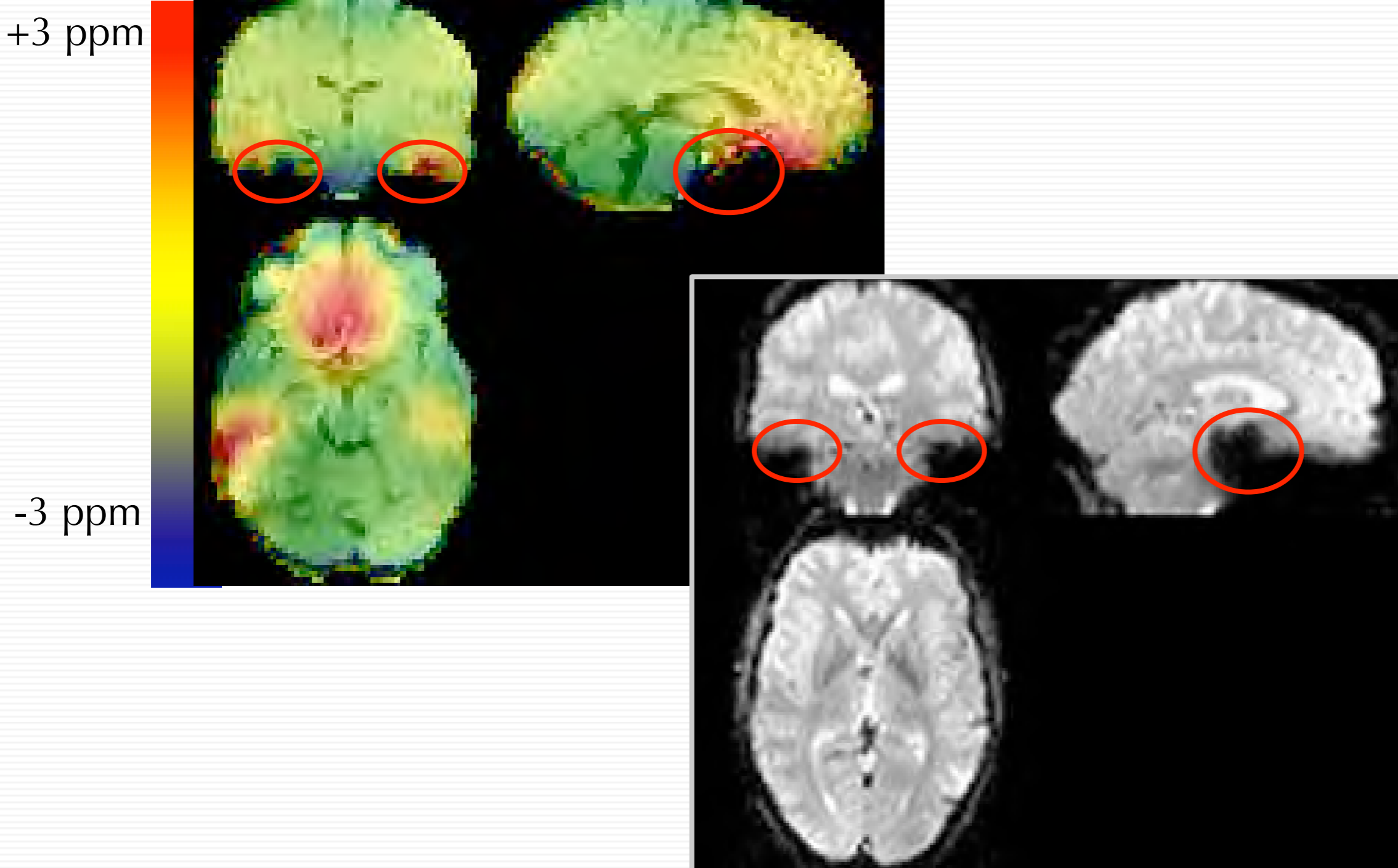
Molecular

Field
Inhomogeneity

Diffusion



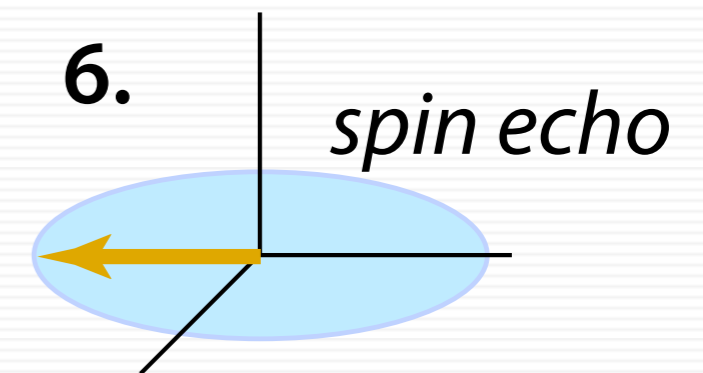
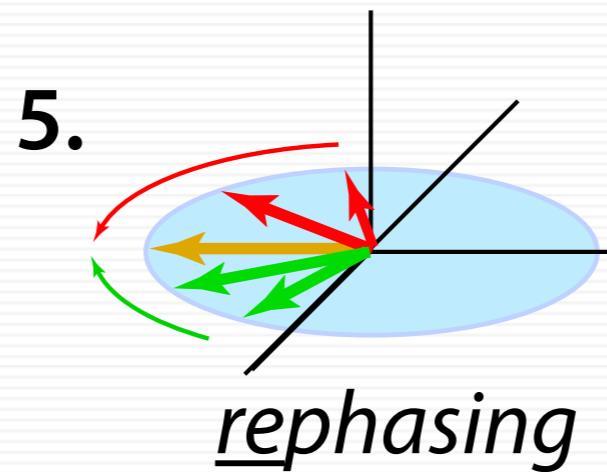
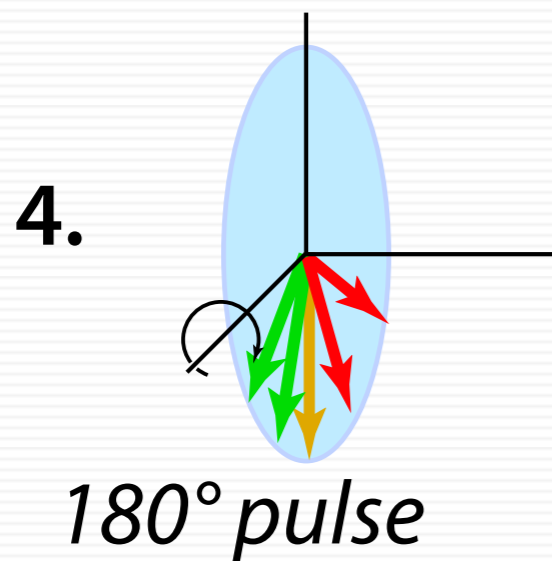
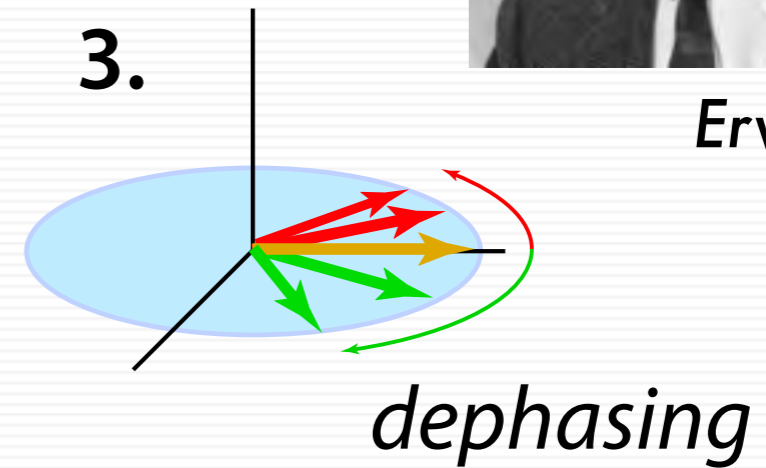
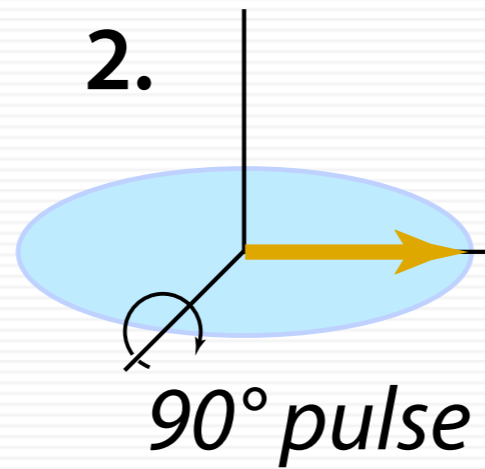
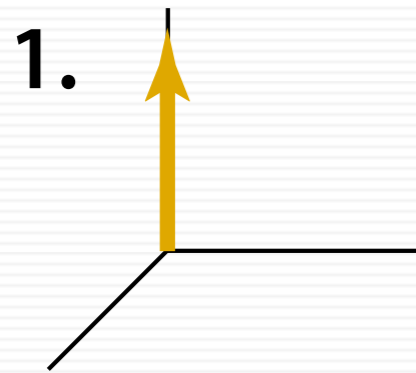
Local field Variations Result in Signal Loss



Hahn Spin Echo



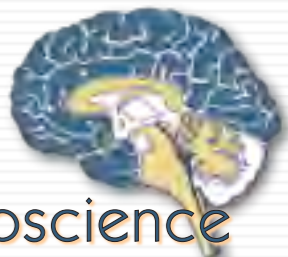
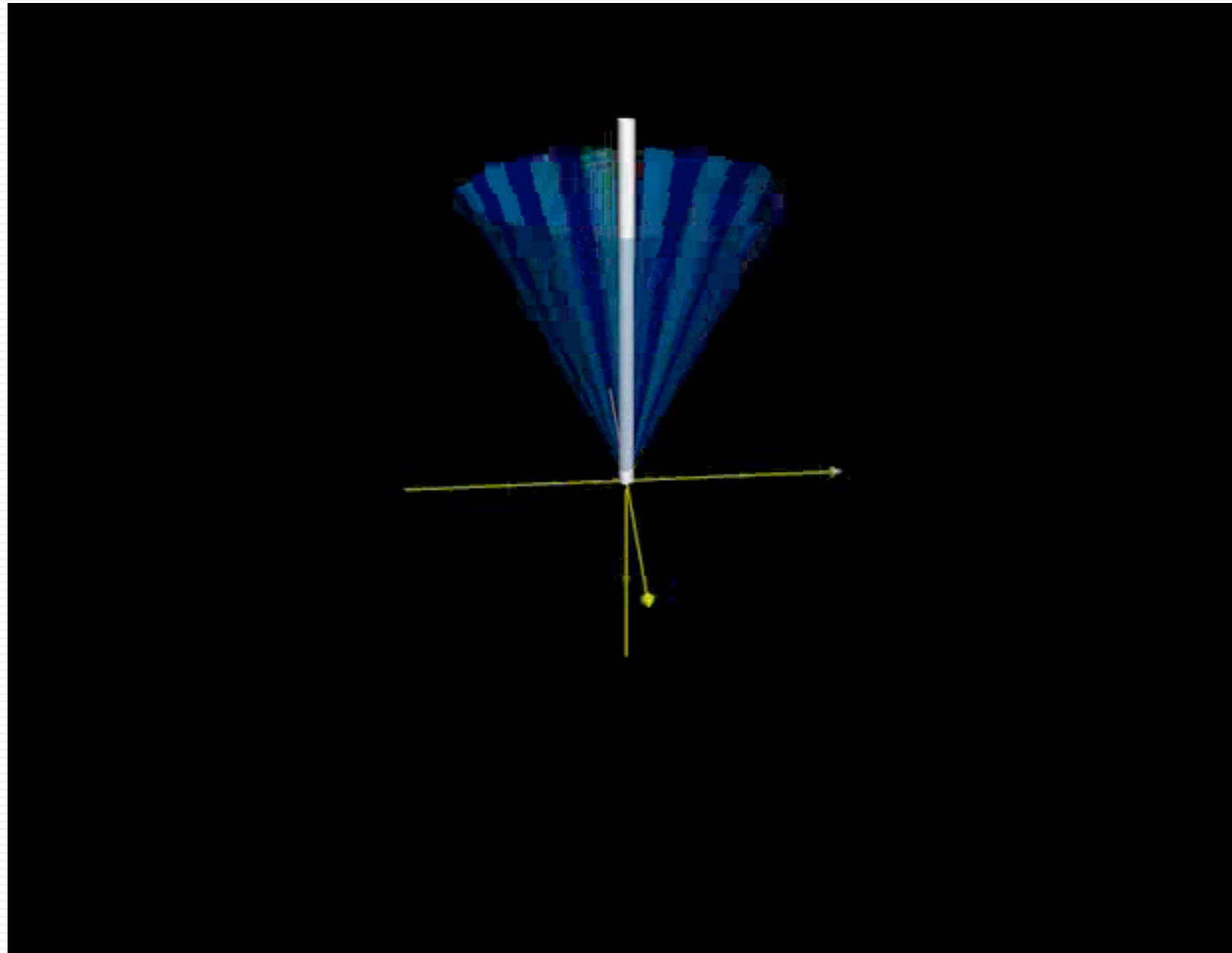
Erwin Hahn



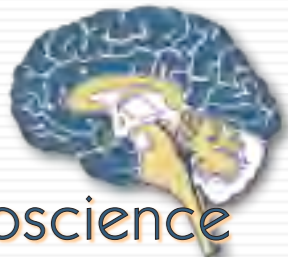
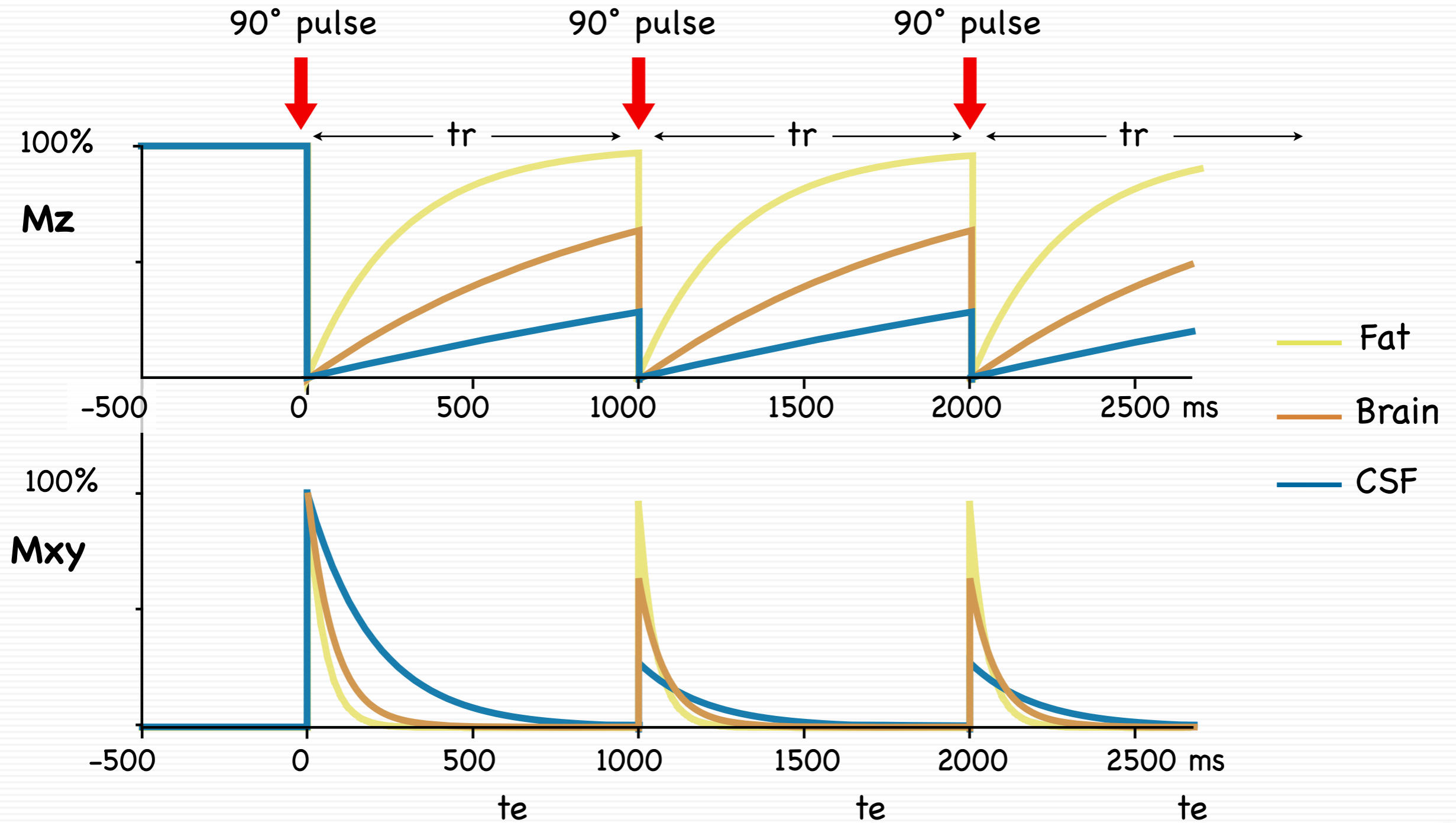
Hahn Spin Echo



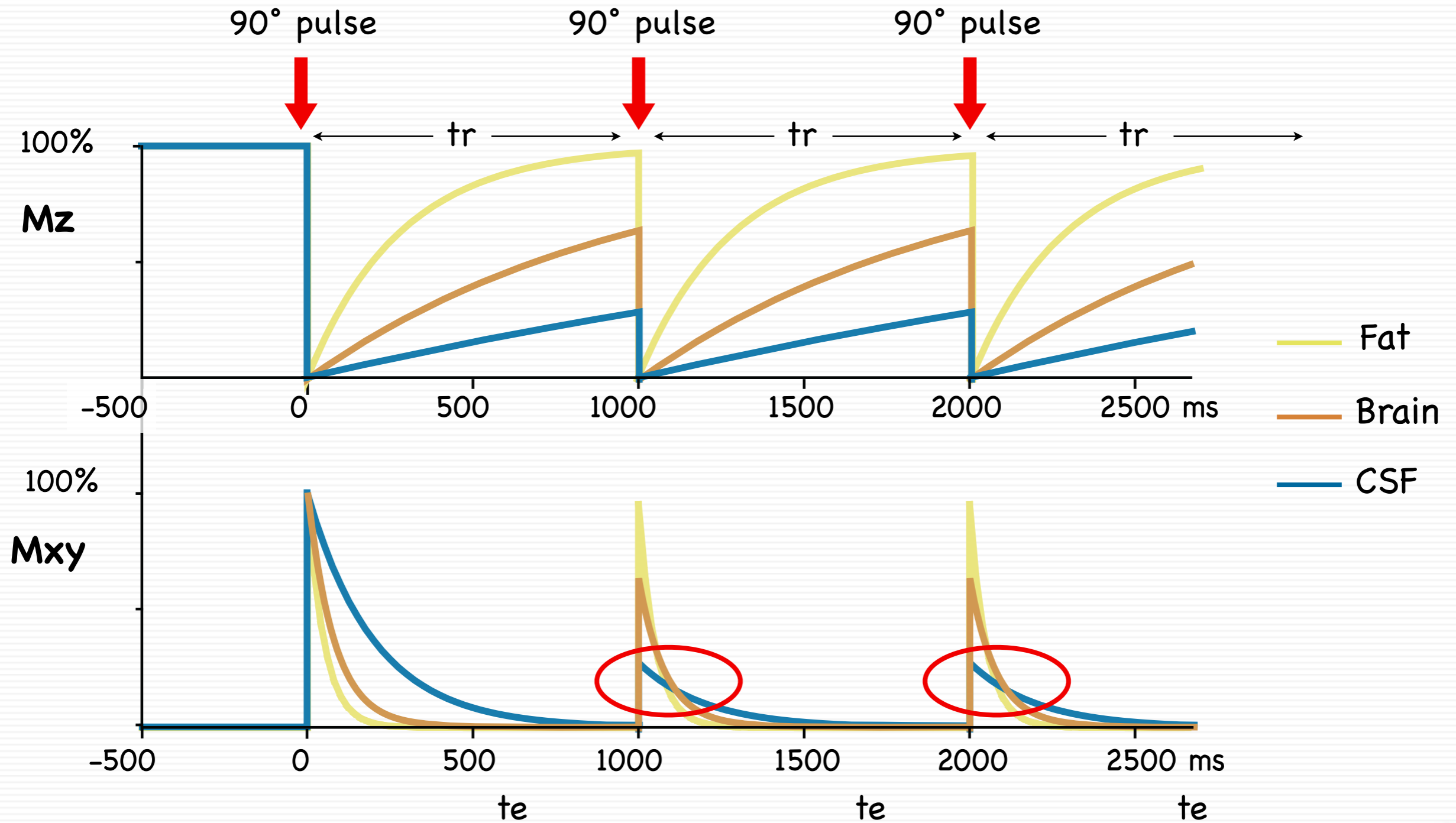
Hahn Spin Echo



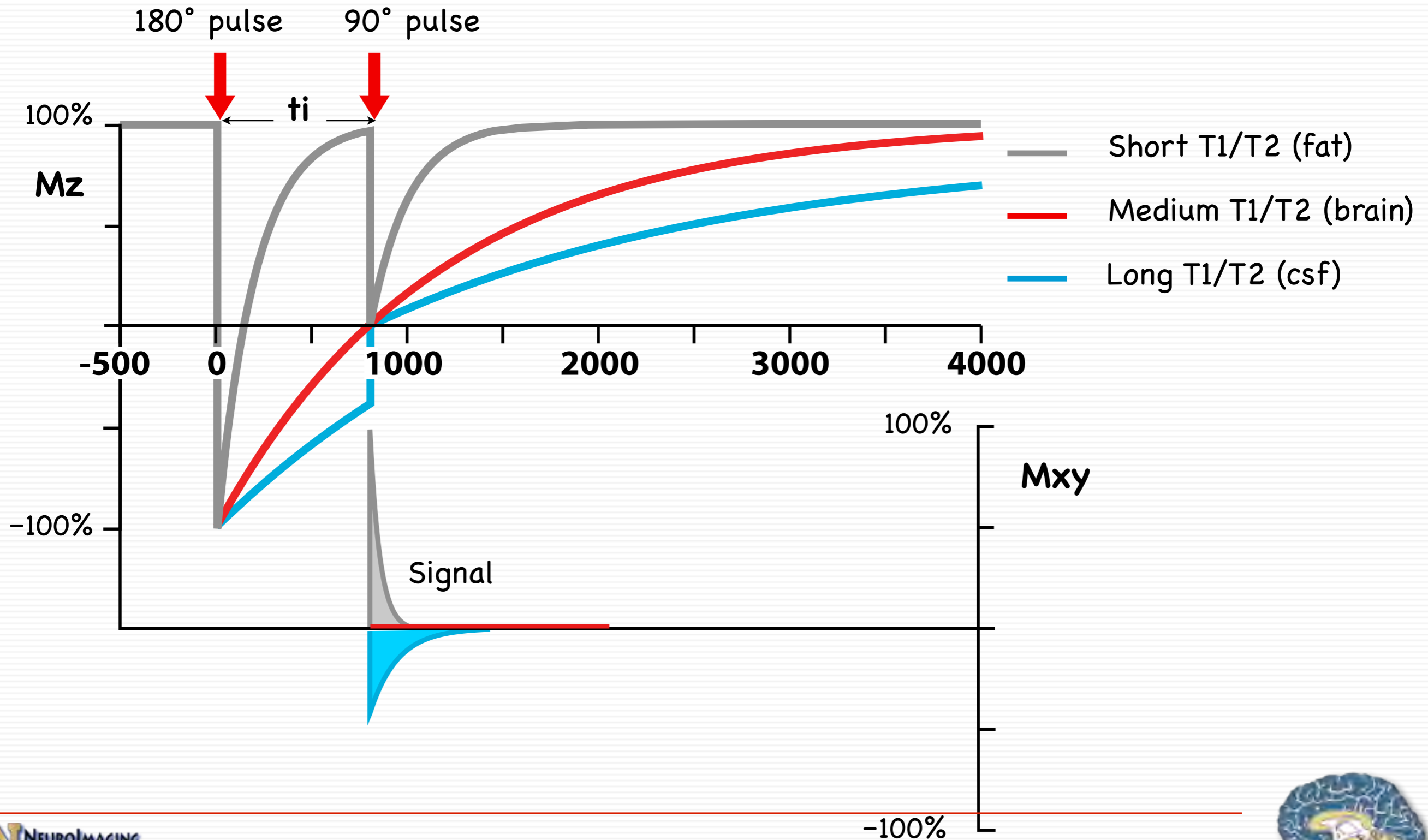
Longitudinal & Transverse Magnetization



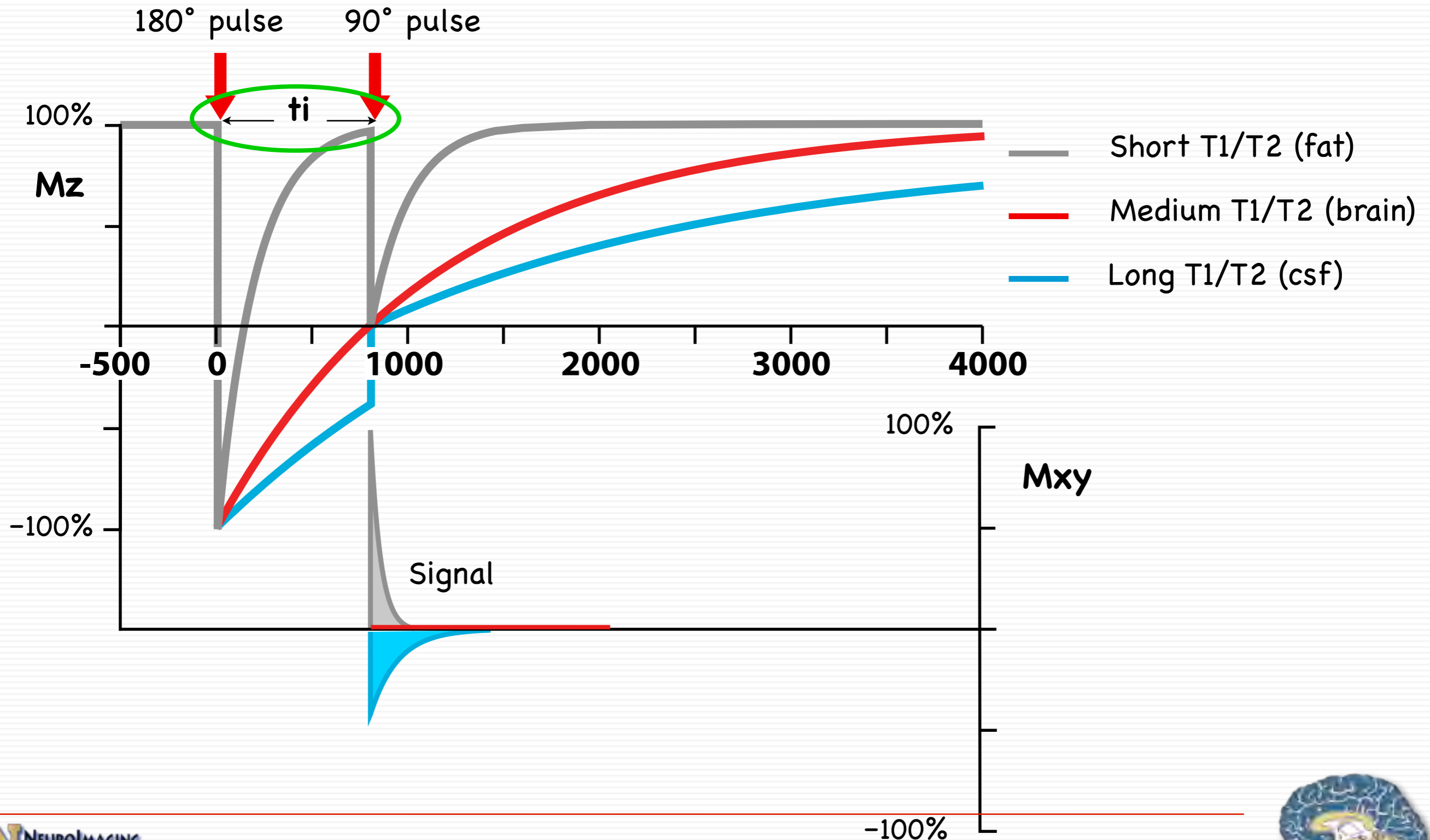
Longitudinal & Transverse Magnetization



Inversion Recovery



Inversion Recovery



3D T1 Images

TE = 3.2

TR = 14.4

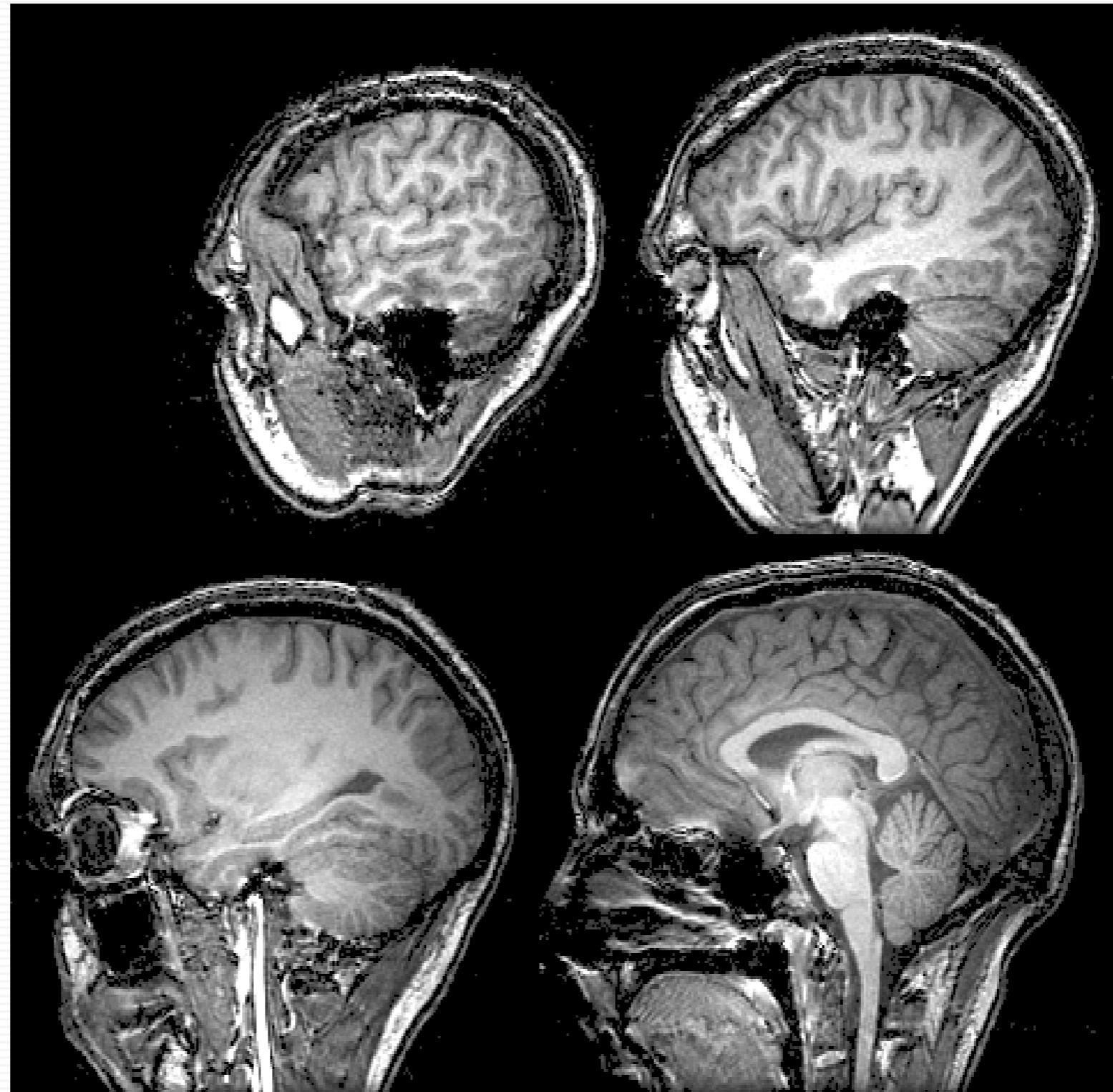
124 slices

1.25 mm thick

1 NEX

Flip Angle 20°

TI = 500



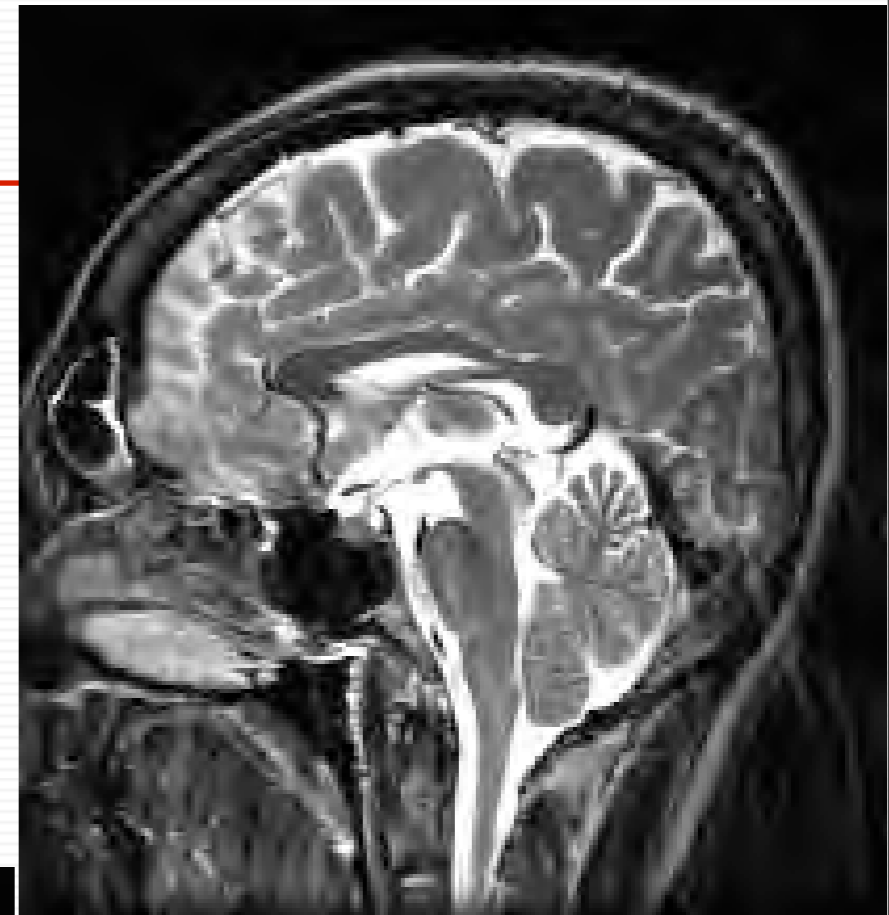


Proton Density

Sample Data Set (normal)

Fast Spin Echo

3 mm Slices



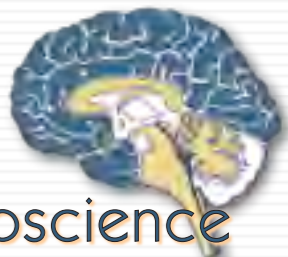
T2-weighted



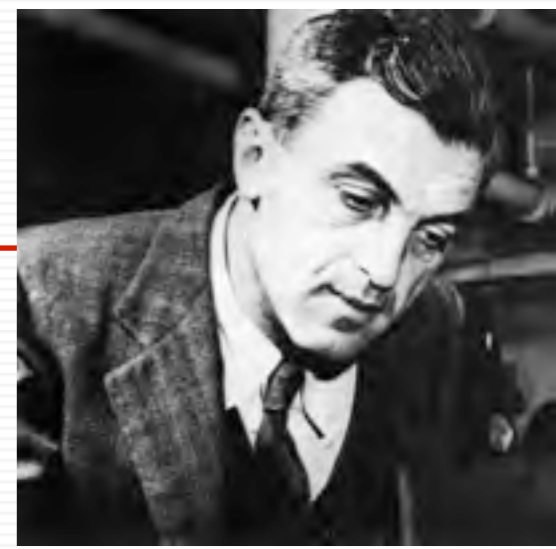
T1-weighted

3D IR-SPGR
TE = 3.2, TI = 700

Sample Data Set (normal)



MR Formulæ



Felix Bloch

$$\text{Spin Echo Signal} = k\rho M_0(1 - e^{-tr/T1})e^{-te/T2}$$

Inversion Recovery Signal =

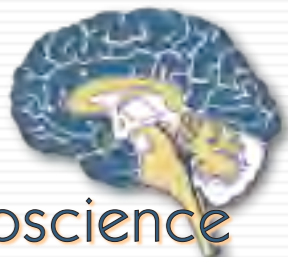
$$k\rho M_0(1 - 2e^{-ti/T1} + e^{-tr/T1})e^{-te/T2}$$

ρ is the proton density

k represents instrument effects

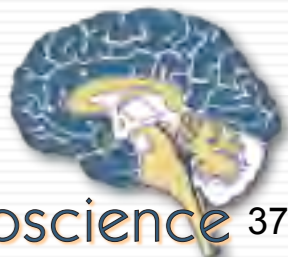
The “Bloch” Equation:

$$d\mathbf{M}/dt = \gamma\mathbf{M} \times \mathbf{B}_1 + (\mathbf{M}_0 - \mathbf{M}_z)/T_1 - (\mathbf{M}_x + \mathbf{M}_y)/T_2$$



MRI Contrast Summary

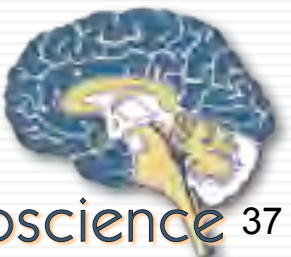
...next: Making an Image



MRI Contrast Summary

- Pulses of Rotating Magnetic Fields (RF) Convert Nuclear Magnetization to Signal

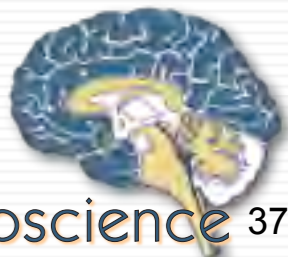
...next: Making an Image



MRI Contrast Summary

- Pulses of Rotating Magnetic Fields (RF) Convert Nuclear Magnetization to Signal
- RF Pulses Add Energy by Displacing Longitudinal Equilibrium

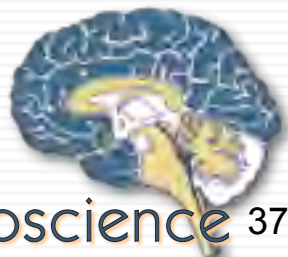
...next: Making an Image



MRI Contrast Summary

- Pulses of Rotating Magnetic Fields (RF) Convert Nuclear Magnetization to Signal
- RF Pulses Add Energy by Displacing Longitudinal Equilibrium
- Contribution of Intrinsic Tissue Properties T1 and T2 Manipulated by Experimenter controlled timing: t_r and t_e respectively.

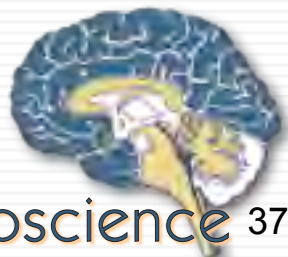
...next: Making an Image



MRI Contrast Summary

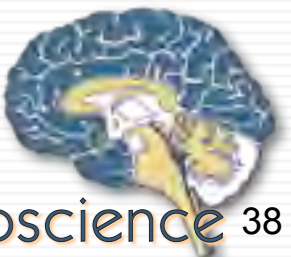
- Pulses of Rotating Magnetic Fields (RF) Convert Nuclear Magnetization to Signal
- RF Pulses Add Energy by Displacing Longitudinal Equilibrium
- Contribution of Intrinsic Tissue Properties T1 and T2 Manipulated by Experimenter controlled timing: t_r and t_e respectively.
- Typically, $0.05 < T1 < 3s$ and $0.005 < T2 < .3s$ for body tissues.

...next: Making an Image

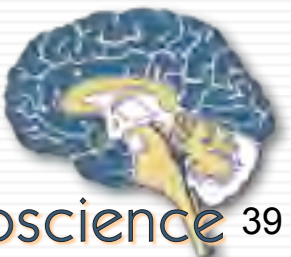


The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
- The “Pulse Sequence” Rules Everything (3)
Seventh Inning Stretch
- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)
- Image Quality and Artifacts (48)

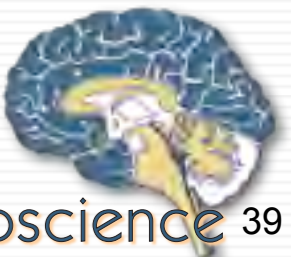


MR Spatial Encoding



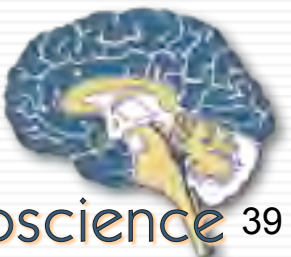
MR Spatial Encoding

- Most MR Spatial encoding is based on a single concept:
 - If the **Magnetic Field** varies by location, the **MR Frequency** will vary by location,
 - Therefore: *We can find the location by measuring the frequency.*

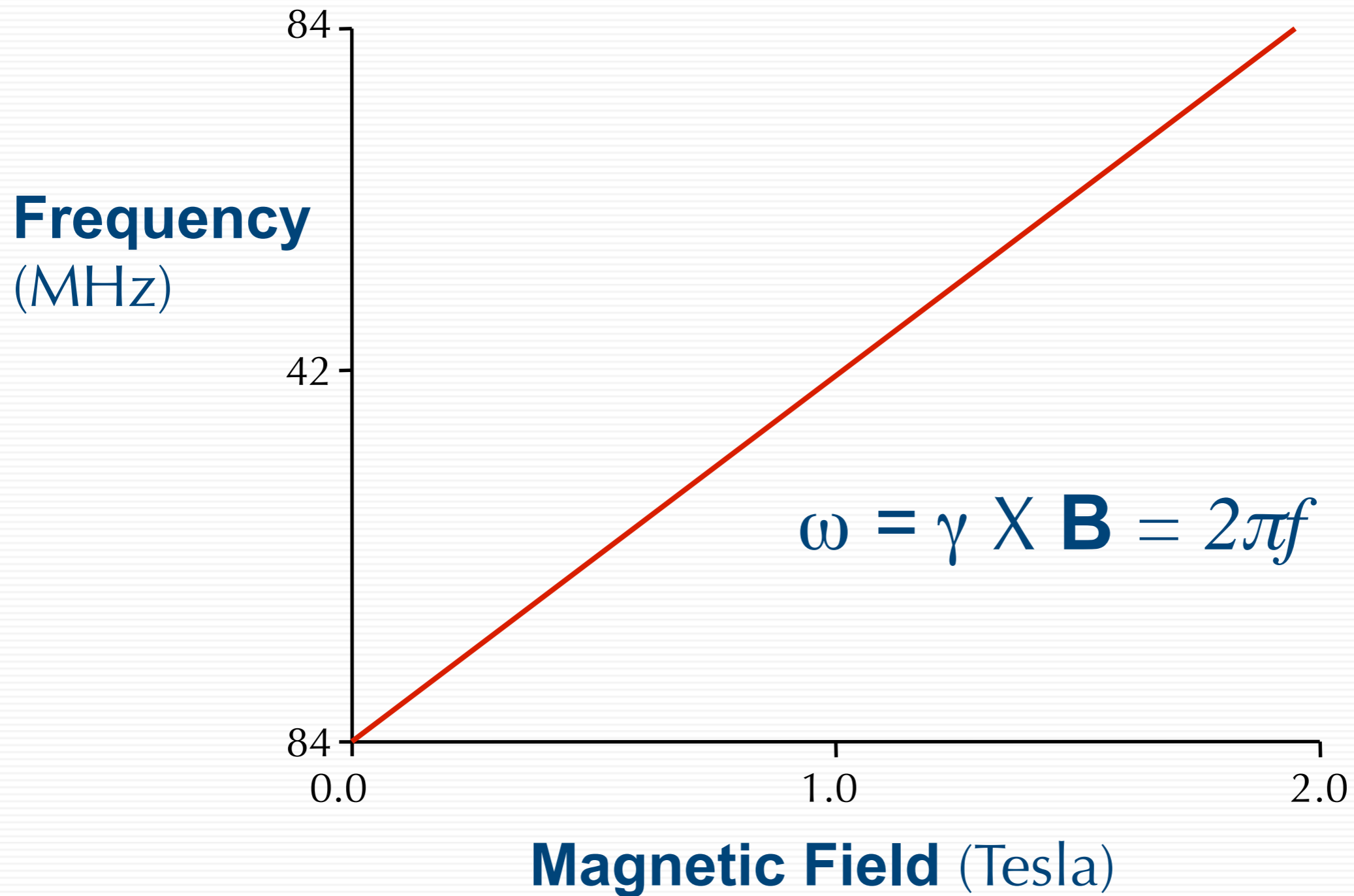


MR Spatial Encoding

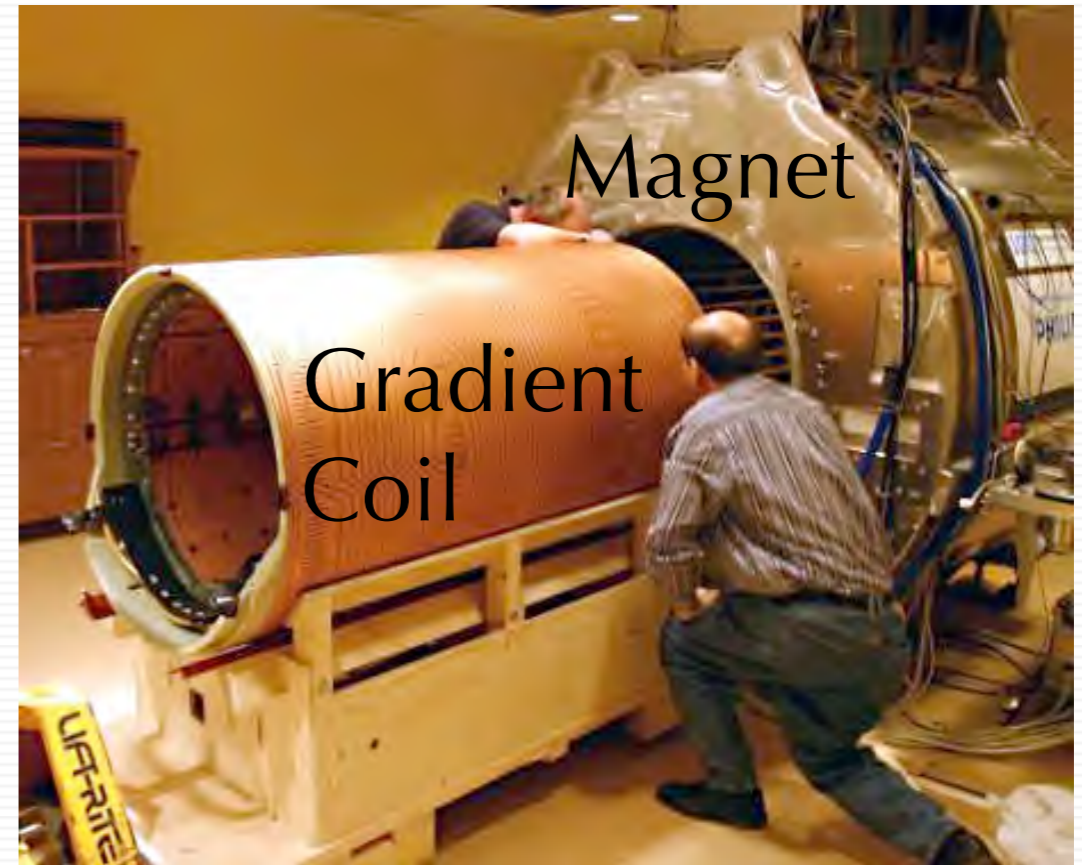
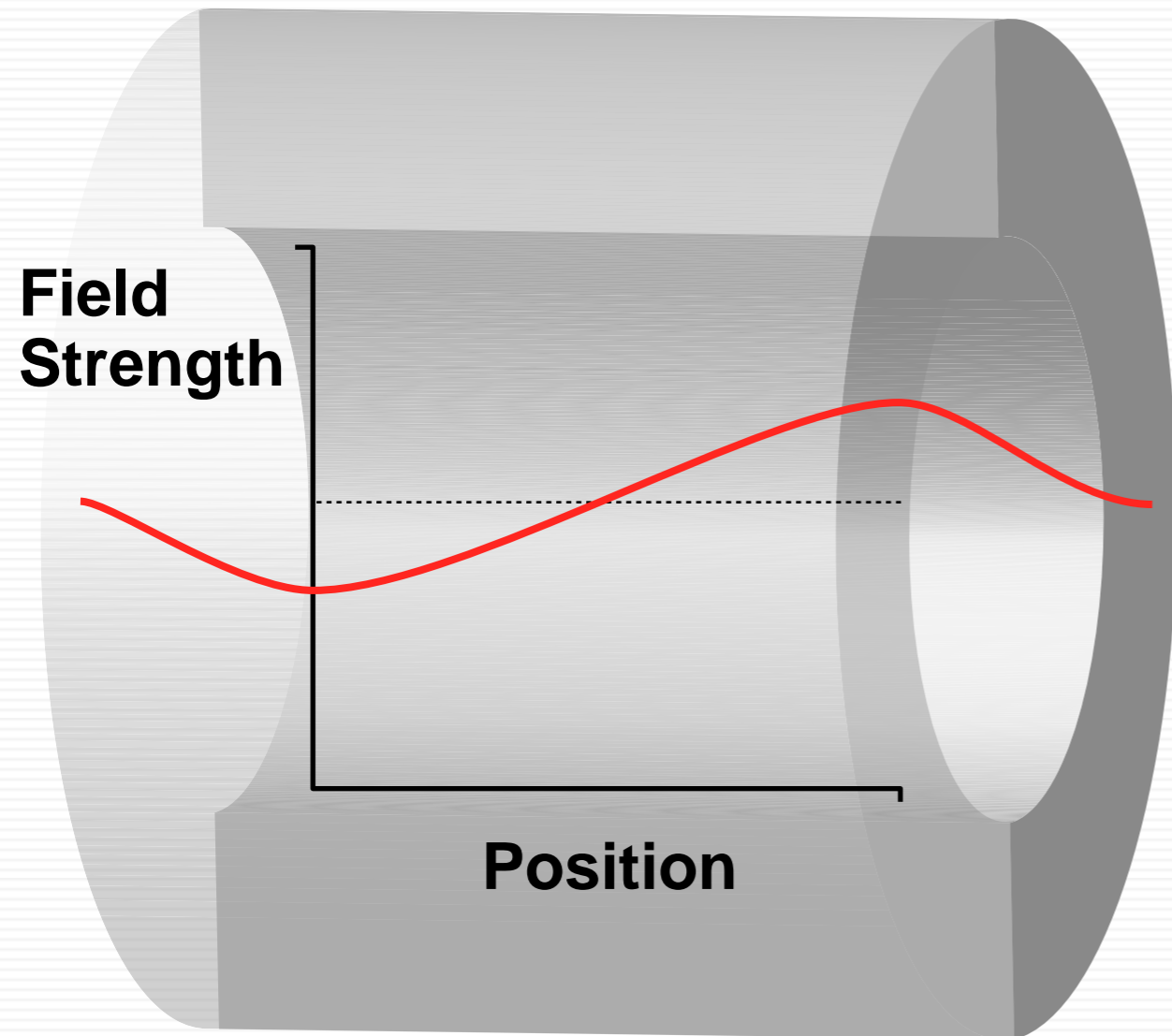
- Most MR Spatial encoding is based on a single concept:
 - If the **Magnetic Field** varies by location, the **MR Frequency** will vary by location,
 - Therefore: *We can find the location by measuring the frequency.*
- Newer methods (e.g., GRAPPA, SENSE) also find location by signal strength as a function of antenna distance



The Larmor Relation



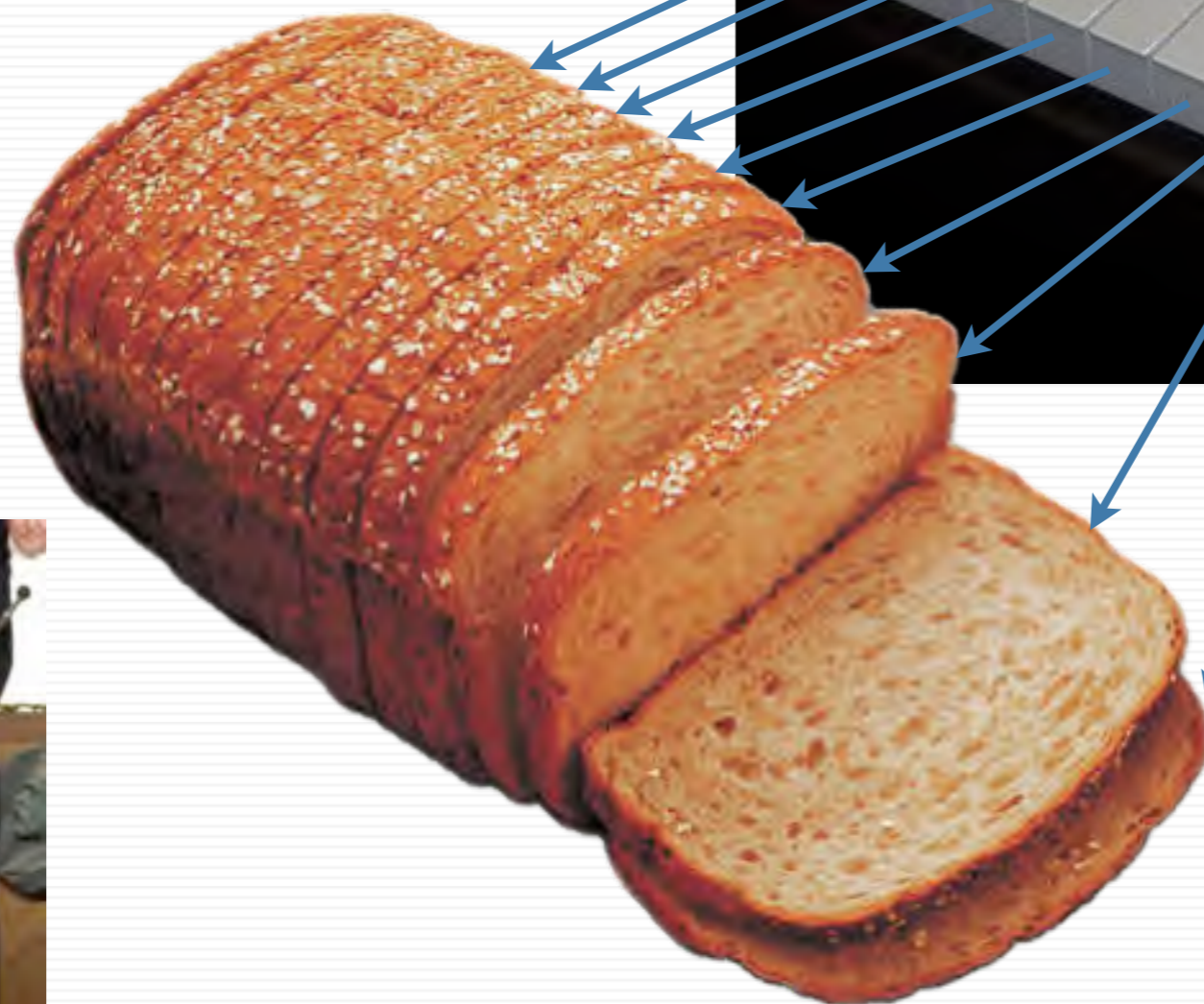
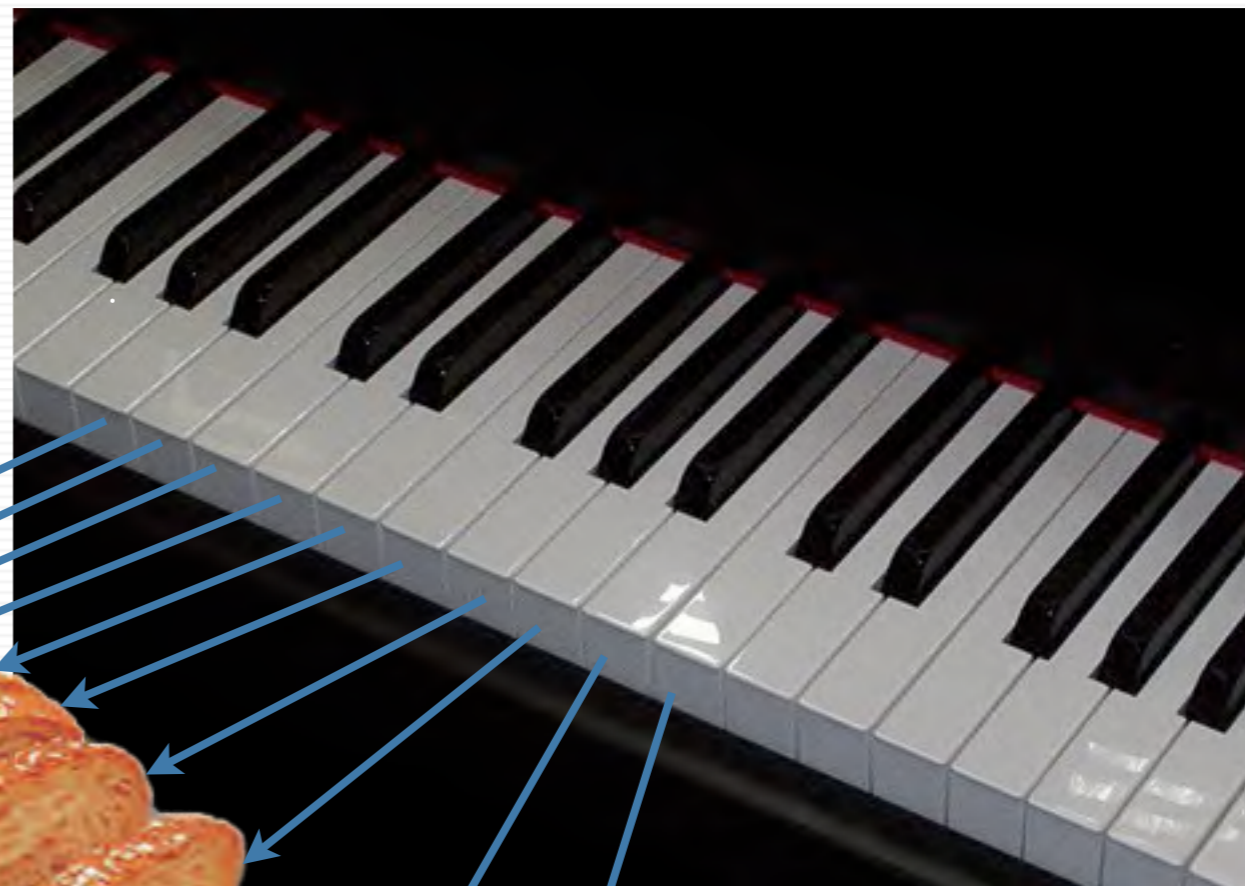
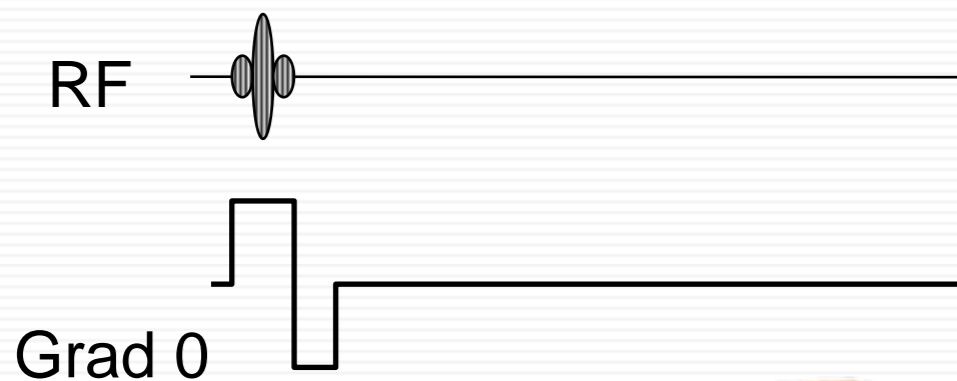
Magnetic Field Gradients



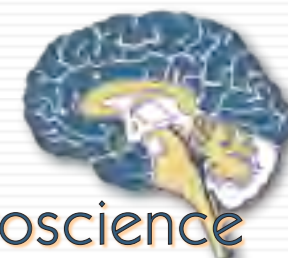
MRI Instrument in Cross Section



Frequency Selective Excitation

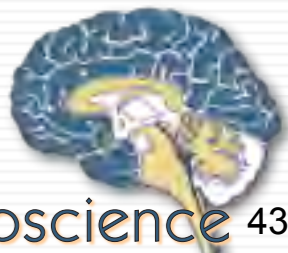
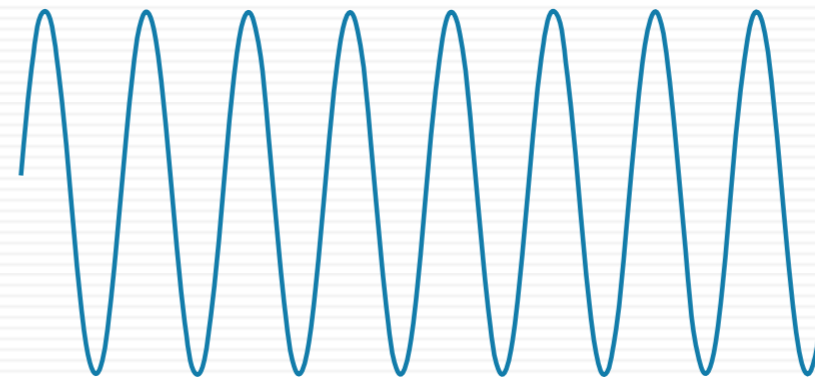
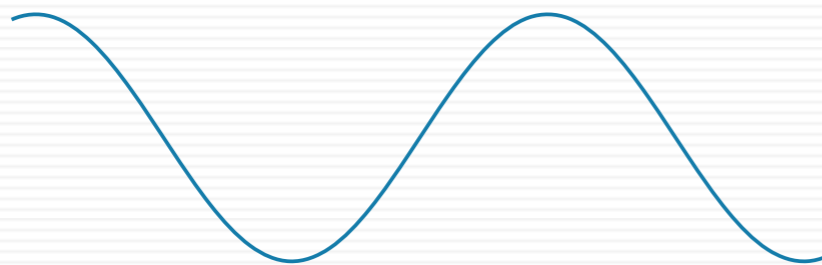
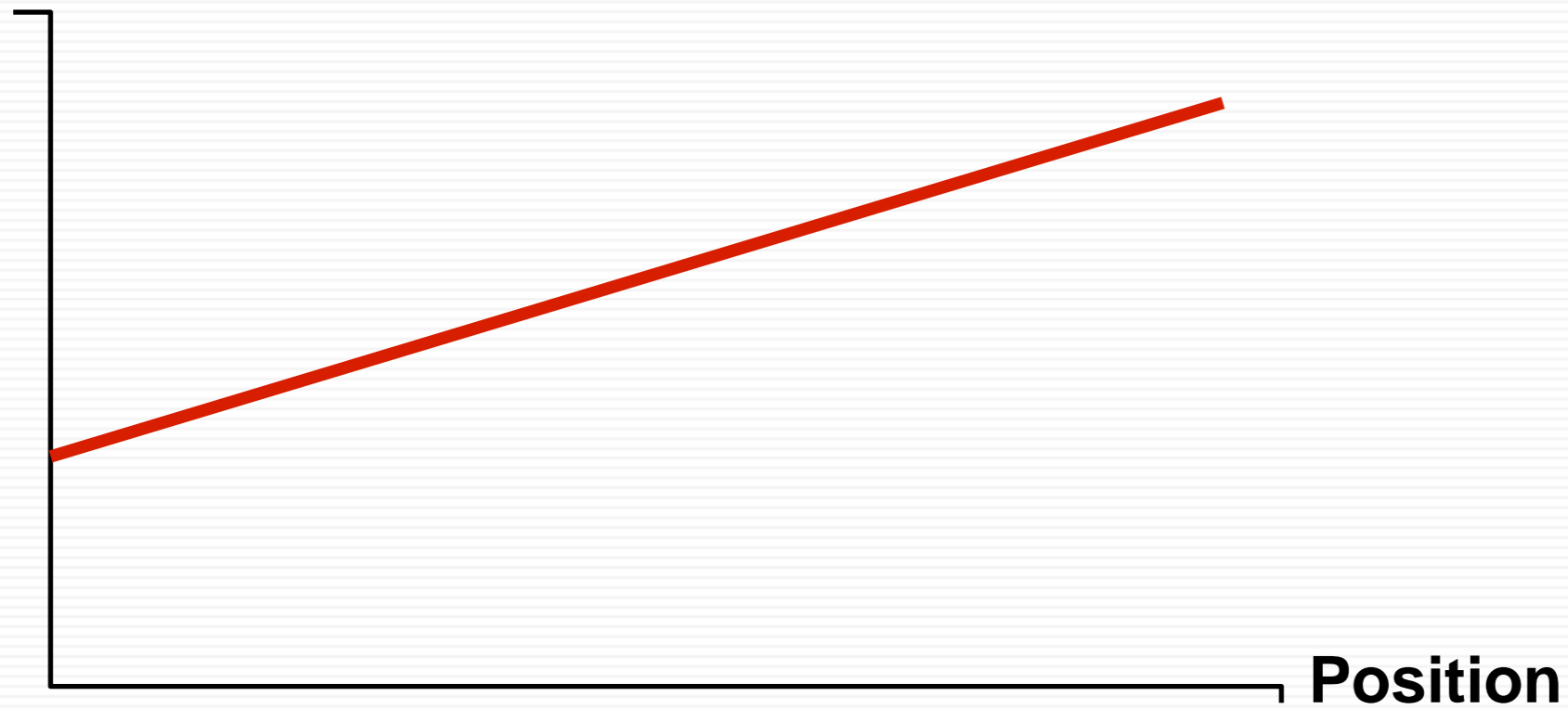


Sir Peter Mansfield

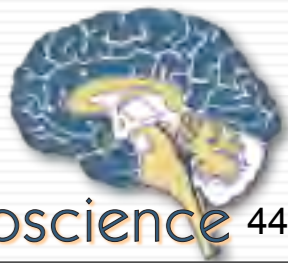
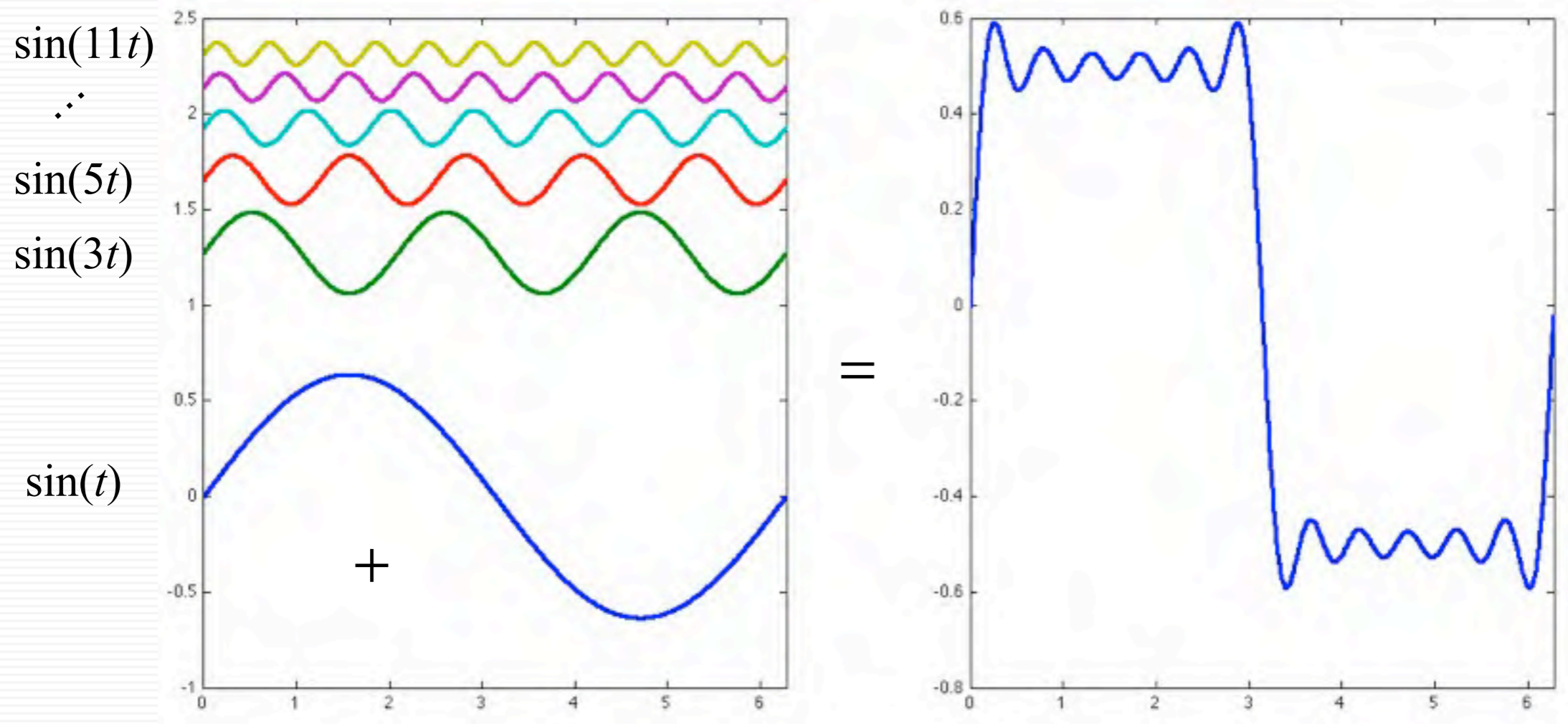


A 1D Image

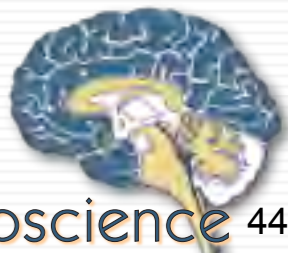
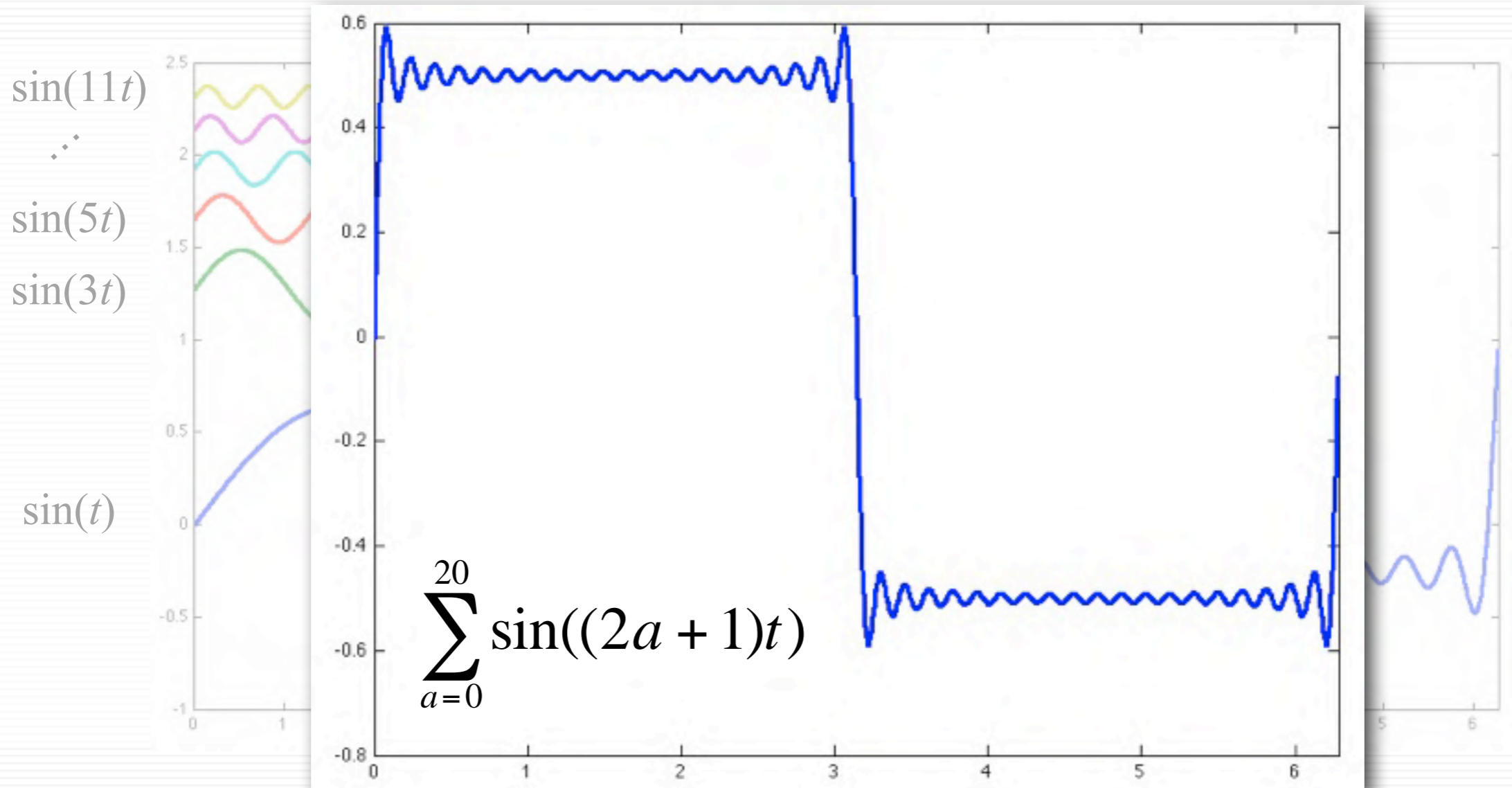
Field
Strength /
Frequency



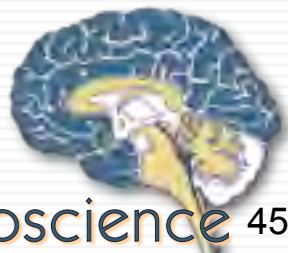
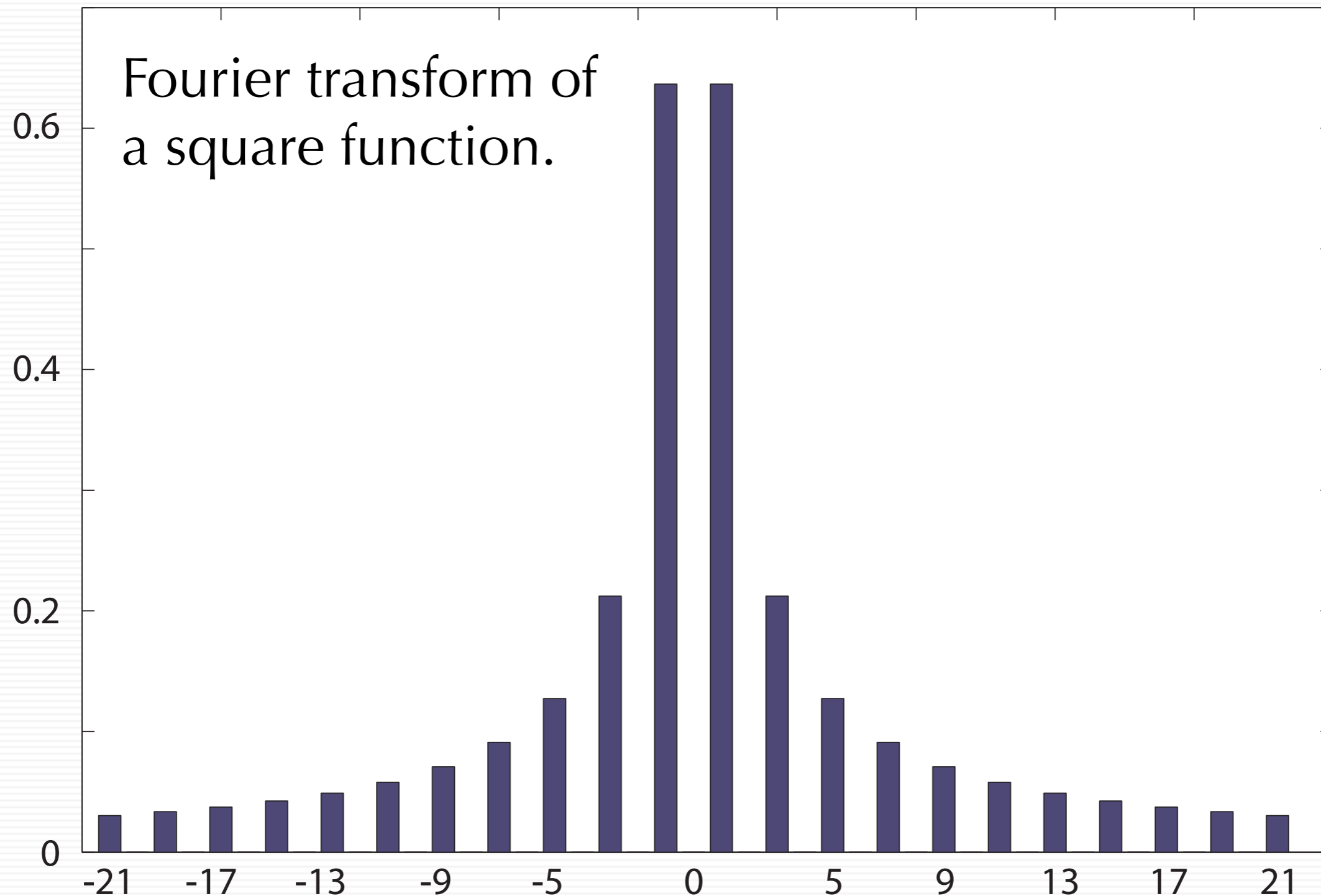
Fourier Sum example



Fourier Sum example



Typical Representation of Fourier Transform

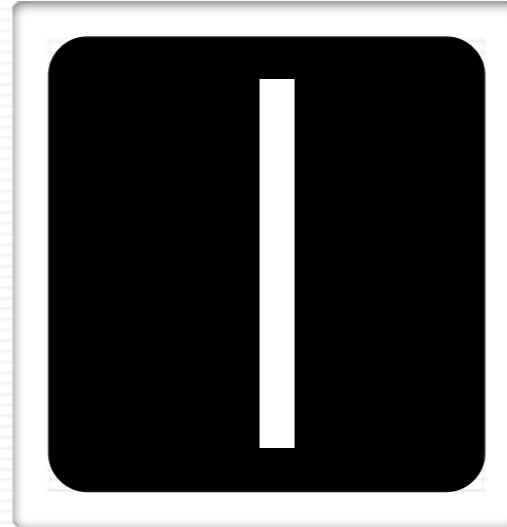


Objects with Finite Width

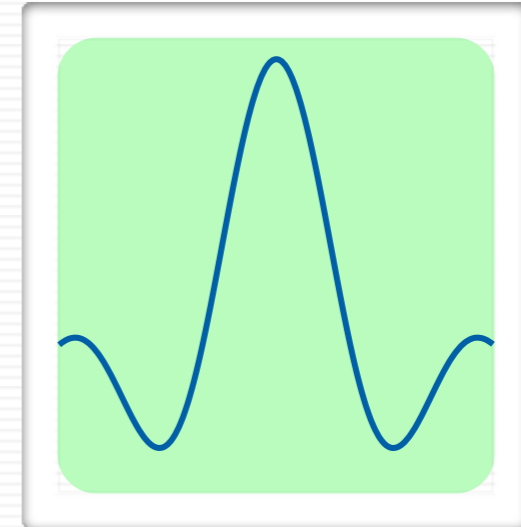


Narrow Feature
→ Wide Frequency Band

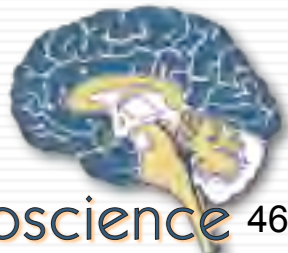
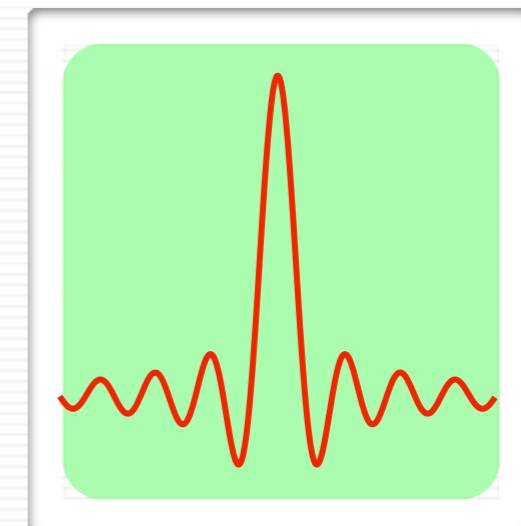
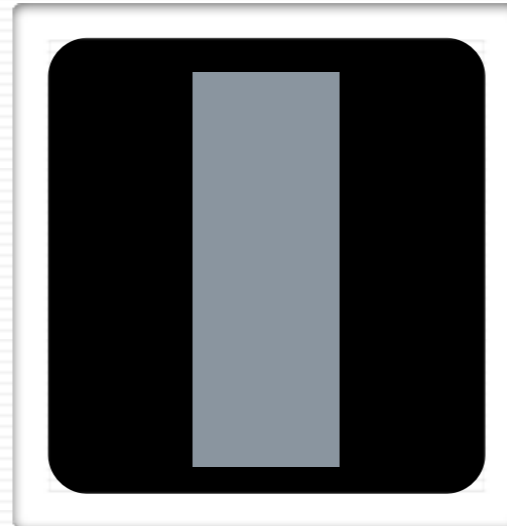
$f(t)$



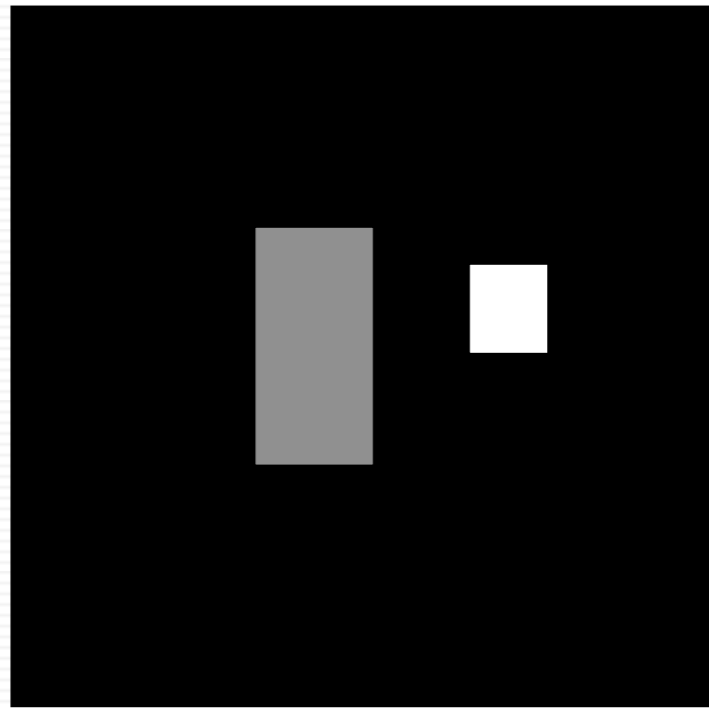
$F(\omega)$



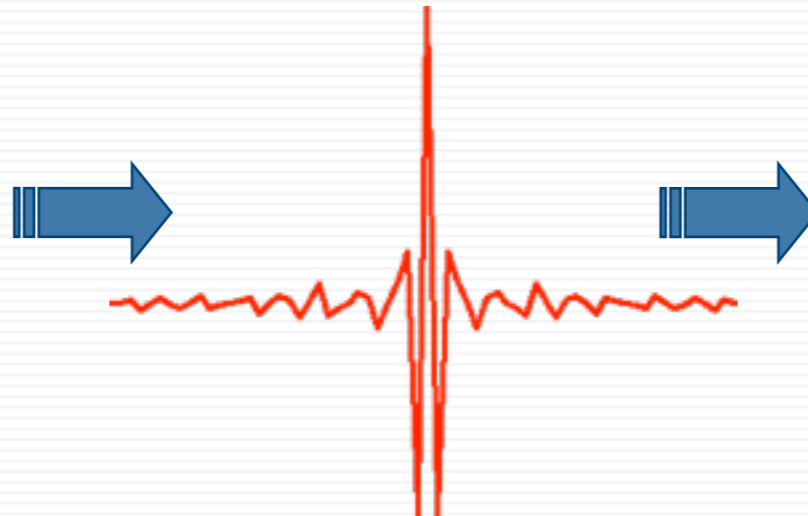
Wide Feature
→ Narrow Frequency Band



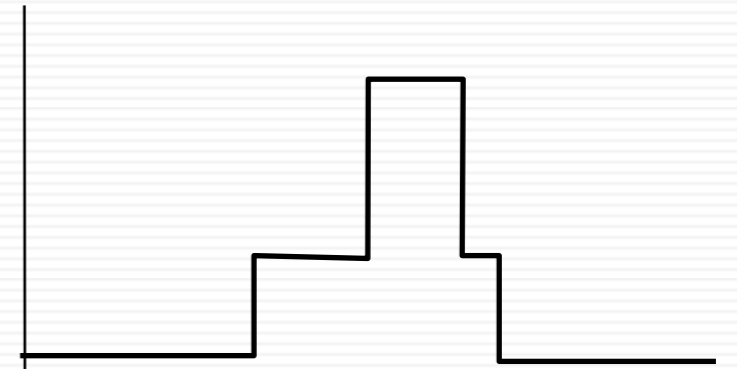
Fourier Projections



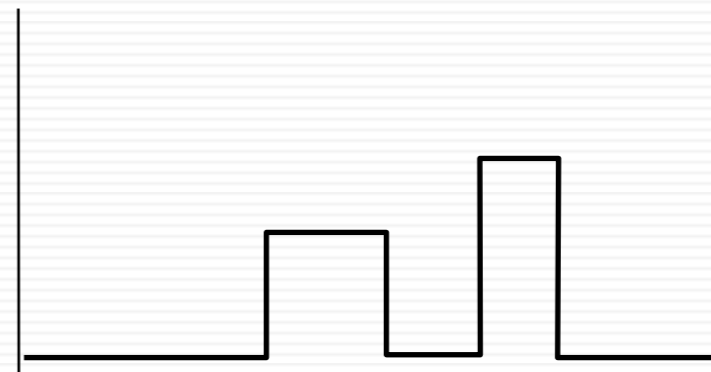
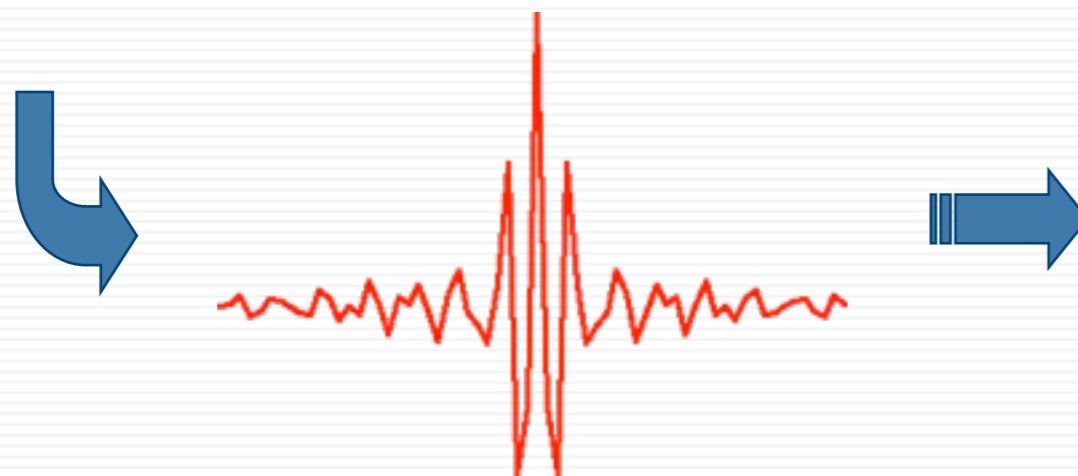
MR Image



Raw Data

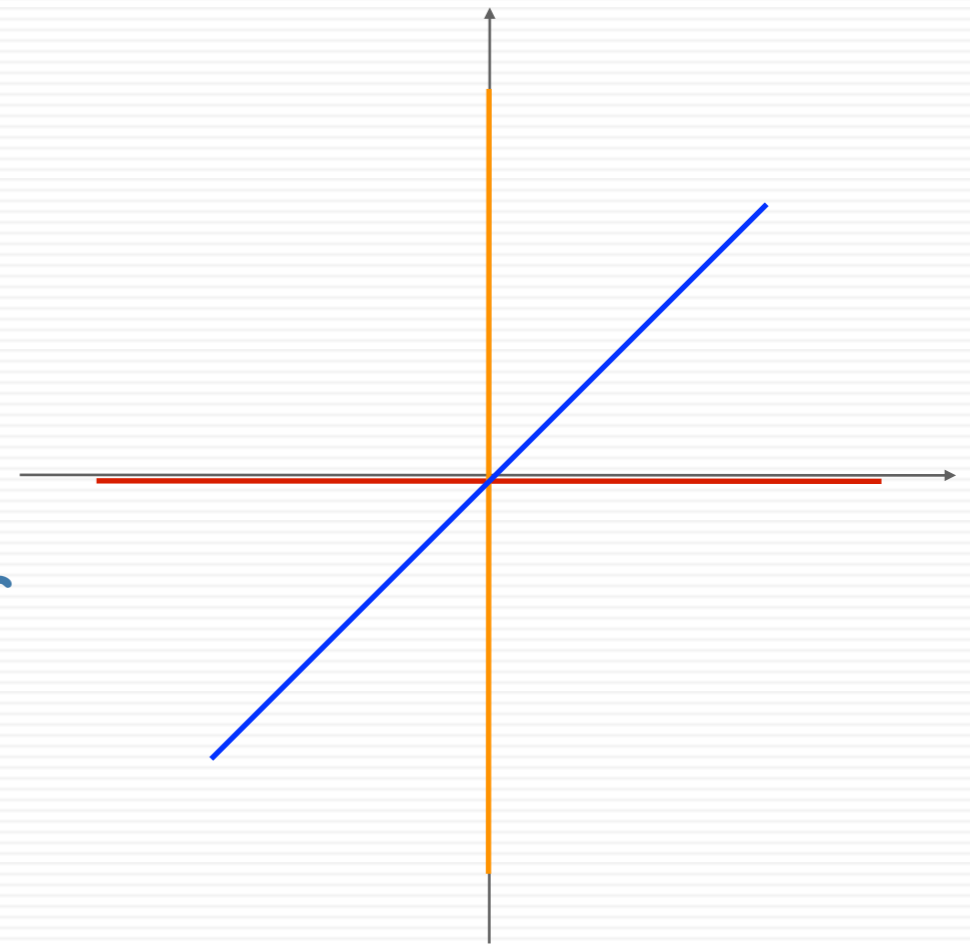
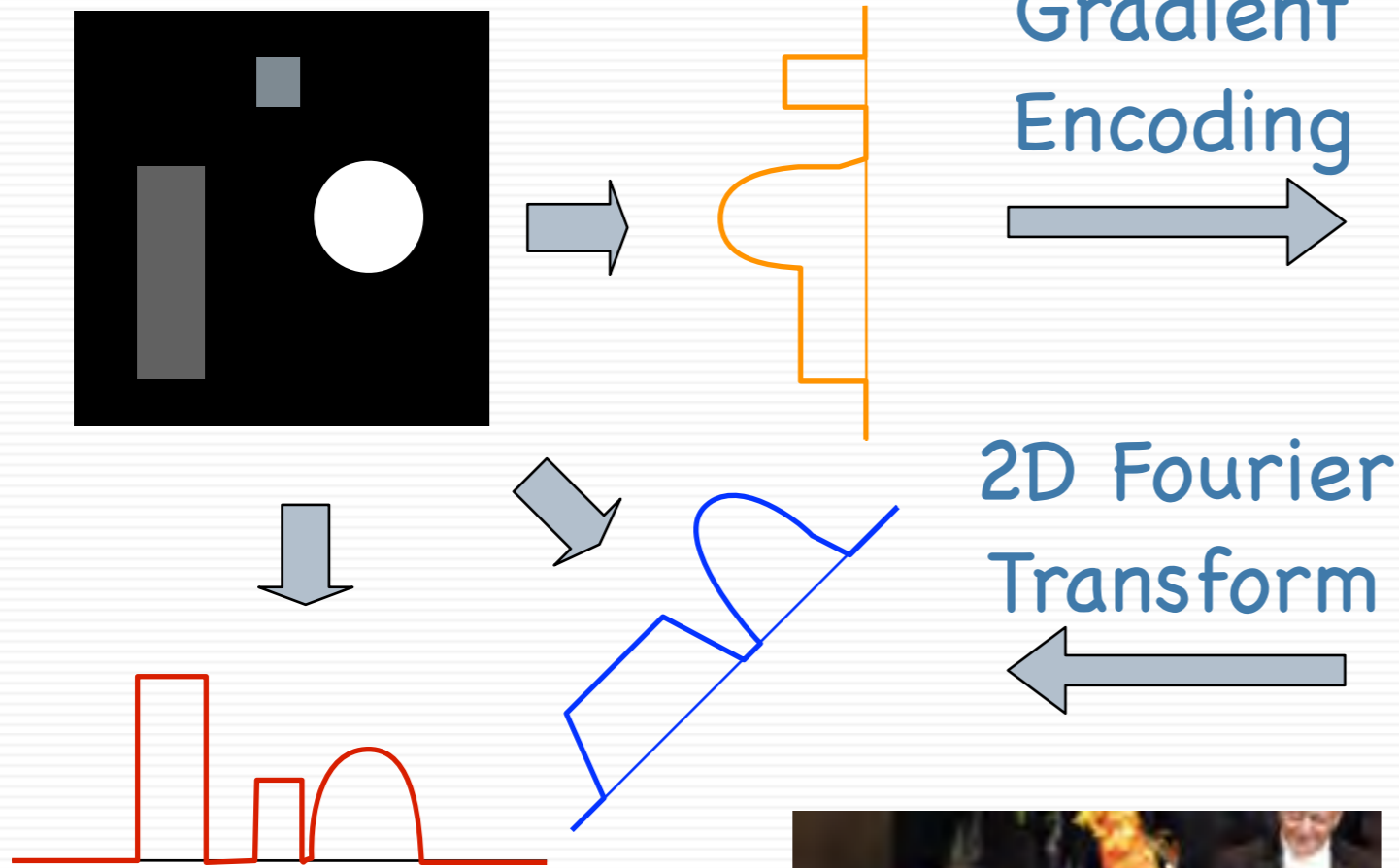


FFT of Raw Data



Back Projection

Image Domain



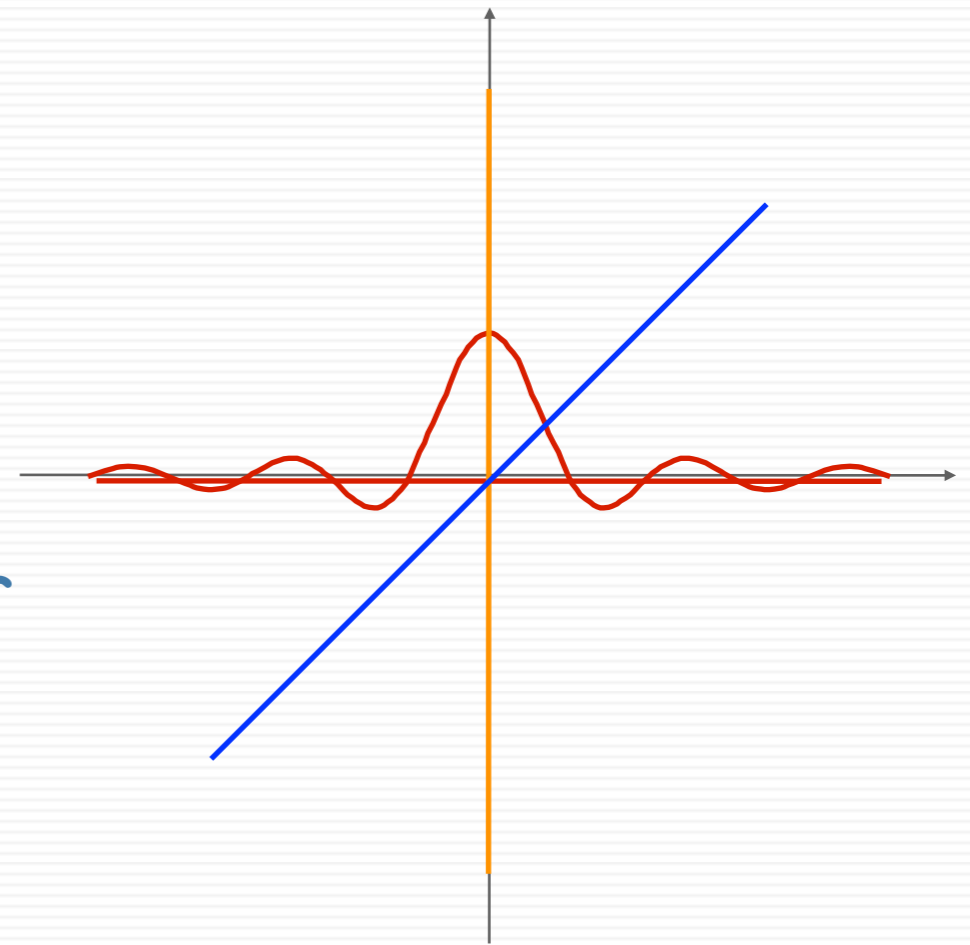
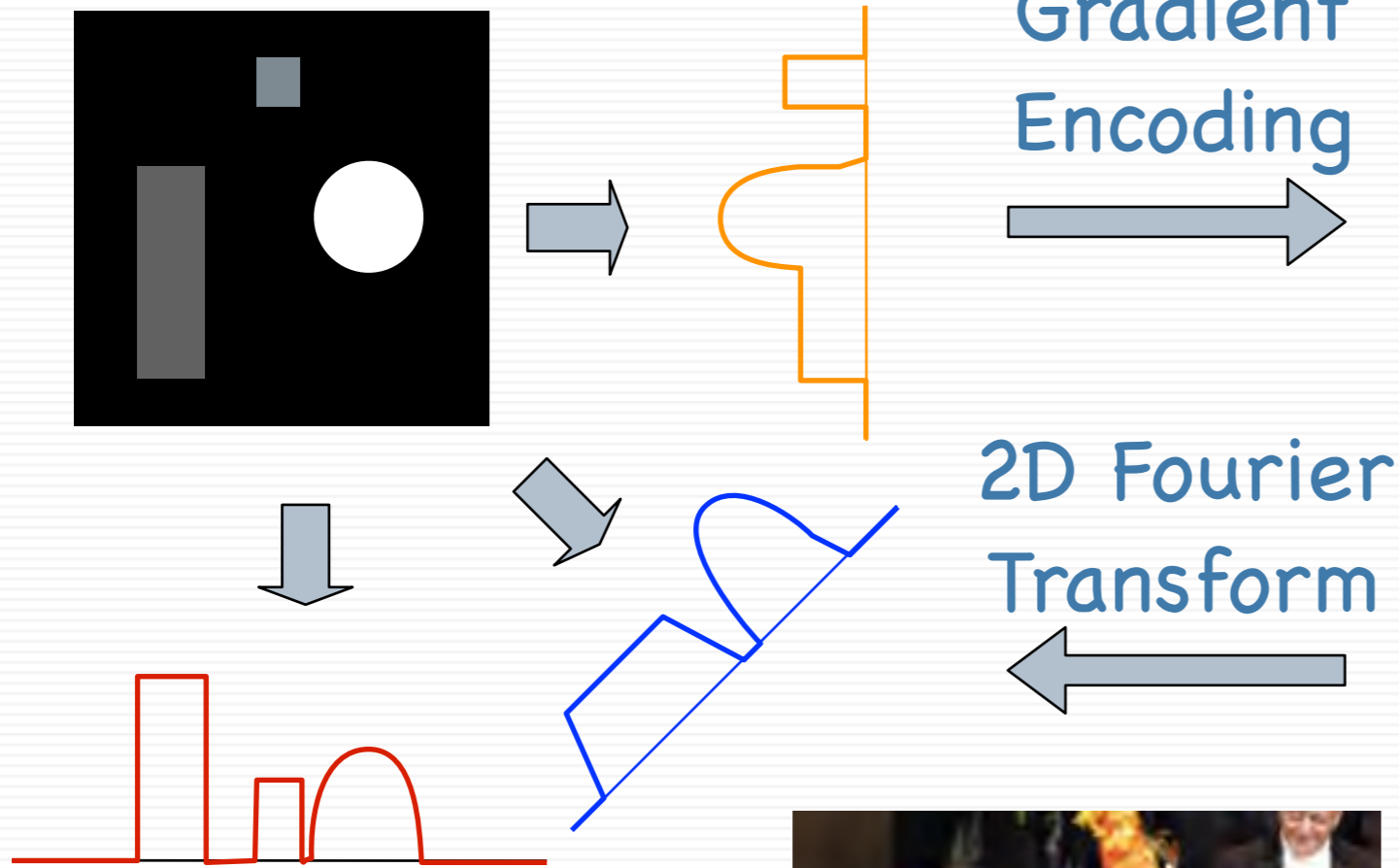
Fourier Domain

**Paul
Lauterbur**



Back Projection

Image Domain



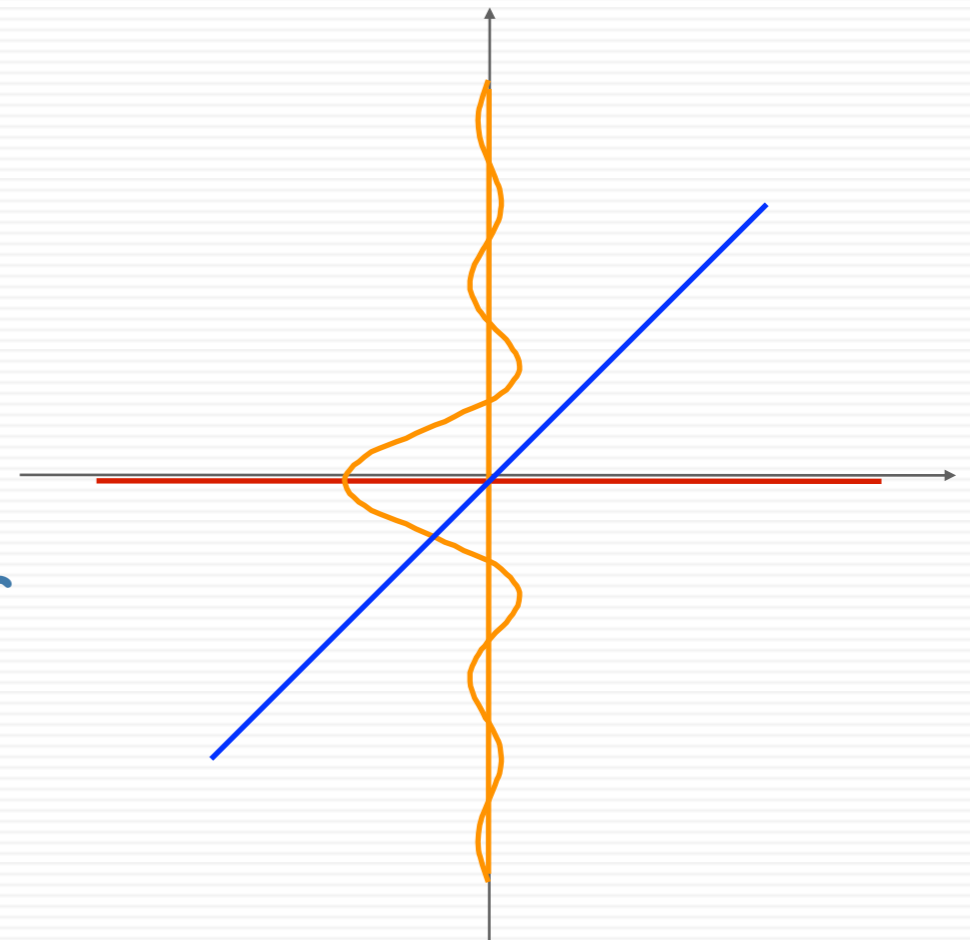
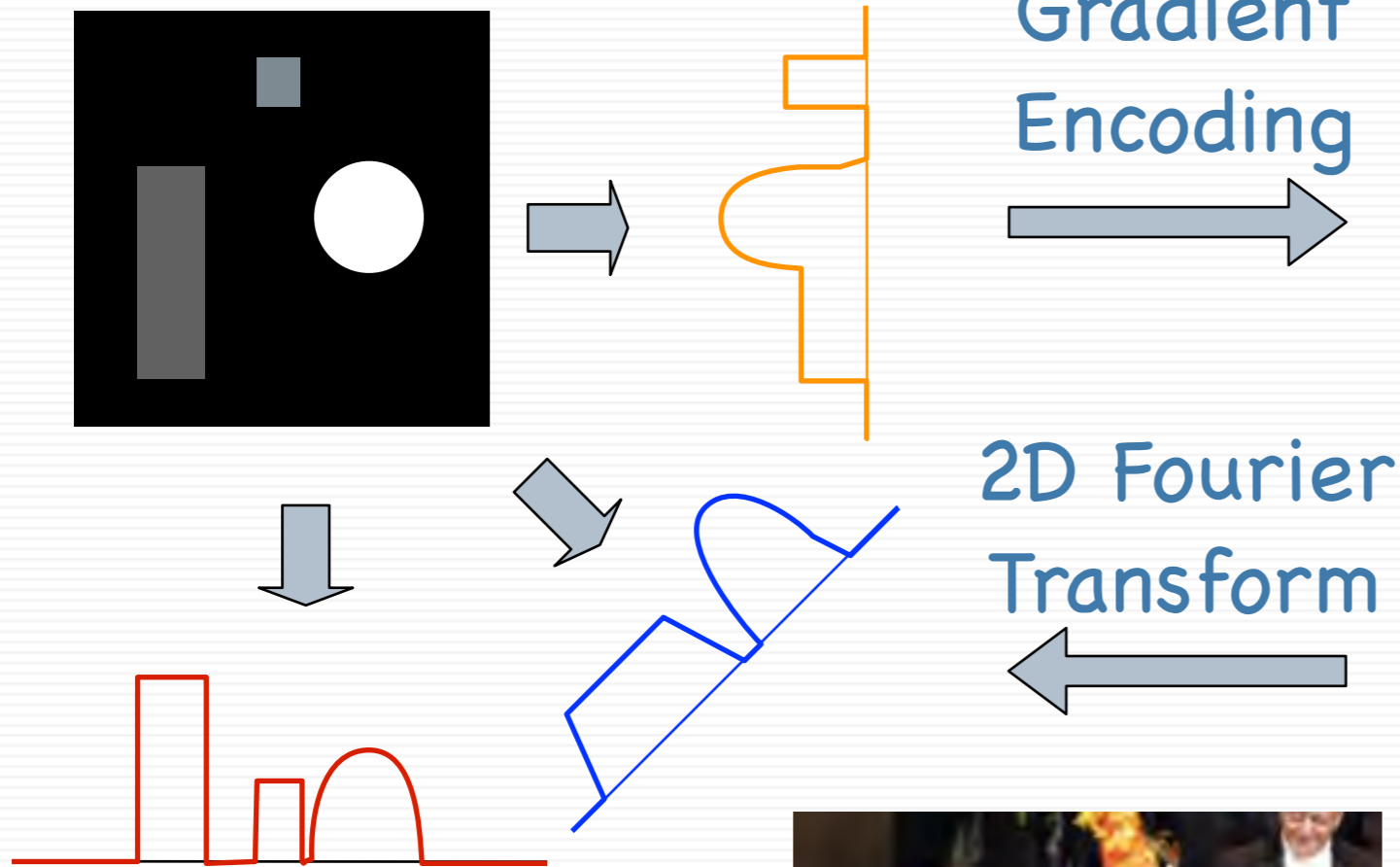
Fourier Domain

Paul
Lauterbur



Back Projection

Image Domain



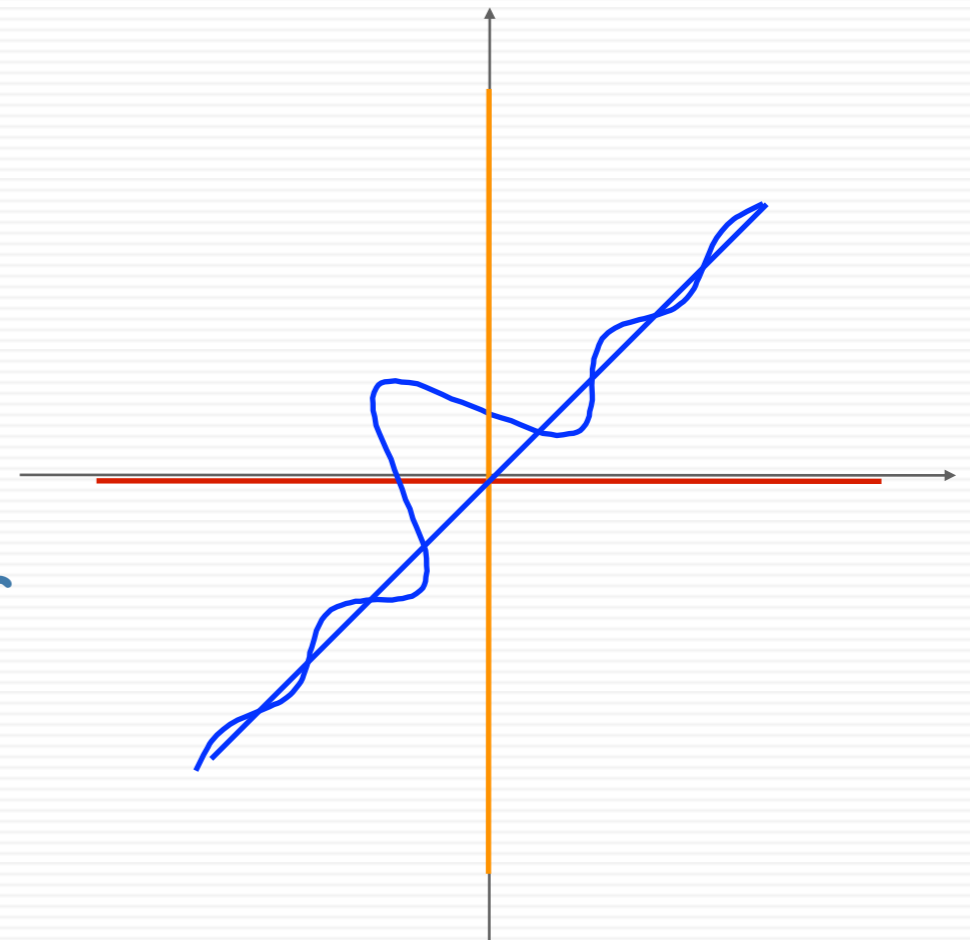
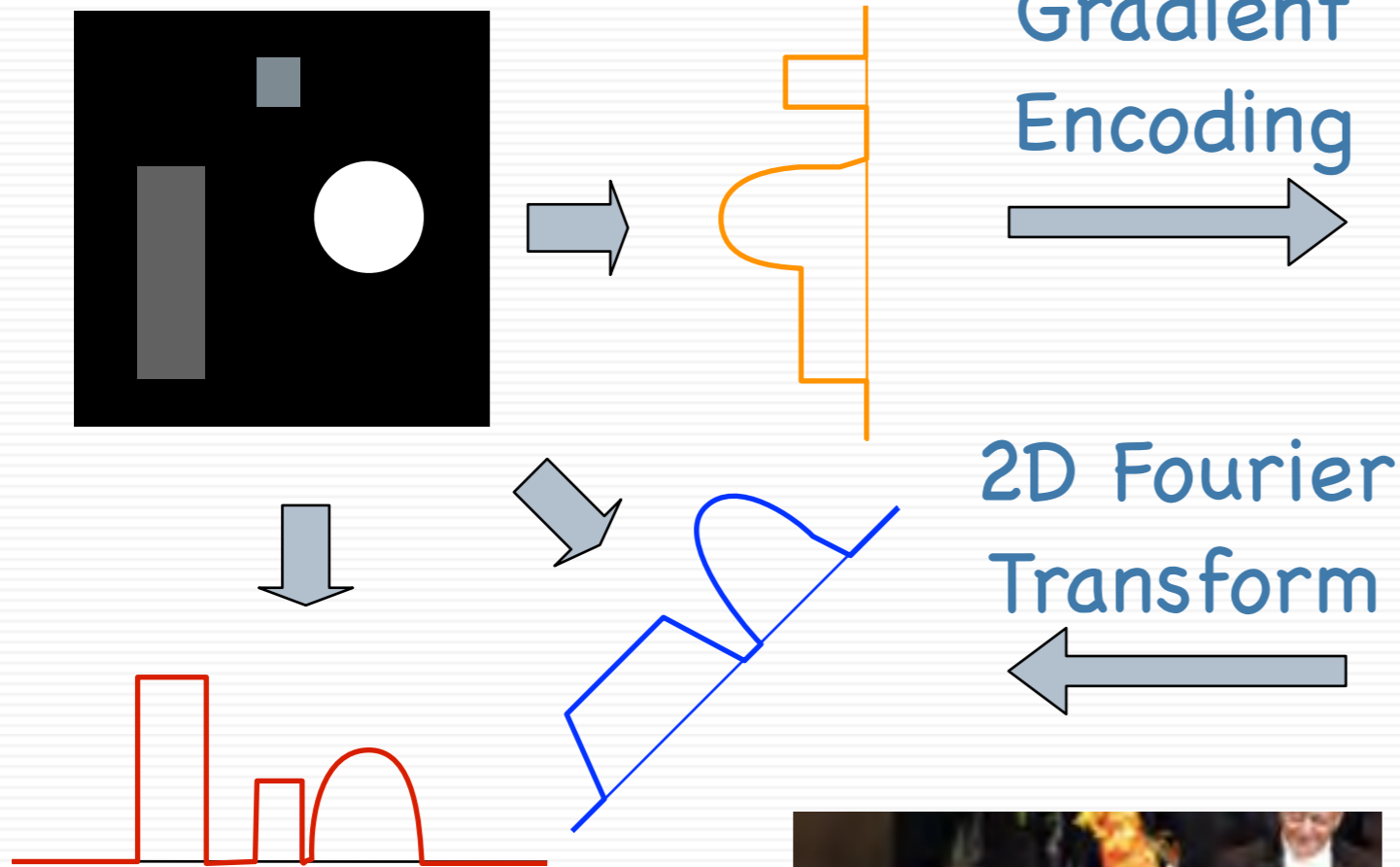
Fourier Domain

Paul
Lauterbur



Back Projection

Image Domain



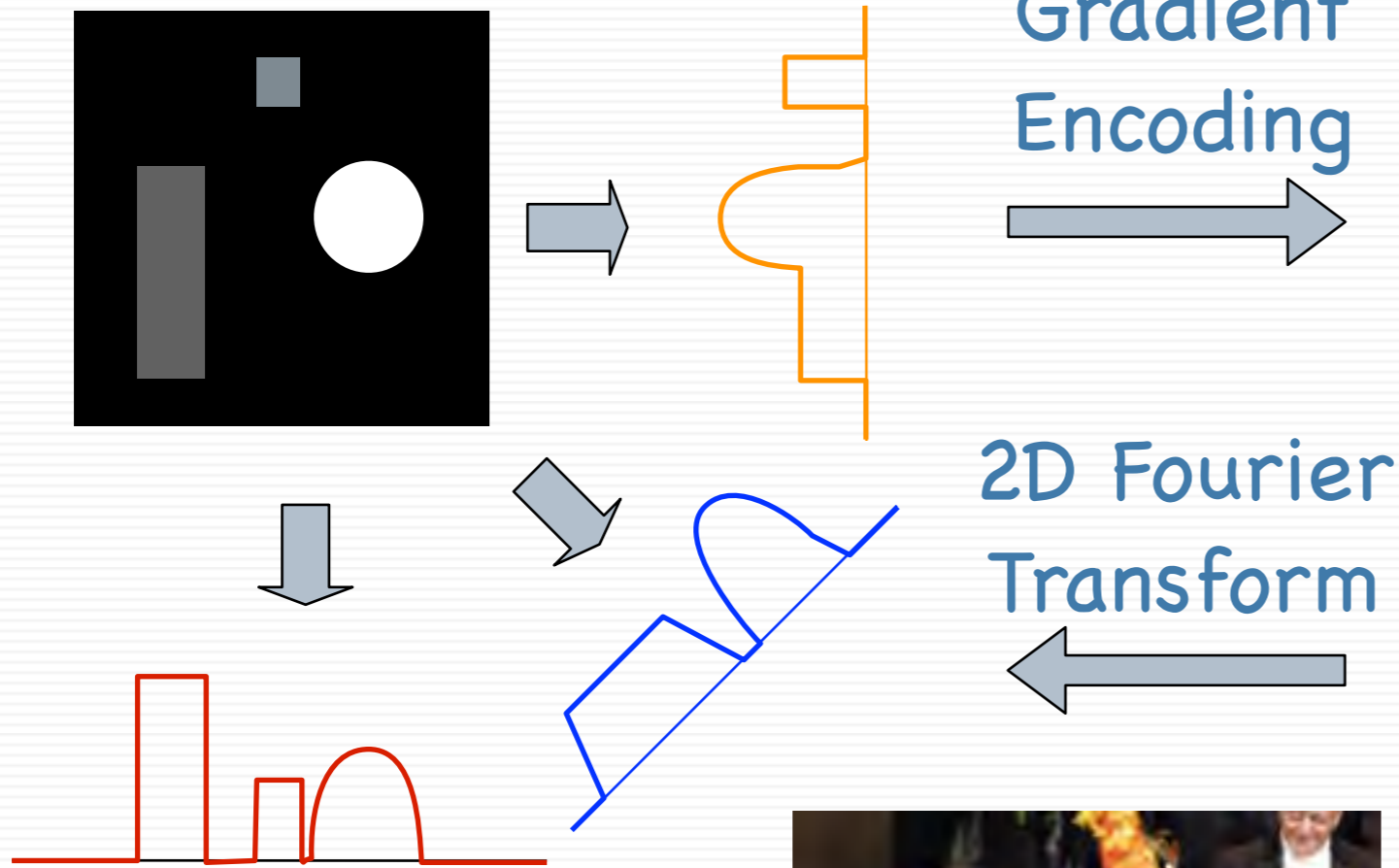
Fourier Domain

Paul
Lauterbur



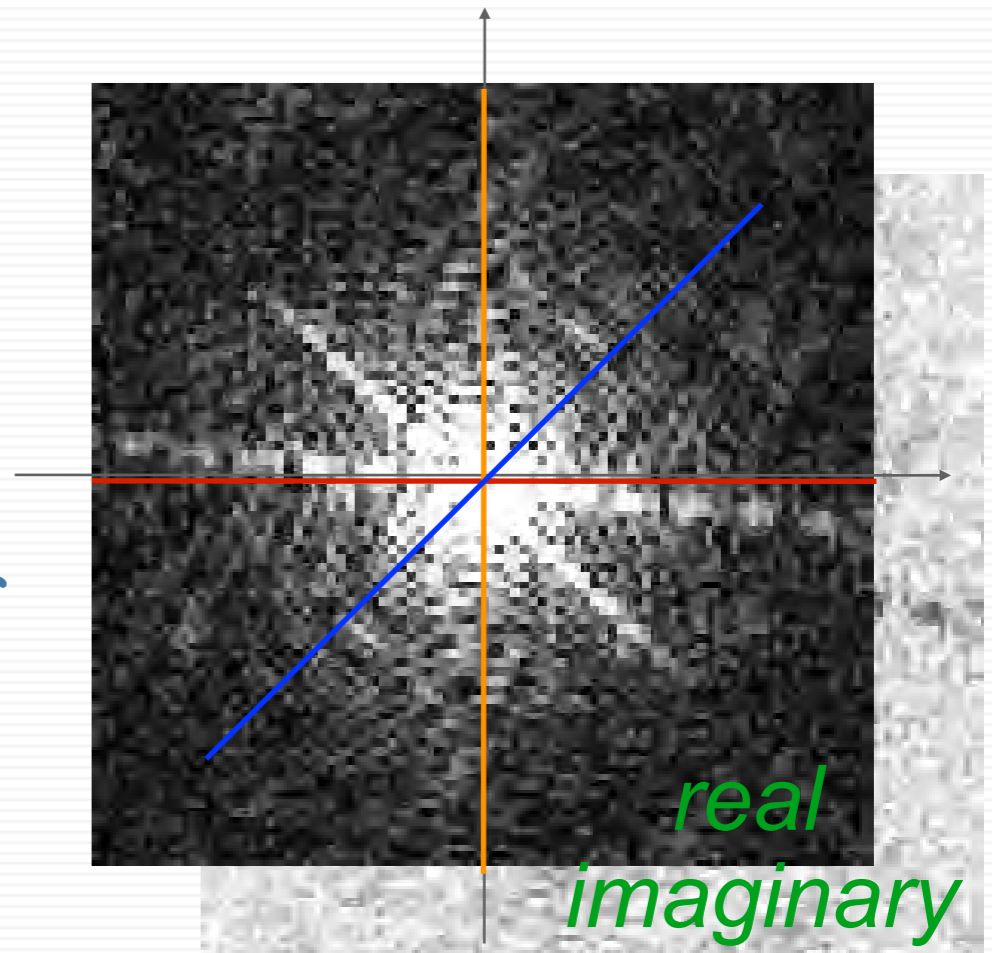
Back Projection

Image Domain



Gradient Encoding

2D Fourier Transform

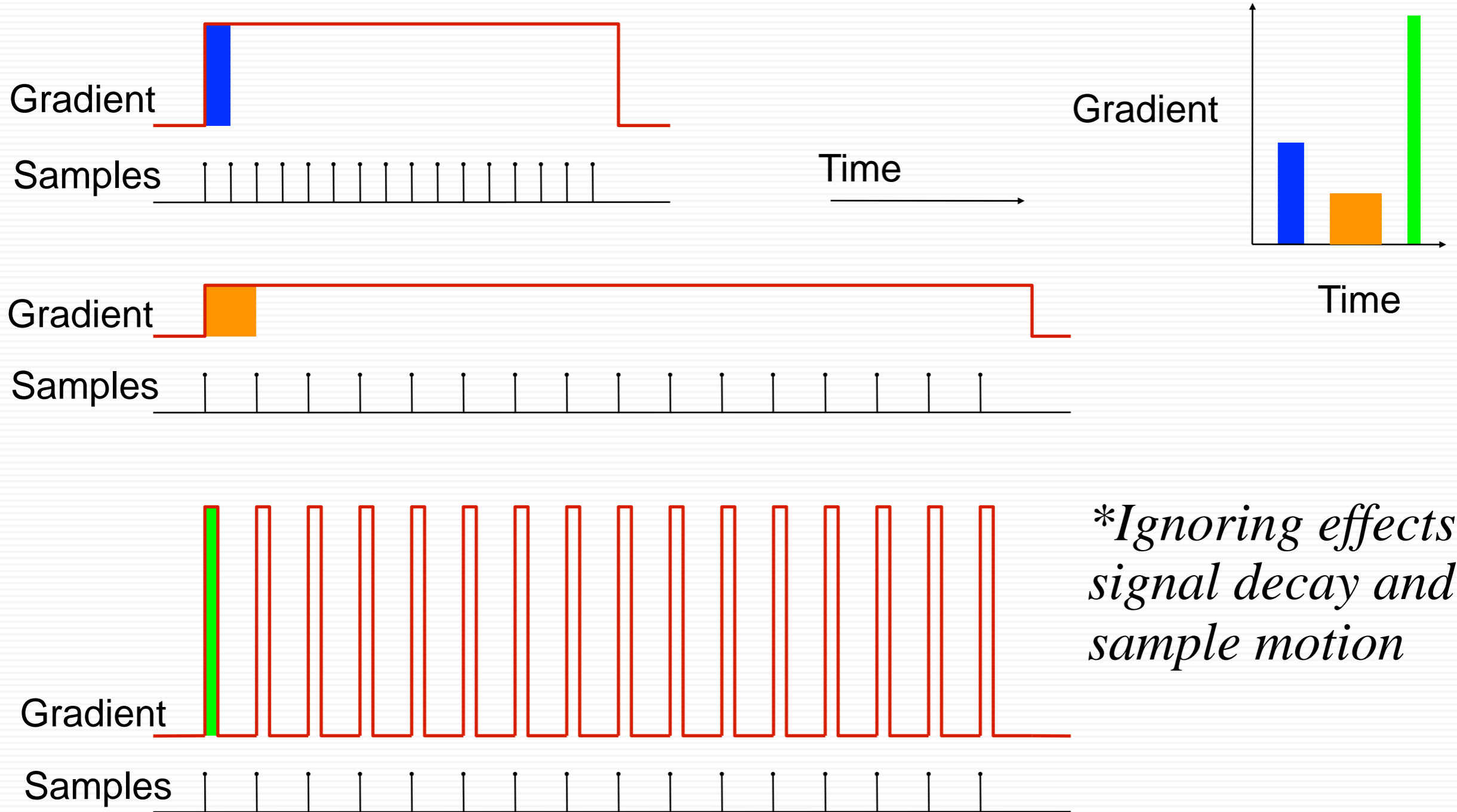


Fourier Domain

Paul
Lauterbur



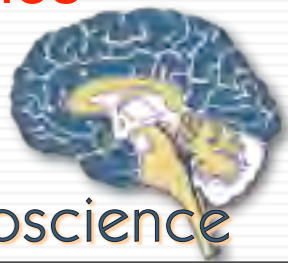
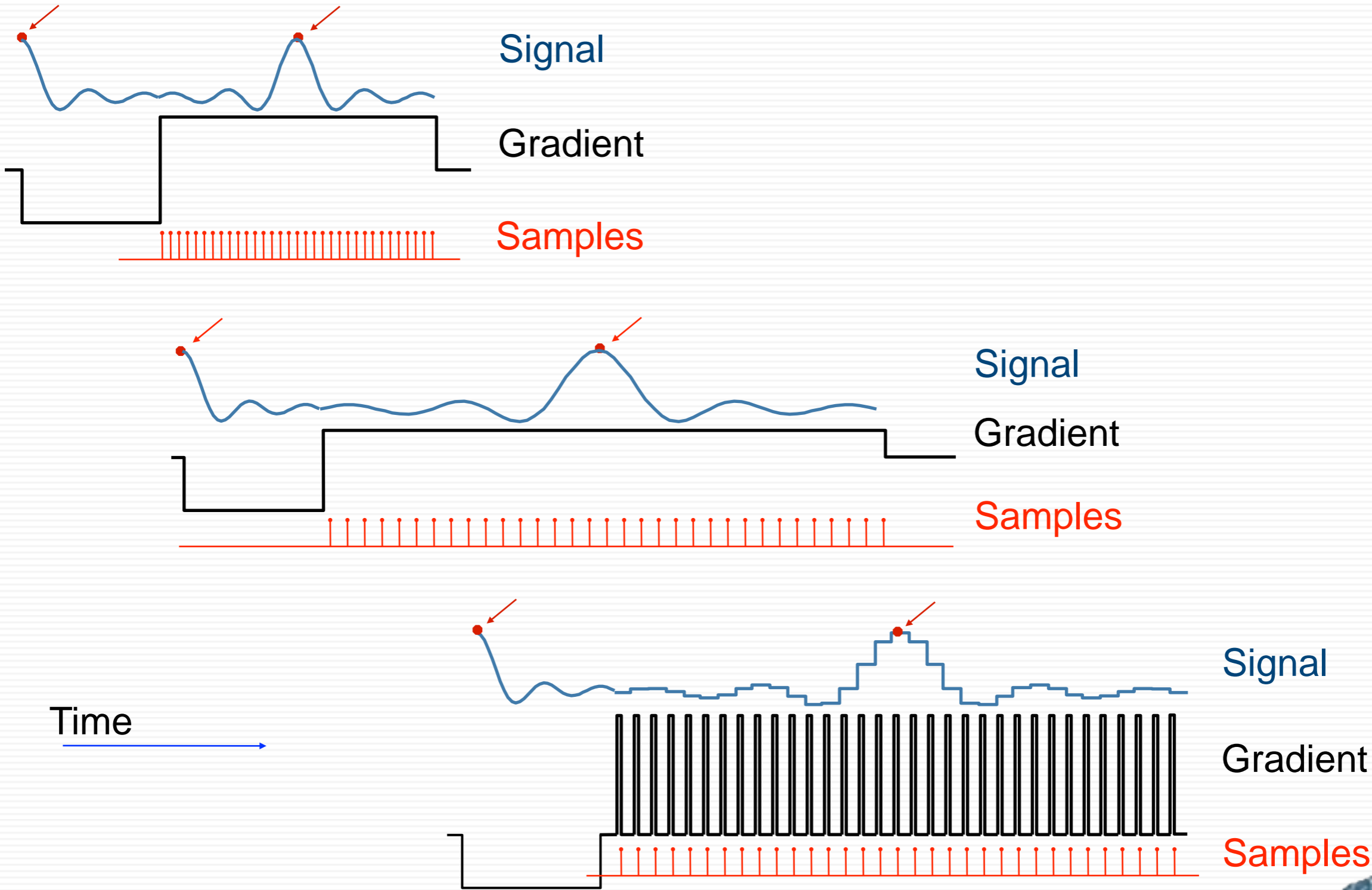
Equivalent Strategies in k-space*



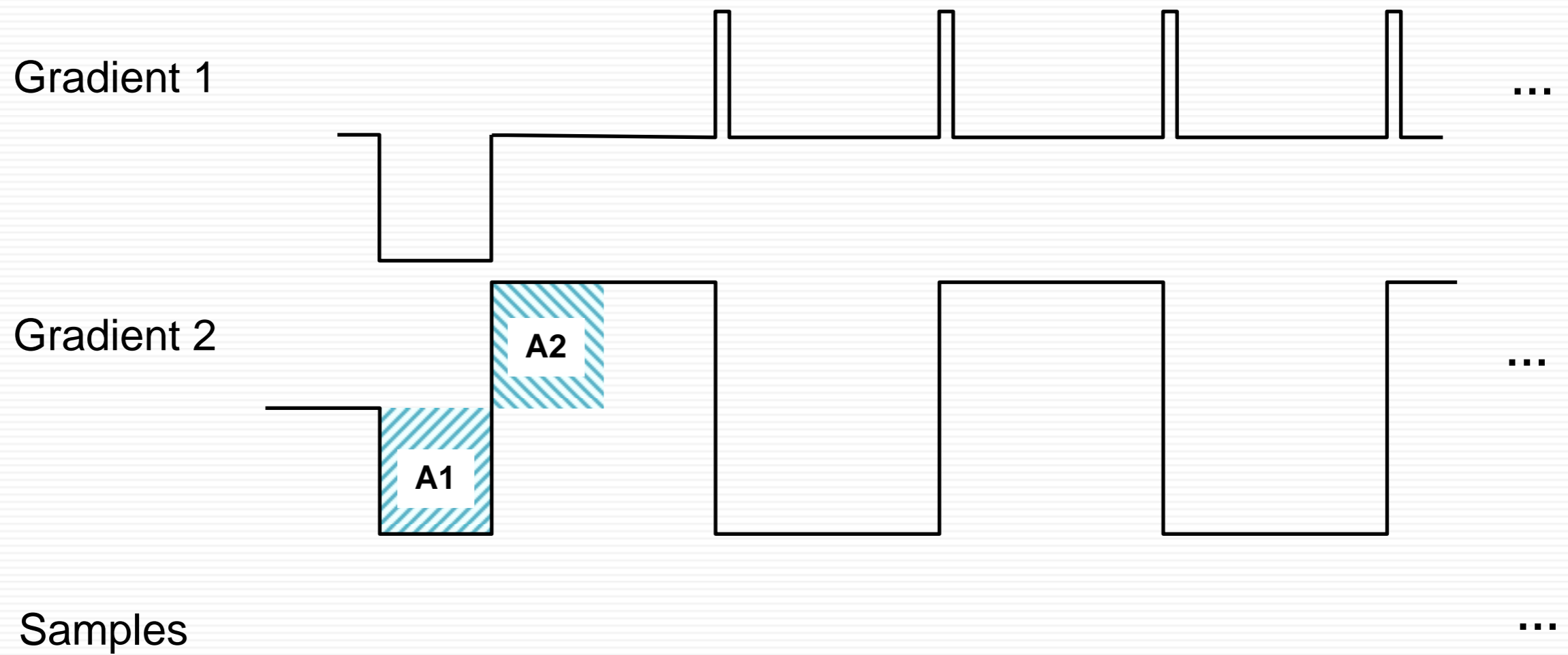
**Ignoring effects of signal decay and sample motion*



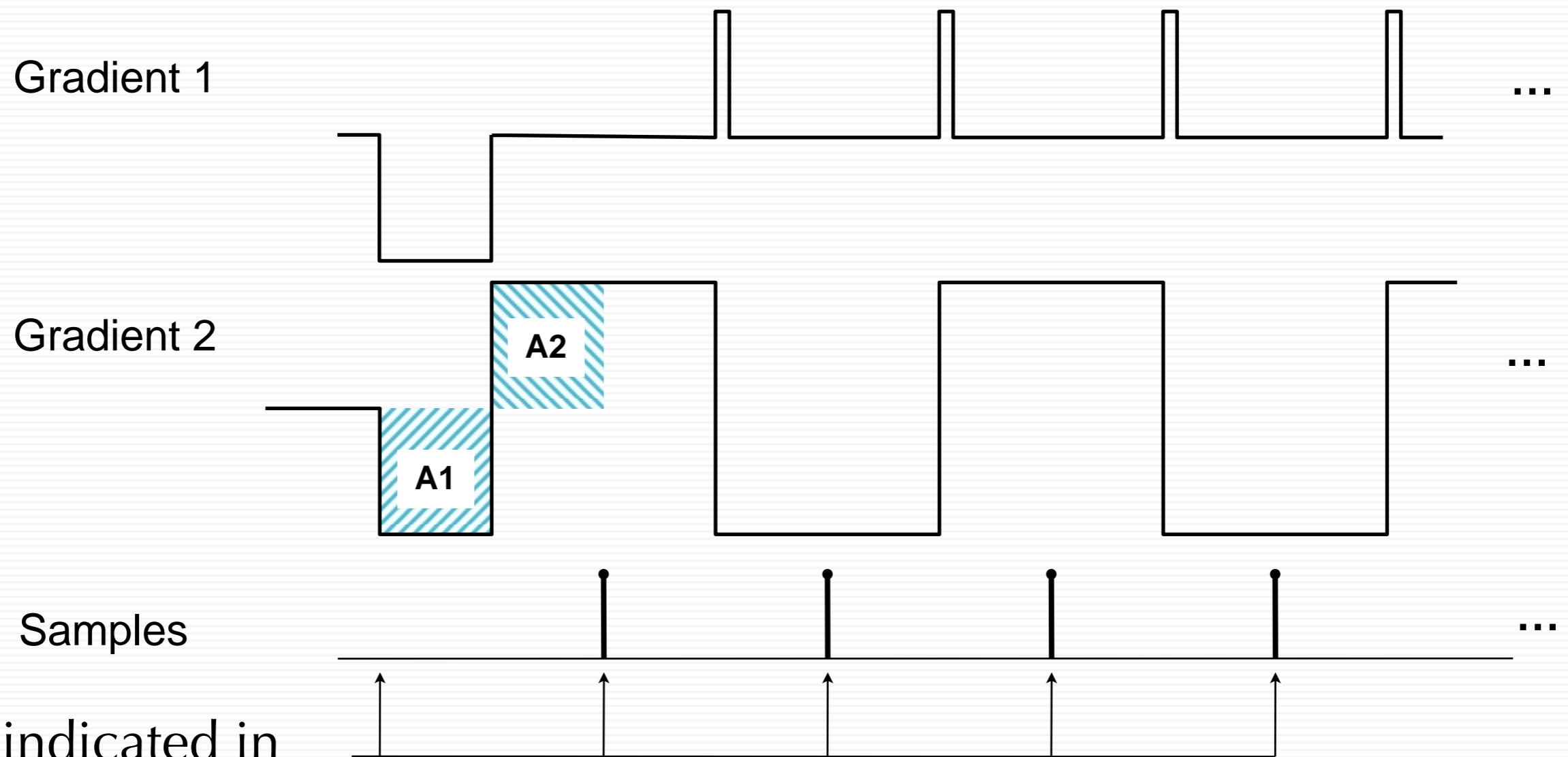
Gradient Pre-encoding



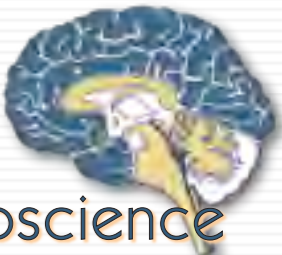
Interleaved Spatial Encoding



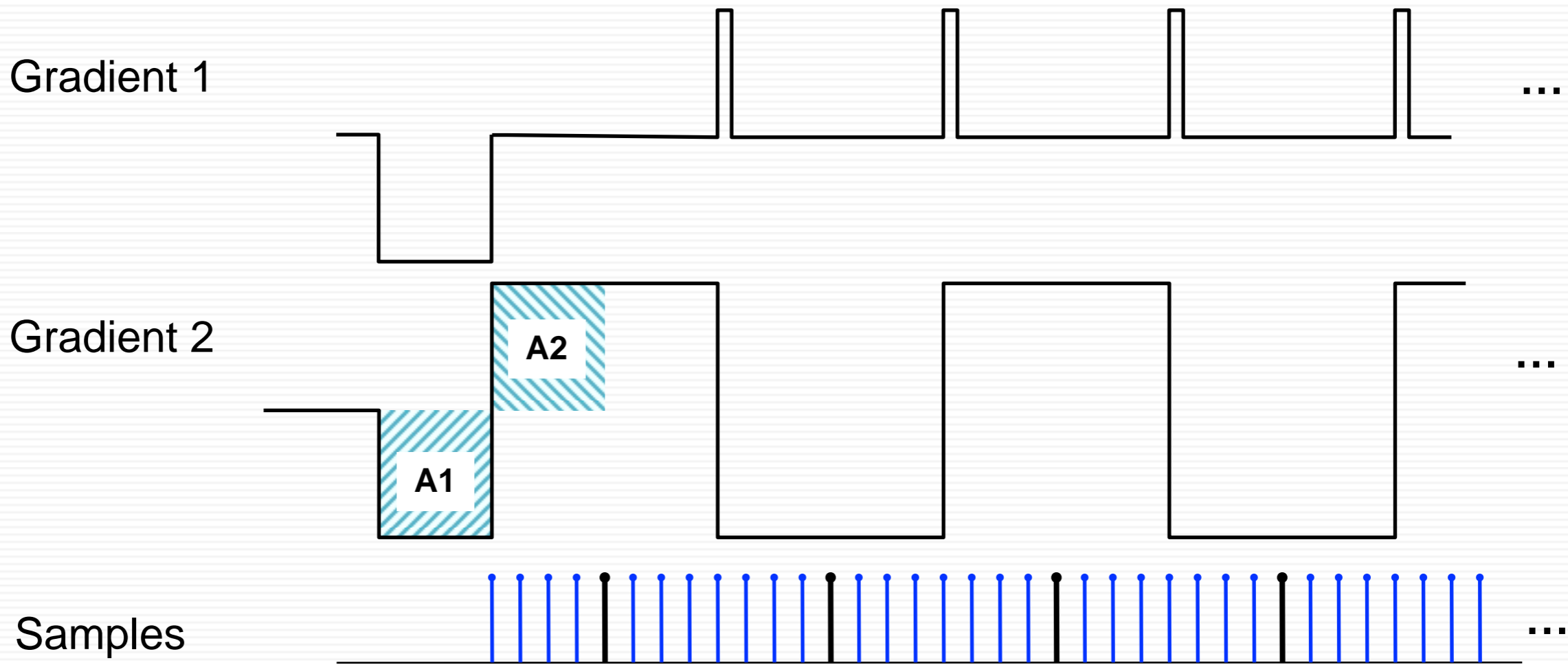
Interleaved Spatial Encoding



Points indicated in black are affected by Gradient 1 but NOT by Gradient 2

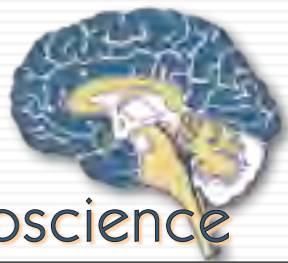


Interleaved Spatial Encoding



Points indicated in black are affected by Gradient 1 but NOT by Gradient 2

Points indicated in Blue are affected by both gradients

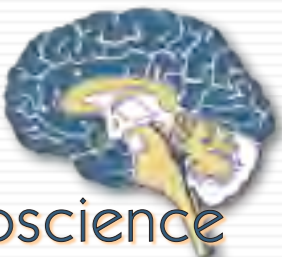
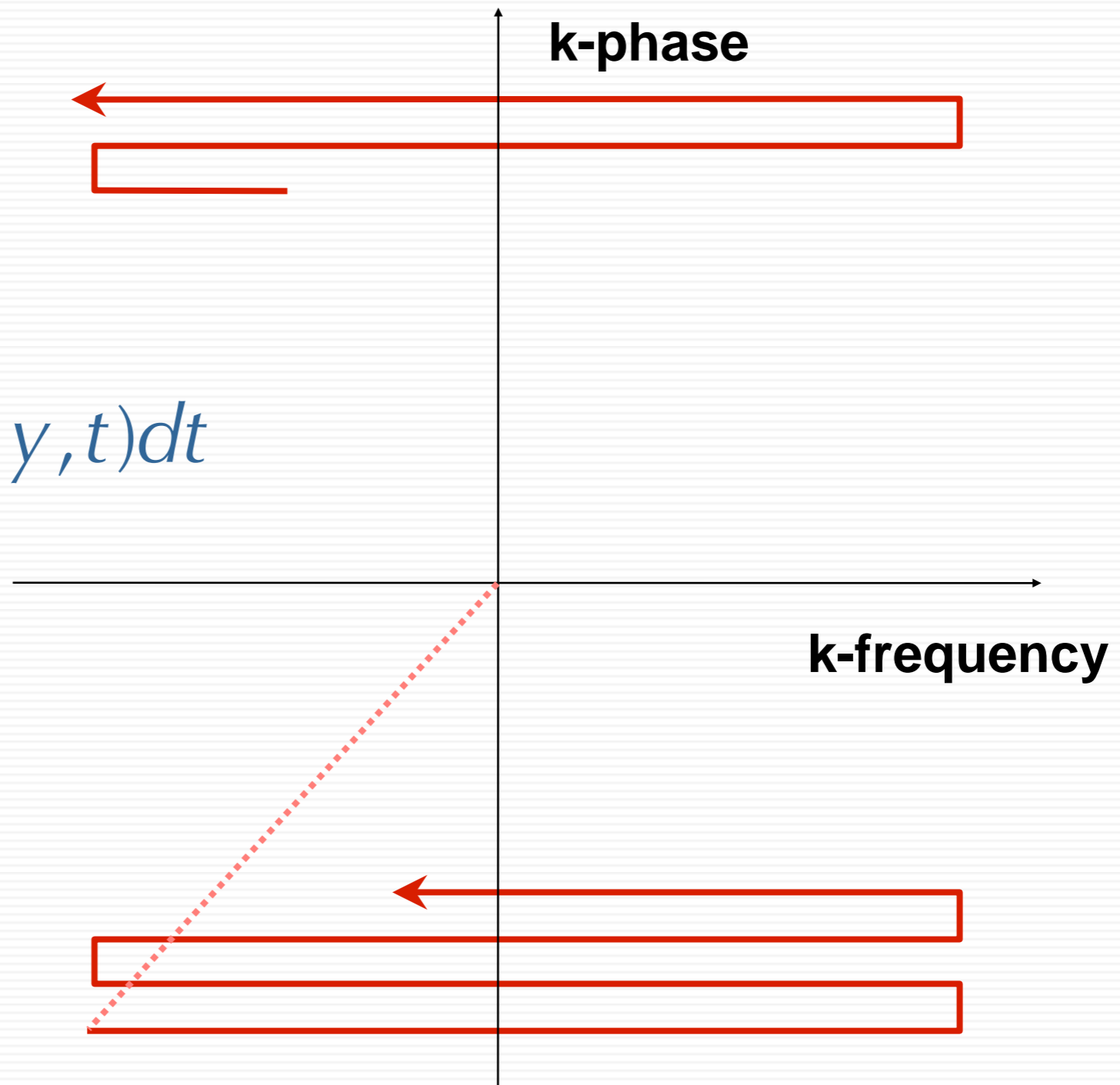


Echo-Planar k-space Trajectory

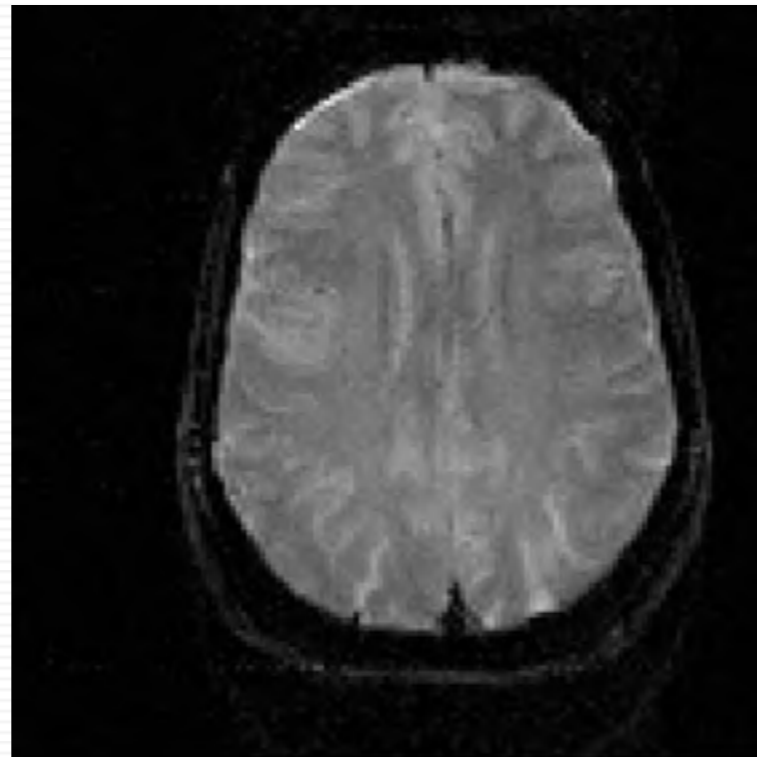
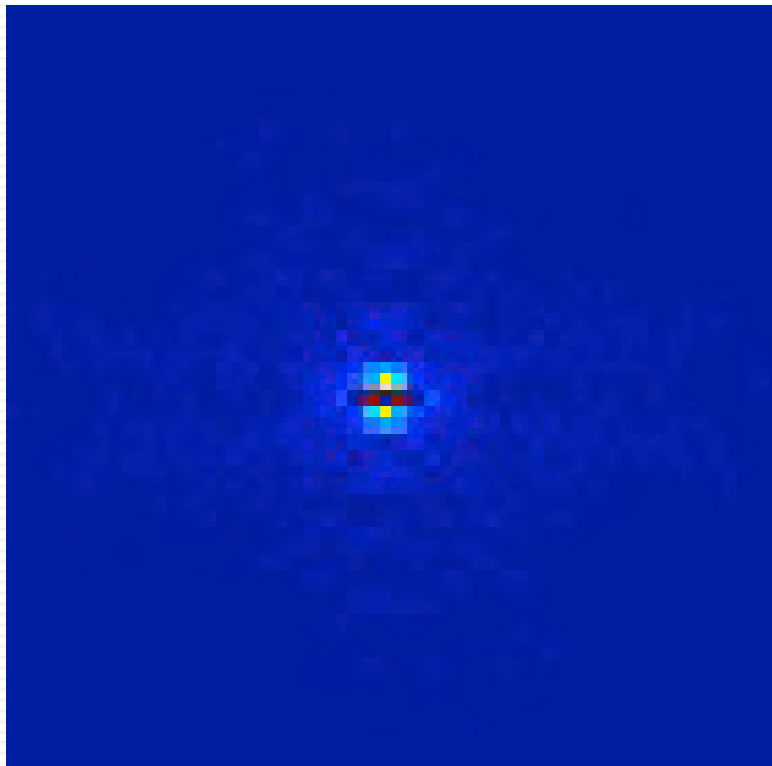
k-space plots the integral of the gradient encoding.

$$k(x, y, t) = \gamma \int_0^T G(x, y, t) dt$$

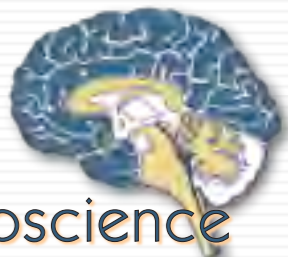
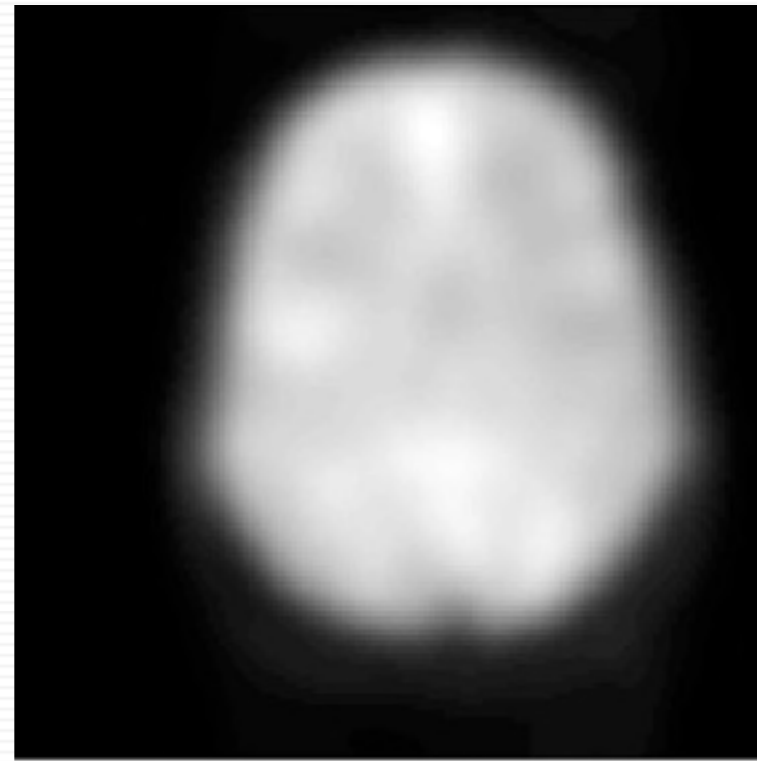
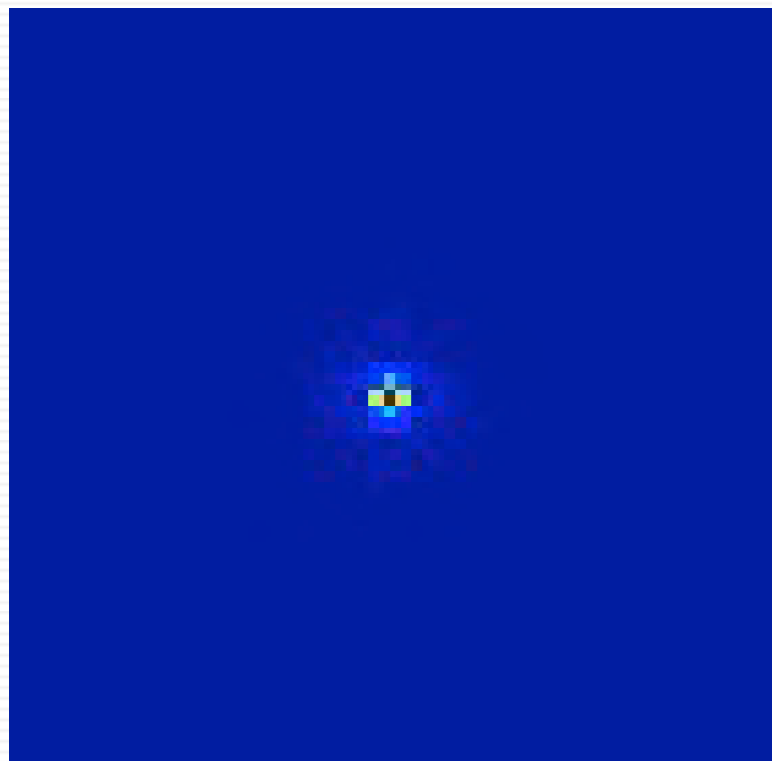
Its Fourier transform is the image.



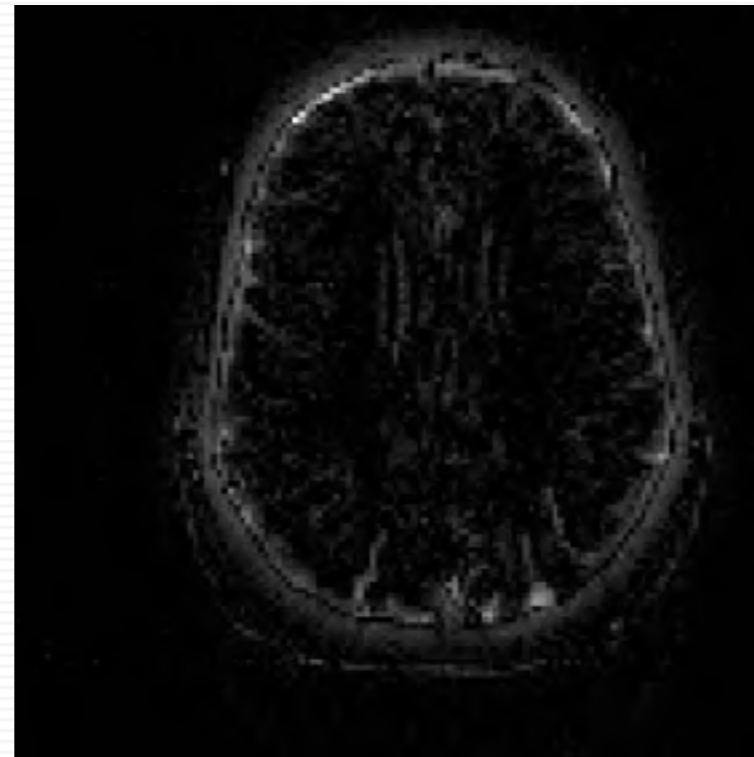
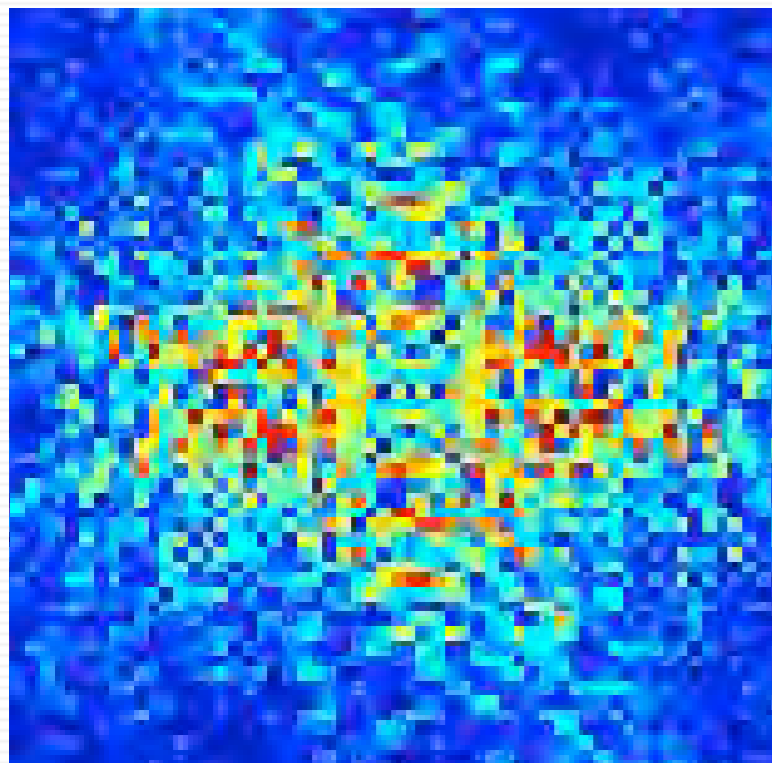
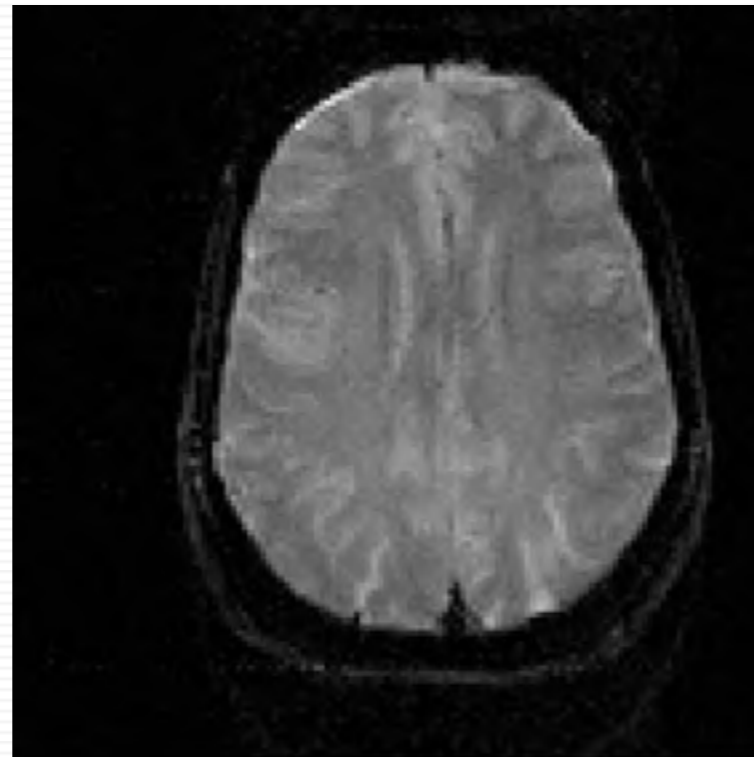
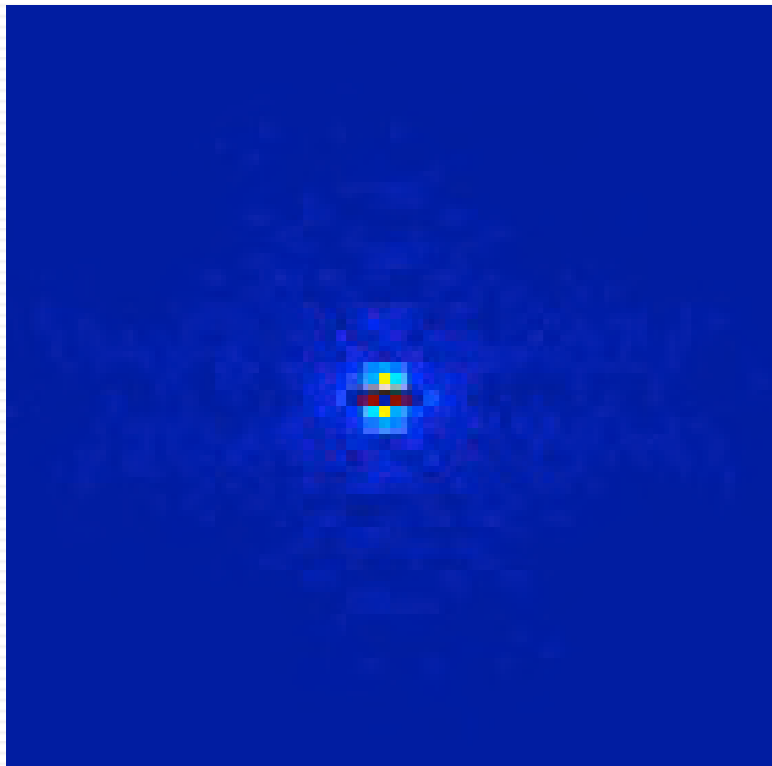
Properties of K-Space



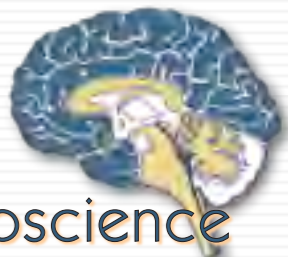
- Increasing K values Represent Higher Spatial Frequencies, thus Higher Resolution
- Finer Grain Sampling Results in Wider FOV



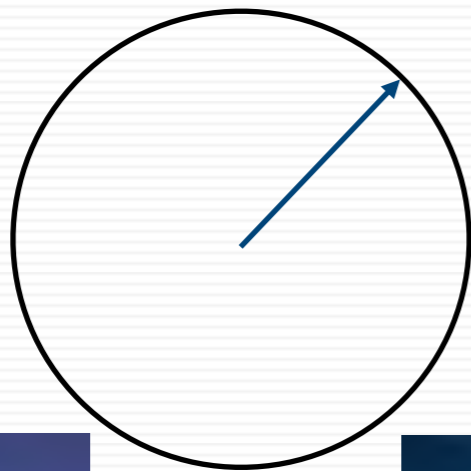
Properties of K-Space



- Increasing K values Represent Higher Spatial Frequencies, thus Higher Resolution
- Finer Grain Sampling Results in Wider FOV



Raw Data Symmetry

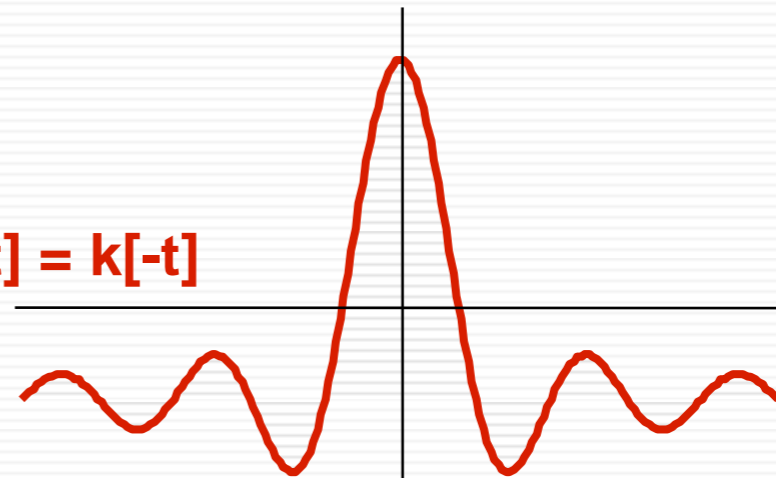


Detector 1

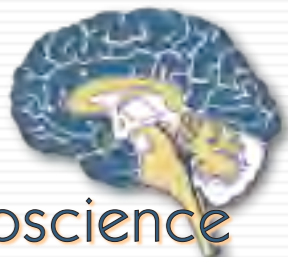
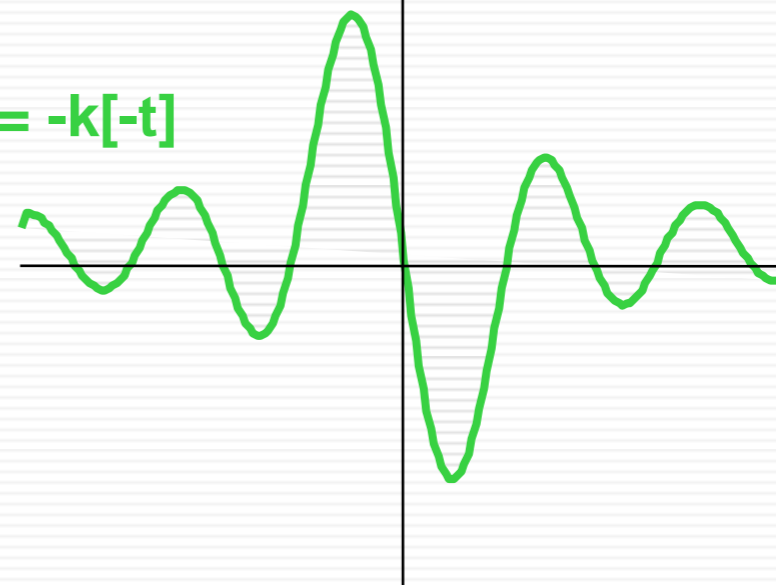


Detector 2

$$k[t] = k[-t]$$



$$k[t] = -k[-t]$$

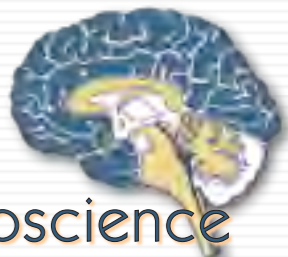


k-space conjugate symmetry

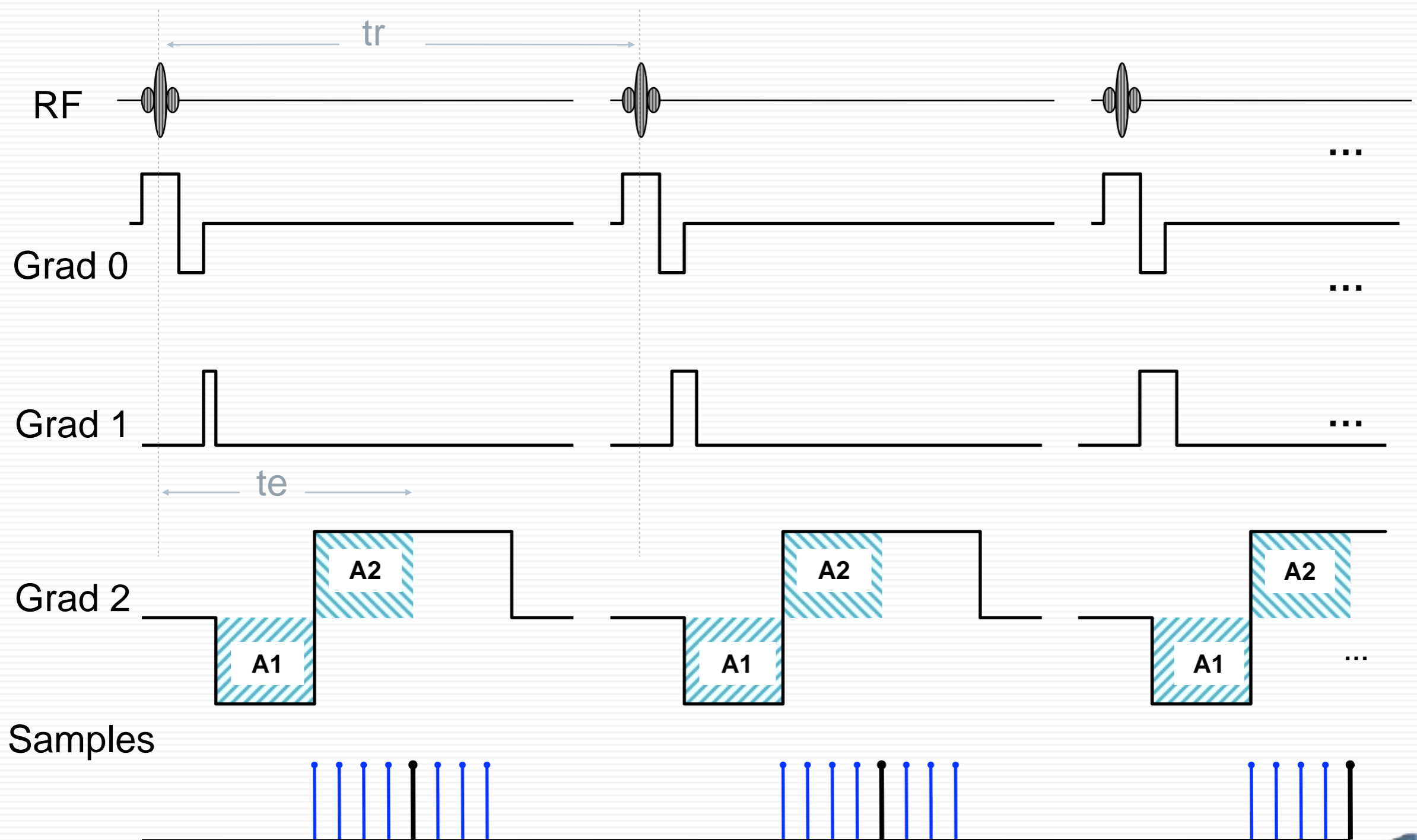
For a Stationary Object,
in a Homogeneous Field: $S(kx, ky) = \overline{S(kx, -ky)}$

where $S(kx, ky)$ is the signal at (kx, ky) .

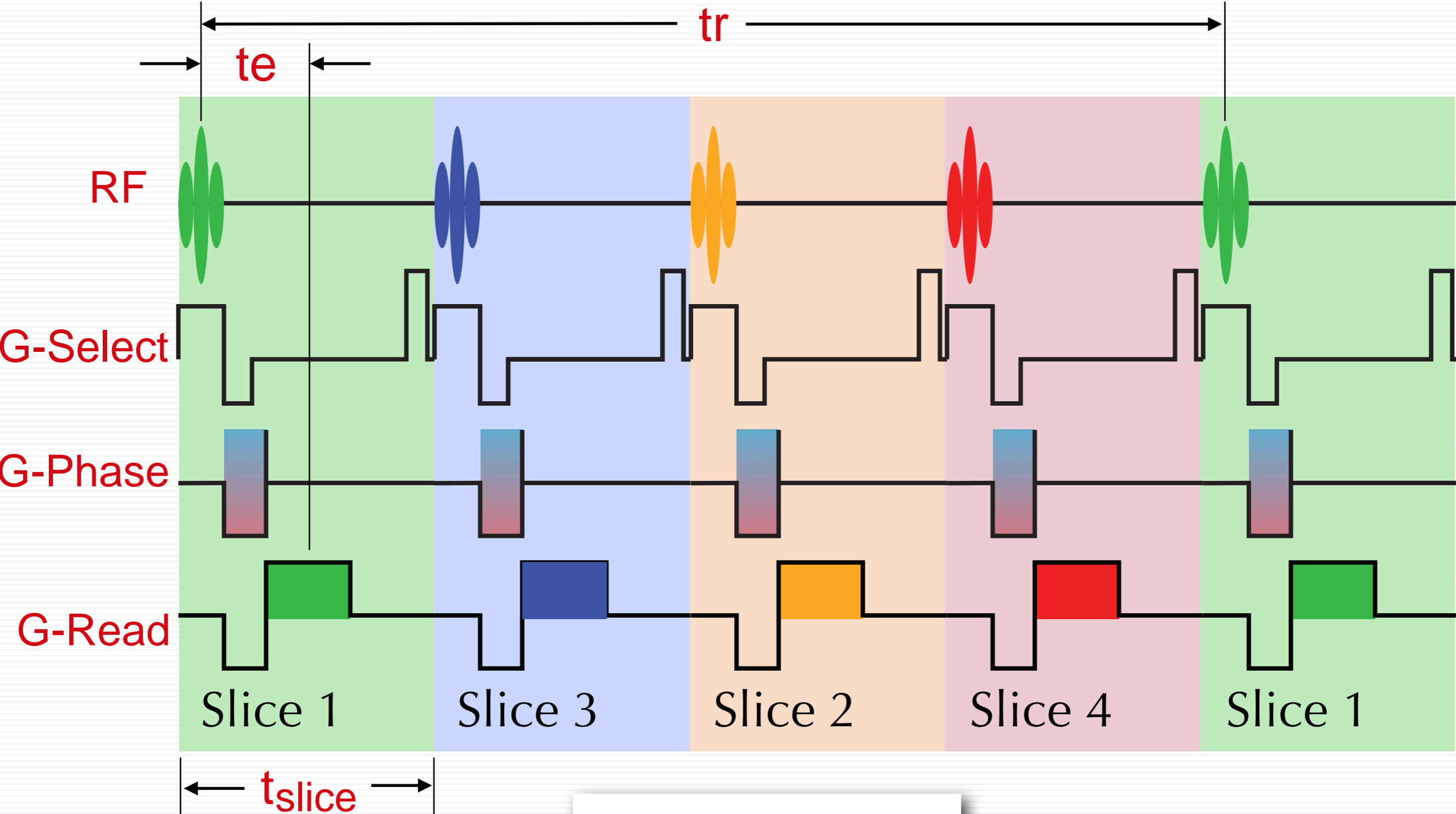
Example: if $S(kx, ky) = a + ib$,
then $S(kx, -ky) = \overline{(a + ib)} = a - ib$.



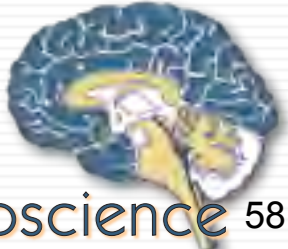
Conventional Spatial Encoding



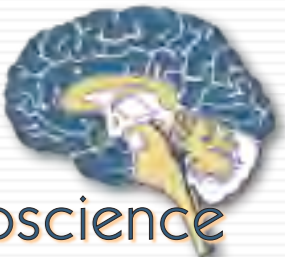
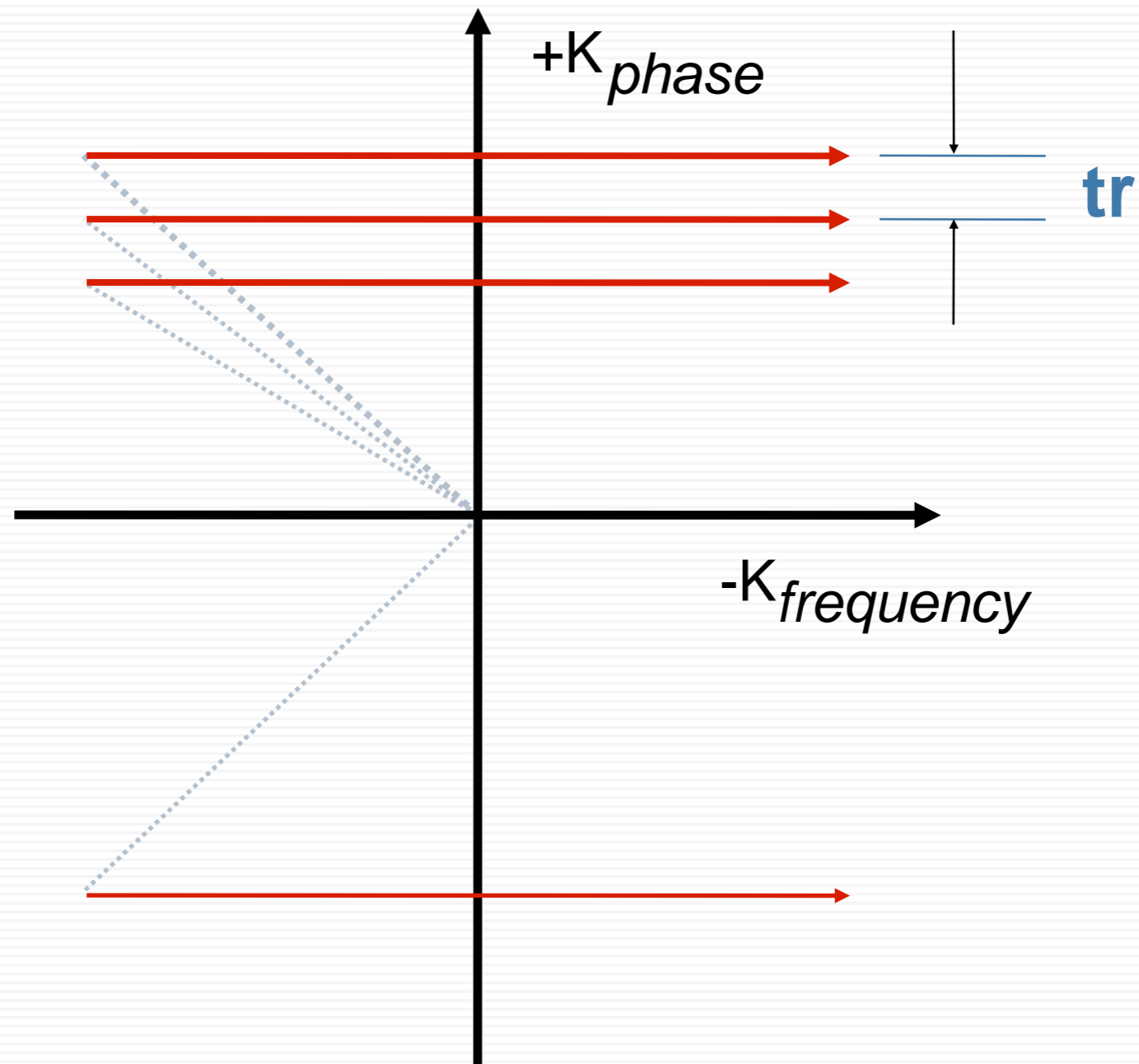
Multi-slice MRI



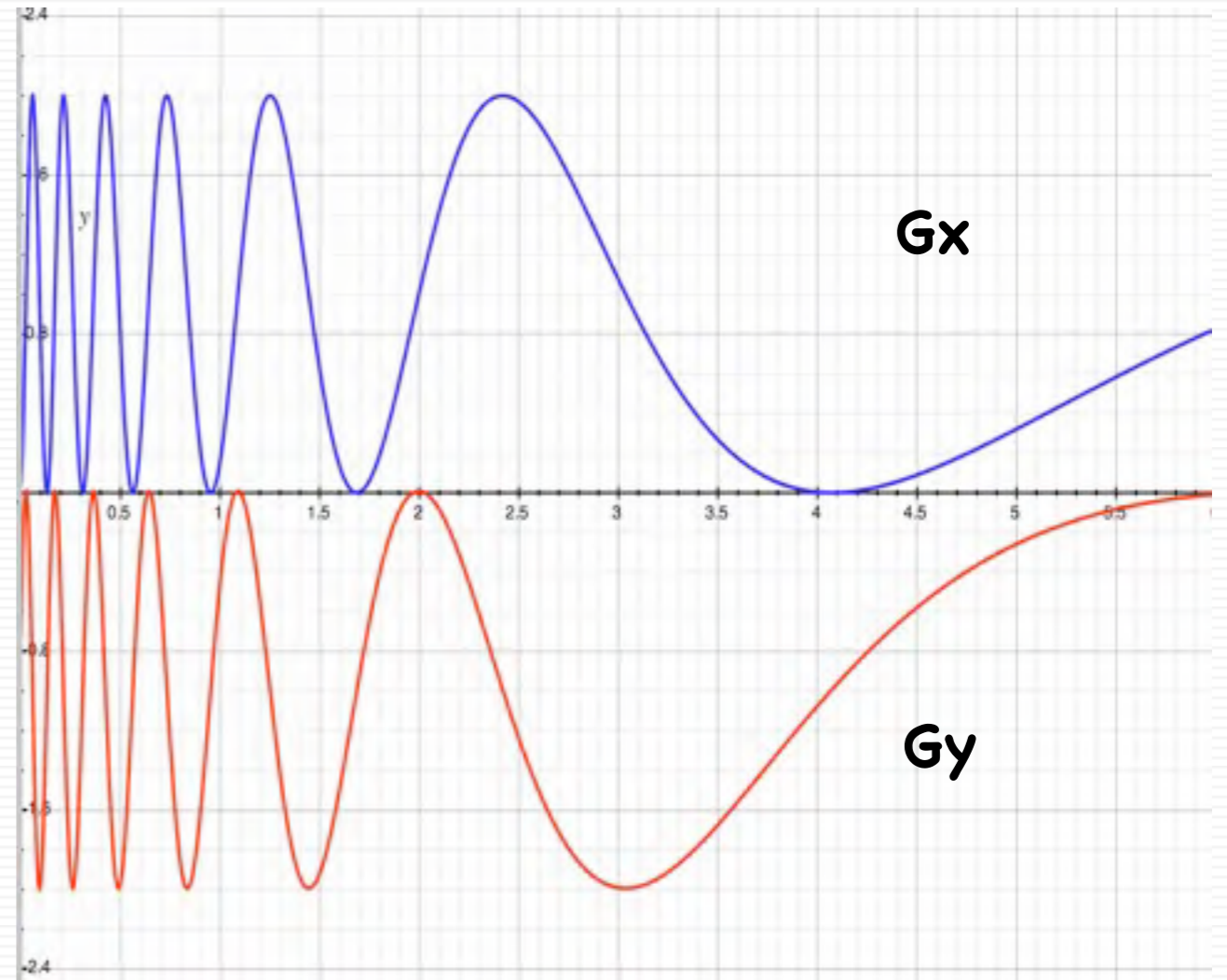
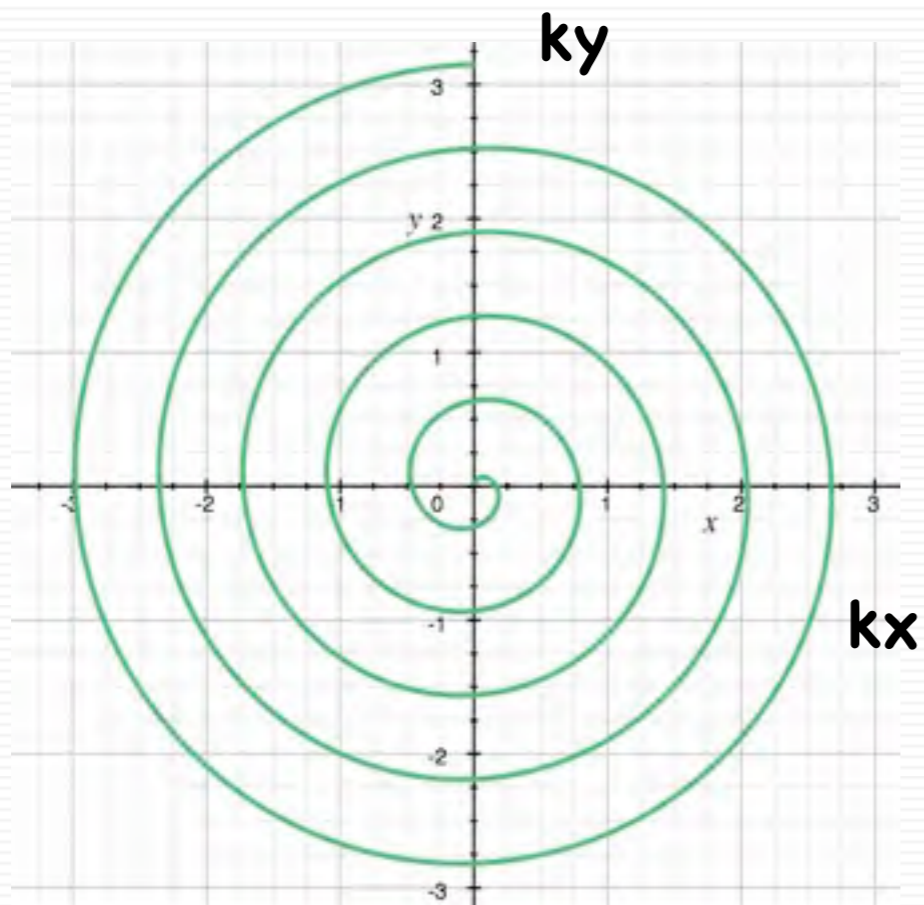
$$N_{slices} = tr / t_{slice}$$



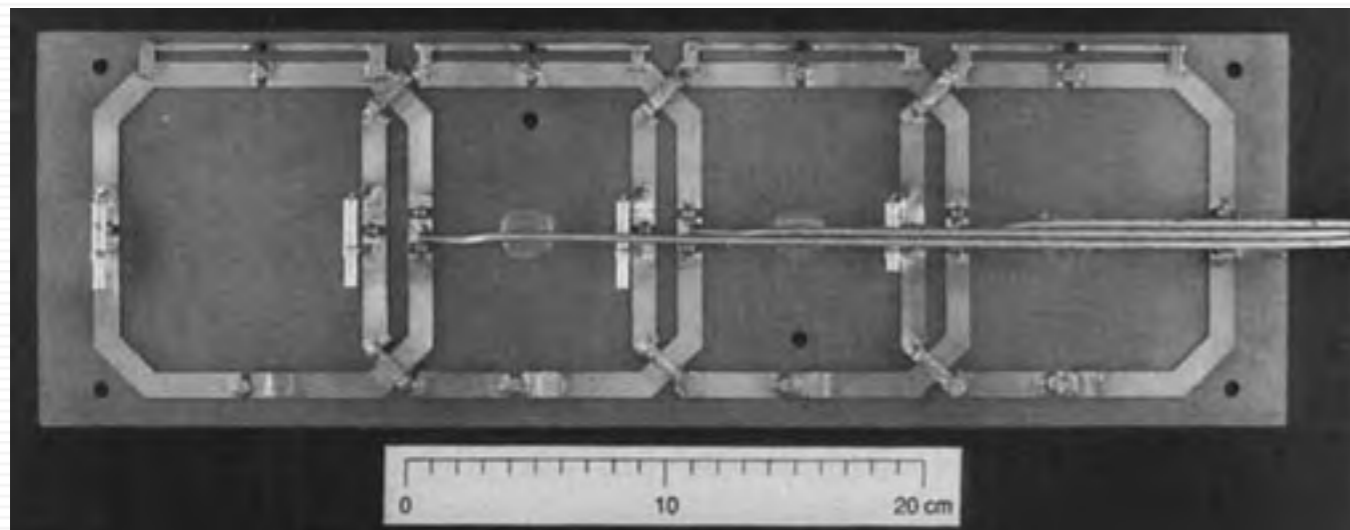
Conventional K-Space Trajectory



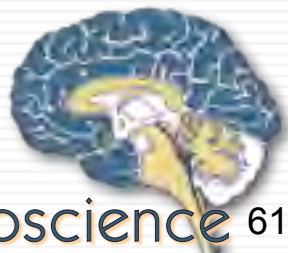
Spiral



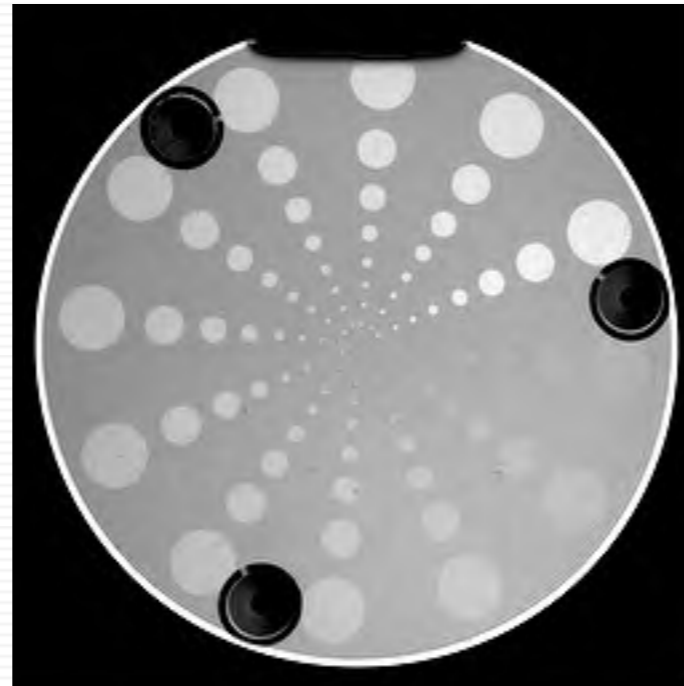
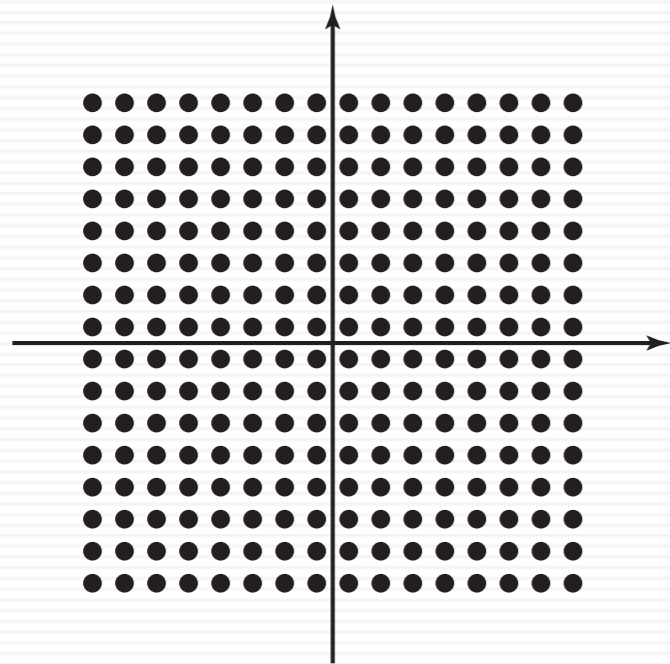
The NMR Phased Array



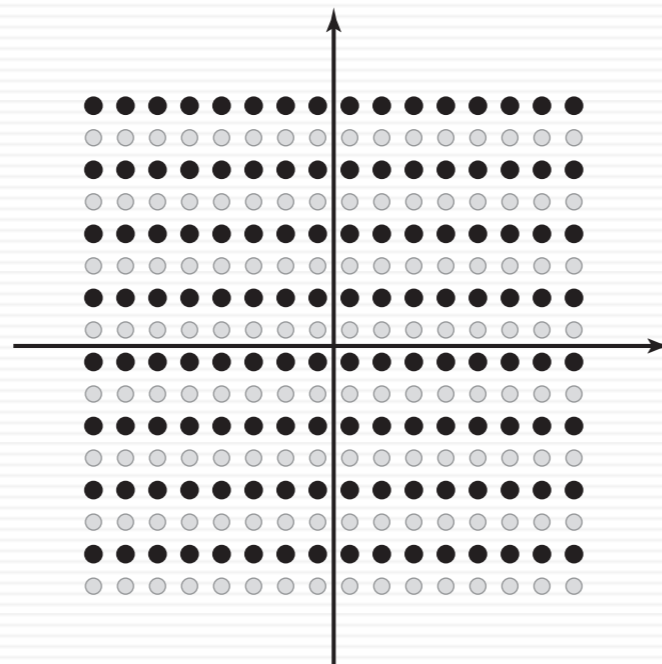
Peter Roemer. et al.,
Magn Reson Med. 16:192, 1990

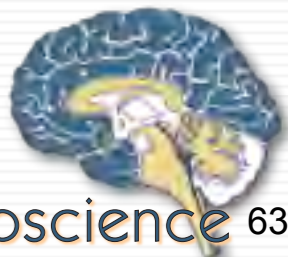
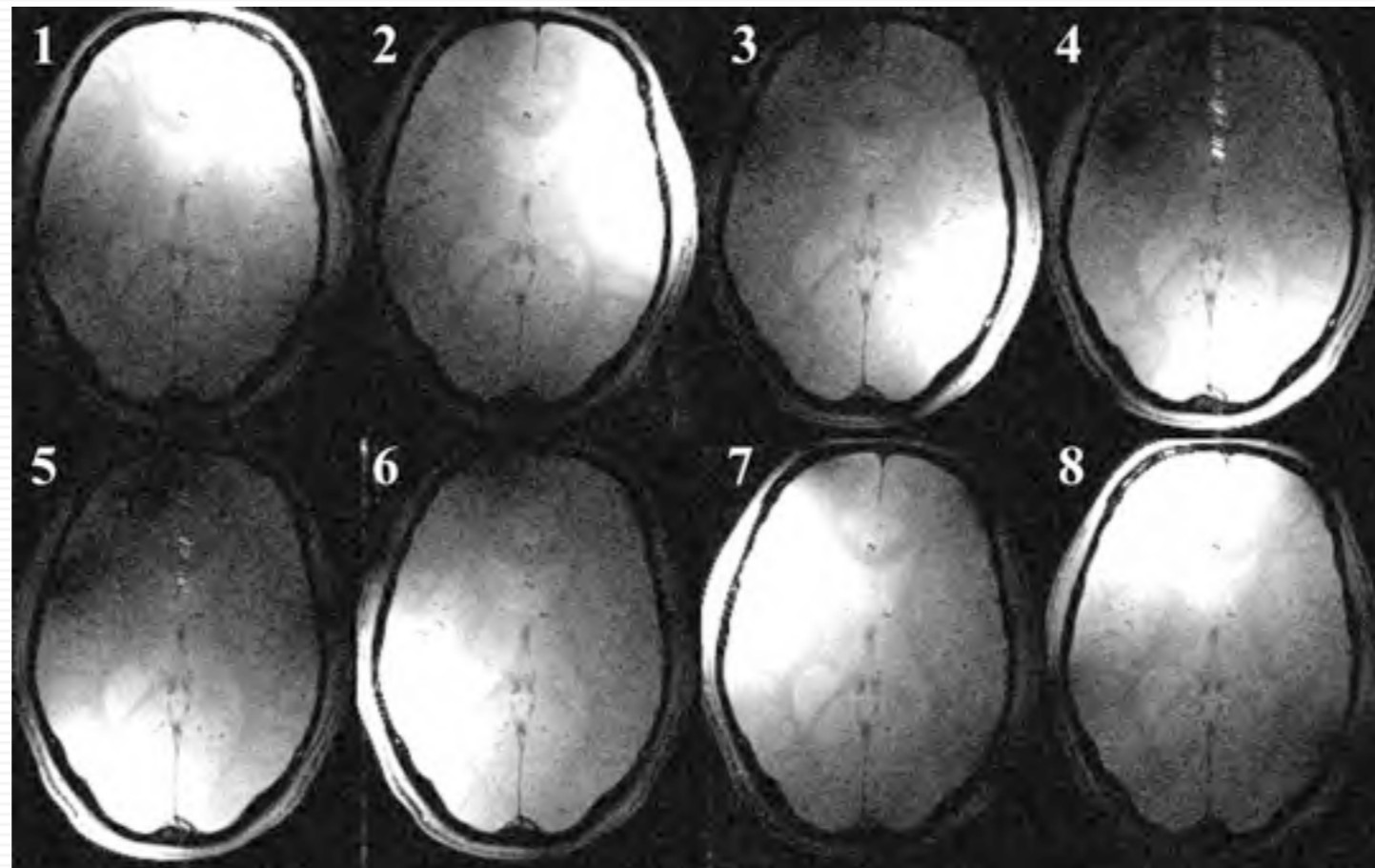


SENSE Encoding

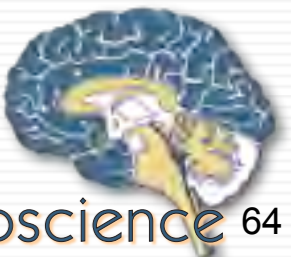


K. P. Pruessmann, et al.,
Magn Reson Med. 42:952, 1999



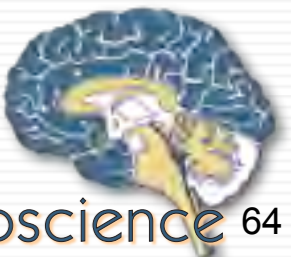


Spatial Encoding Summary



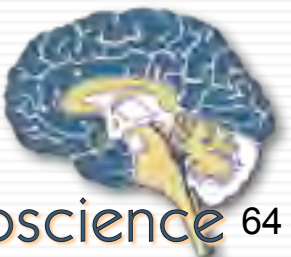
Spatial Encoding Summary

- Spatial Encoding and Contrast are Linked through the Pulse Sequence;



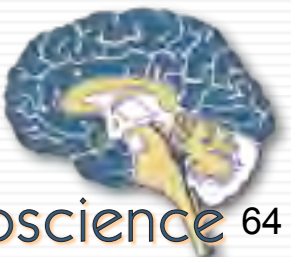
Spatial Encoding Summary

- Spatial Encoding and Contrast are Linked through the Pulse Sequence;
- The MRI Raw Data are the *2D Fourier Transform* of the Final Image (usually the *Magnitude Transform*);



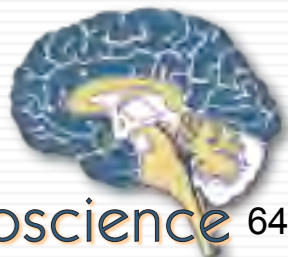
Spatial Encoding Summary

- Spatial Encoding and Contrast are Linked through the Pulse Sequence;
- The MRI Raw Data are the *2D Fourier Transform* of the Final Image (usually the *Magnitude Transform*);
- Spatial Encoding is Added through Gradient Coils;



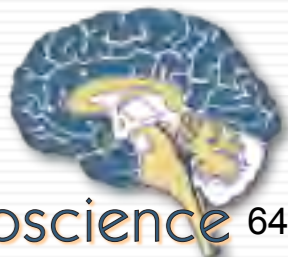
Spatial Encoding Summary

- Spatial Encoding and Contrast are Linked through the Pulse Sequence;
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- Spatial Encoding is Added through Gradient Coils;
- Hermite Symmetry of the Raw Data may be used to Reduce Scan Times;



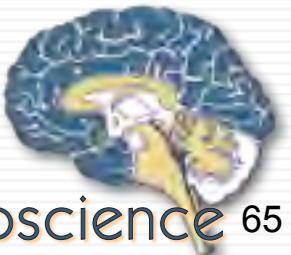
Spatial Encoding Summary

- Spatial Encoding and Contrast are Linked through the Pulse Sequence;
- The MRI Raw Data are the *2D Fourier Transform* of the Final Image (usually the *Magnitude Transform*);
- Spatial Encoding is Added through Gradient Coils;
- Hermite Symmetry of the Raw Data may be used to Reduce Scan Times;
- Literally Hundreds of Pulse Sequences are in Common Use,



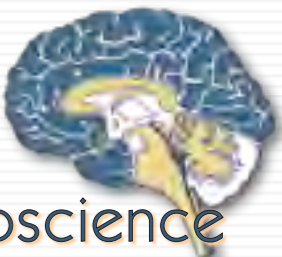
The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
- The “Pulse Sequence” Rules Everything (3)
Seventh Inning Stretch
- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)
- Image Quality and Artifacts (48)

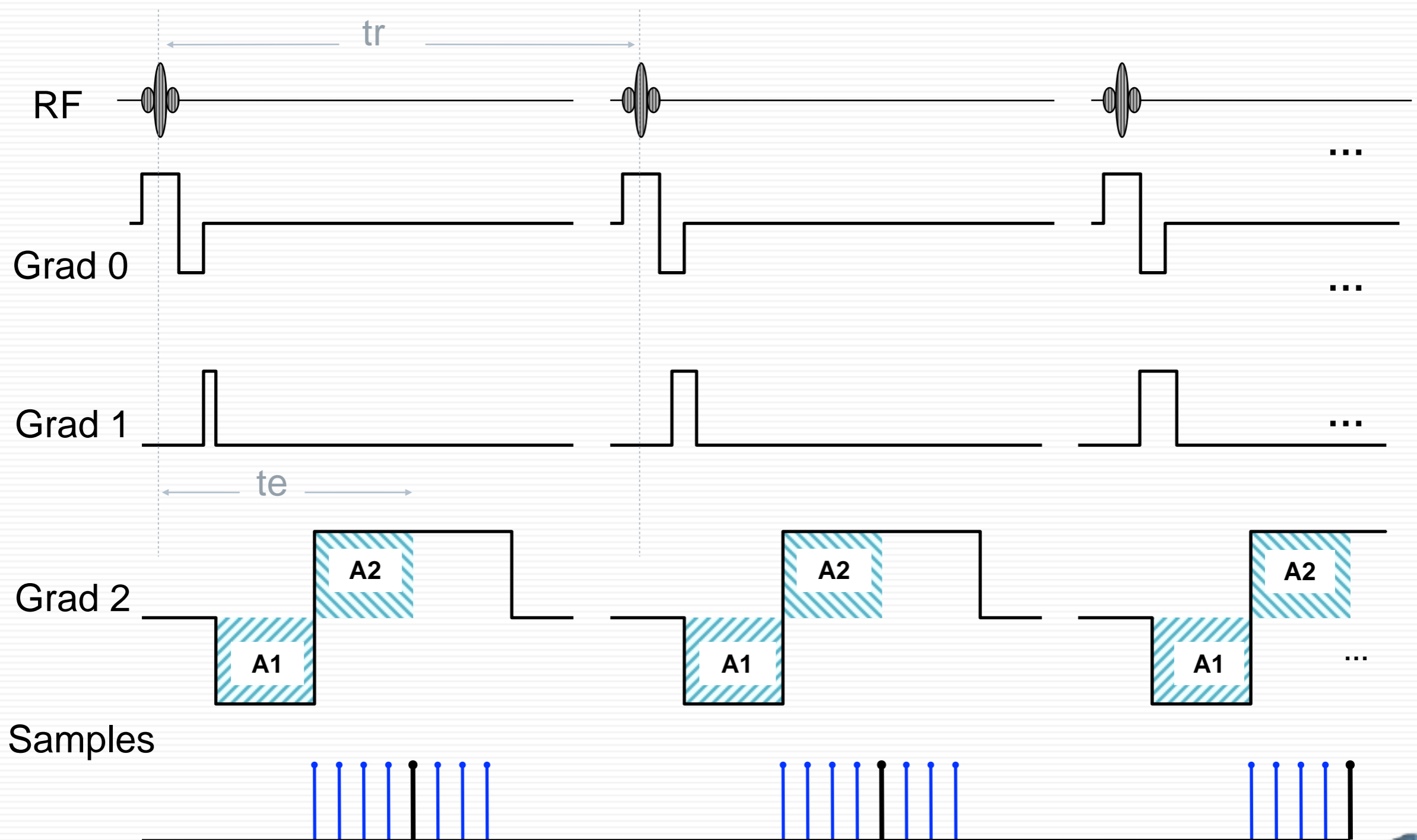


A Pulse Sequence Controls

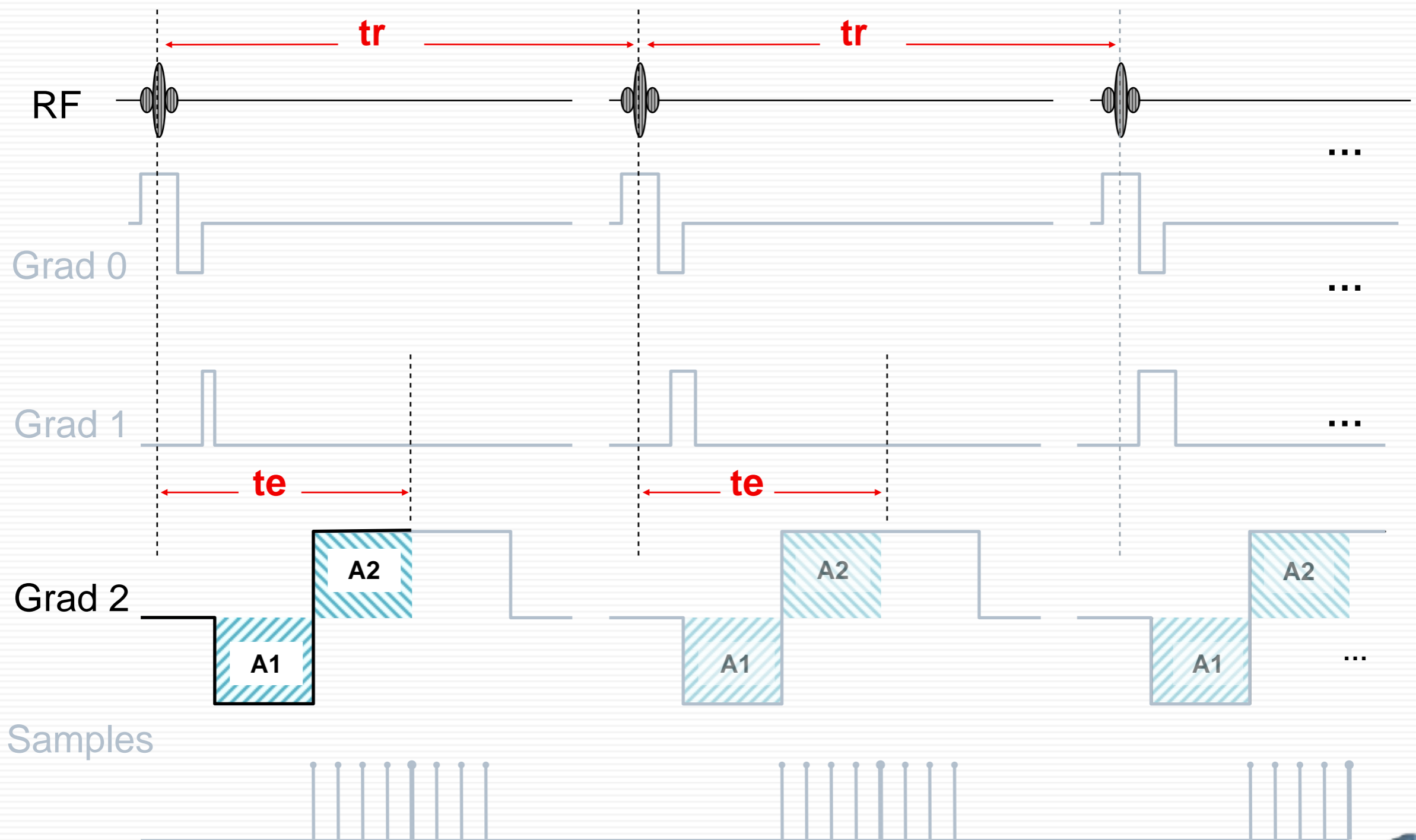
- Slice Location
- Slice Orientation
- Slice Thickness
- Number of Slices
- Resolution
(*FOV and Matrix*)
- Contrast
TR, TE, TI, Flip Angle, Diffusion, etc...
- Artifact Correction
Saturation Pulses, Flow Comp, Fat Suppression, etc...



Conventional Spatial Encoding



Contrast Encoding



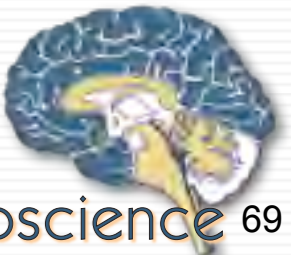
The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
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Seventh Inning Stretch

- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)

- Image Quality and Artifacts (48)



Reduced Flip Angle Imaging

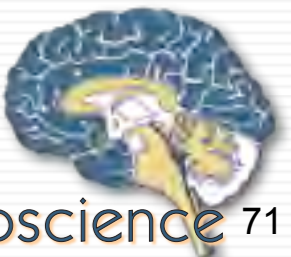
Outline

- Determinants of Imaging Time
- TR, Saturation and Image Quality
- Reduced Flip Angle Techniques
 - FLASH (=SPGR)
 - FISP (=GRASS)
- Gradient Echoes
- Applications of Shallow Flip Imaging
- Ultra-Fast Imaging

Determinants of Imaging Time

Scan Time =

Repetition Time (TR)
x Number of Phase Encodes
x NEX (Averages)
x Number of 3D Steps



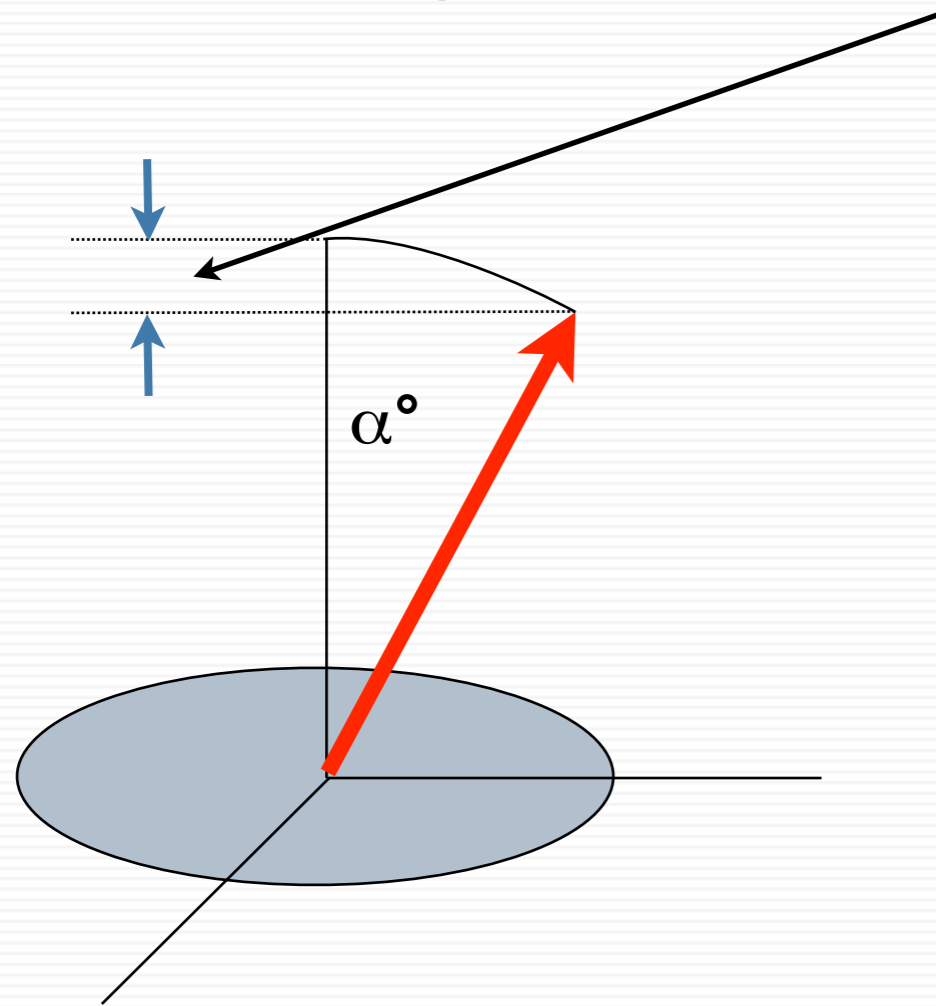
TR and Image Quality

Reduced TR Yields:

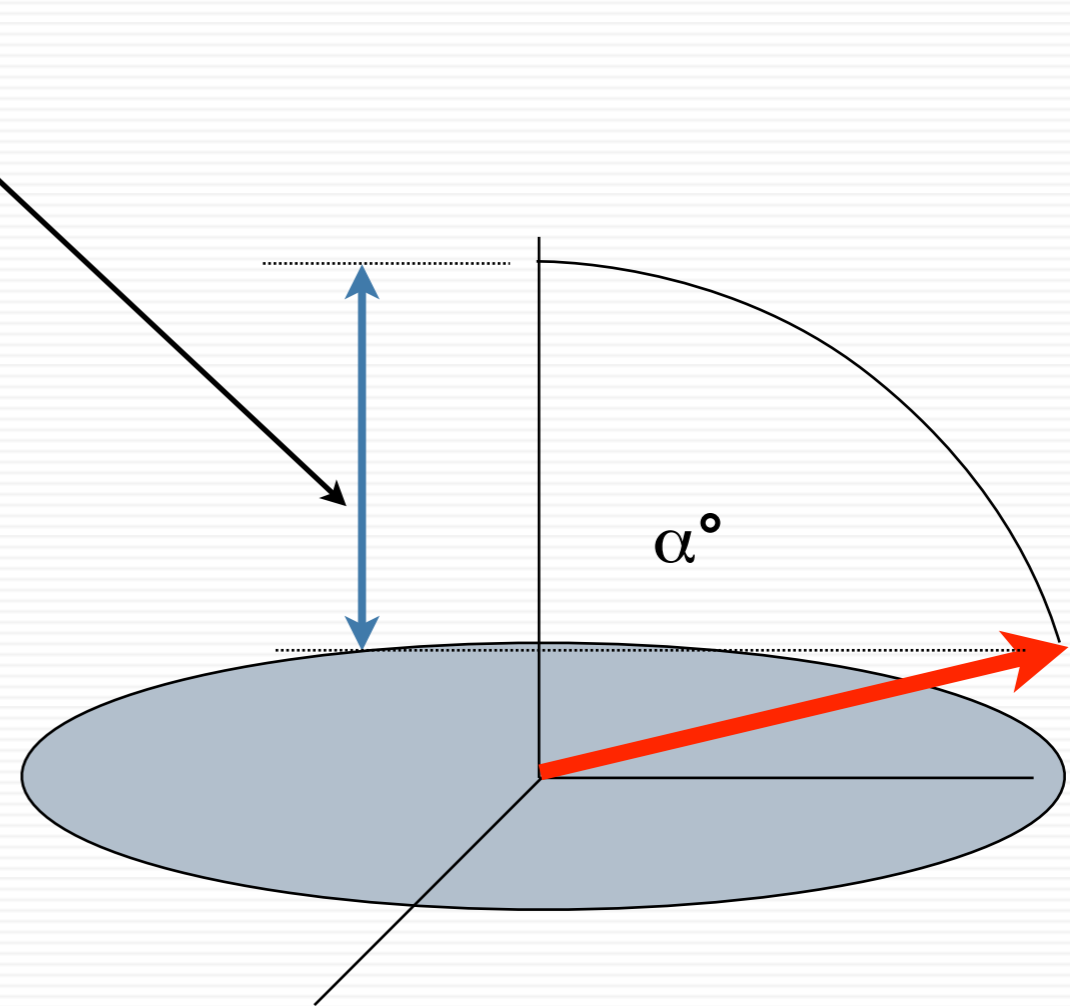
- Decreased Scan Time
- Increased T1 Contrast
- Reduced (Useable) T2 Contrast
- Reduced Signal to Noise Ratio
- Increased Power Deposition
- Reduced Slice Coverage

Signal and Flip Angle

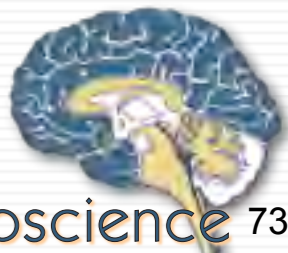
Loss of Longitudinal Magnetization



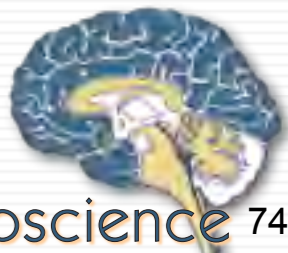
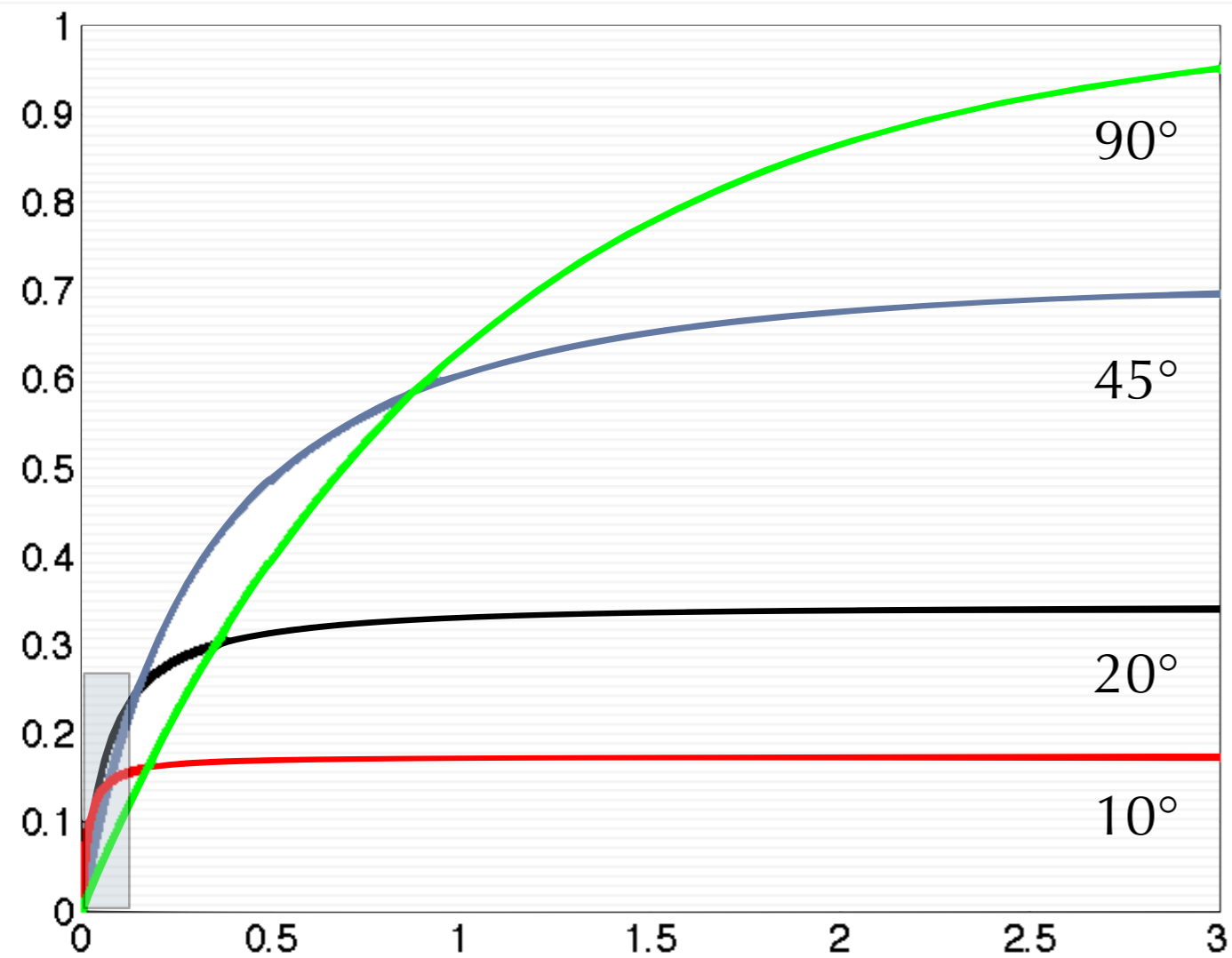
Small Flip Angle



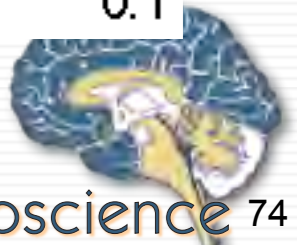
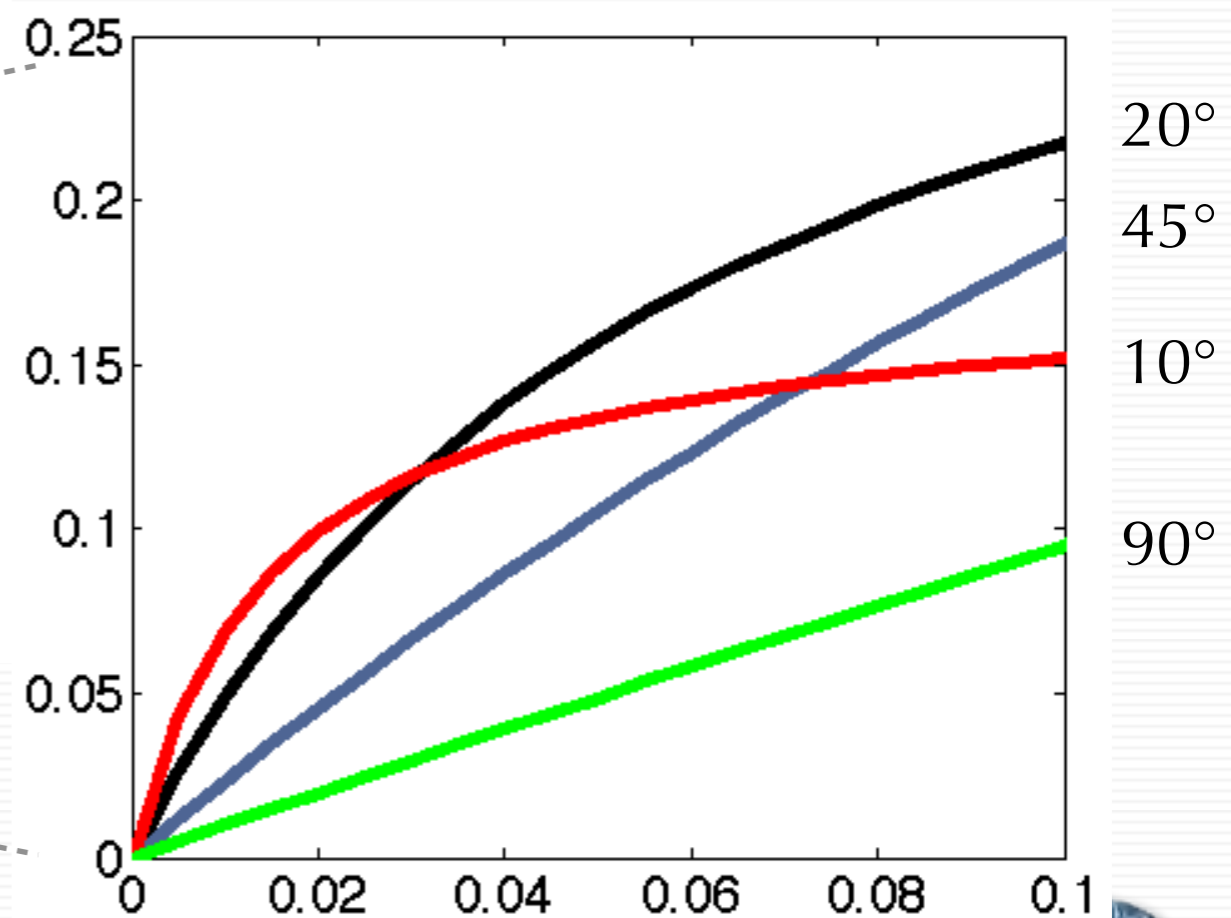
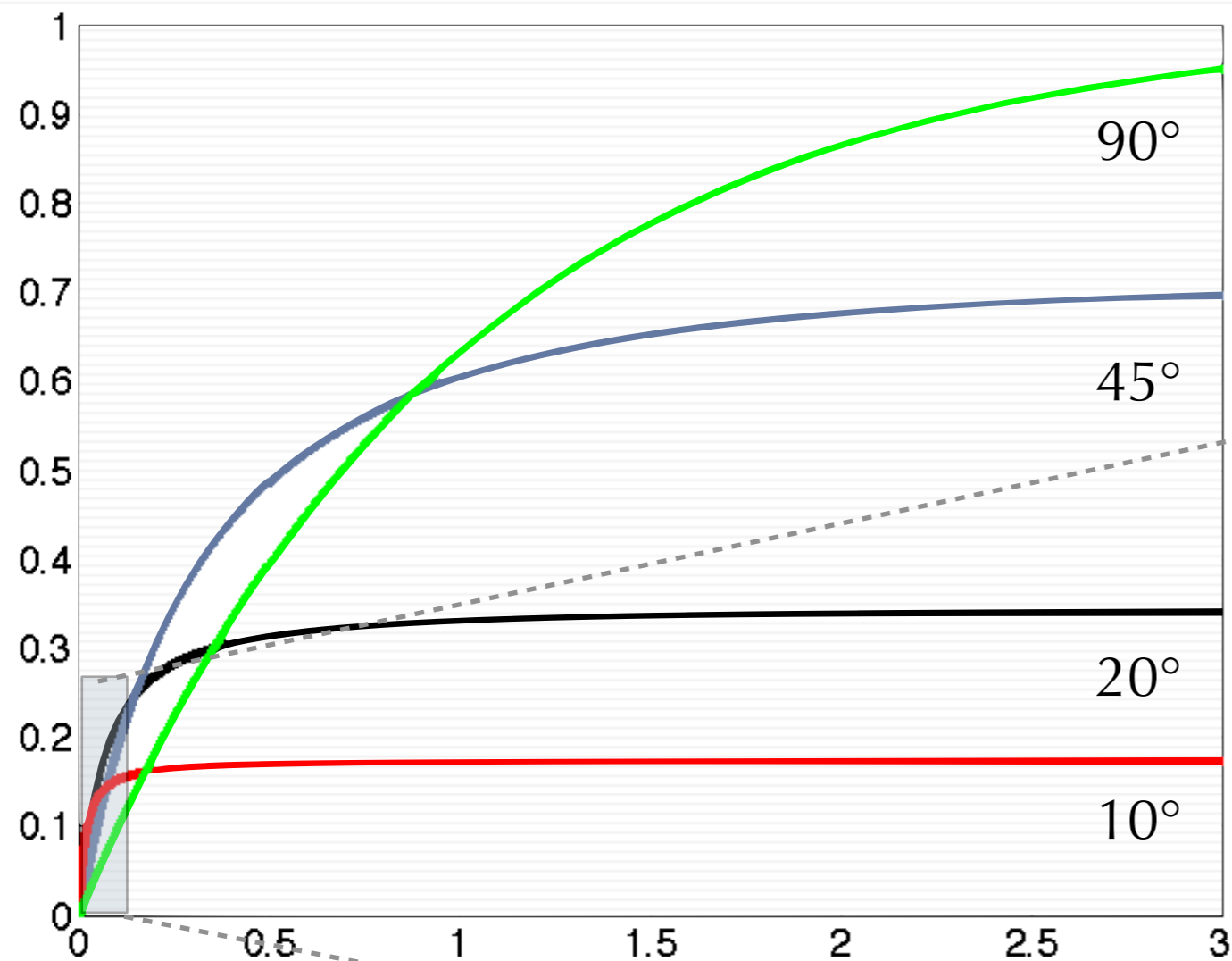
Large Flip Angle



Flip Angle and TR/T1



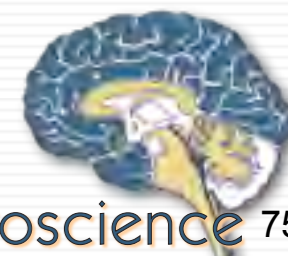
Flip Angle and TR/T1



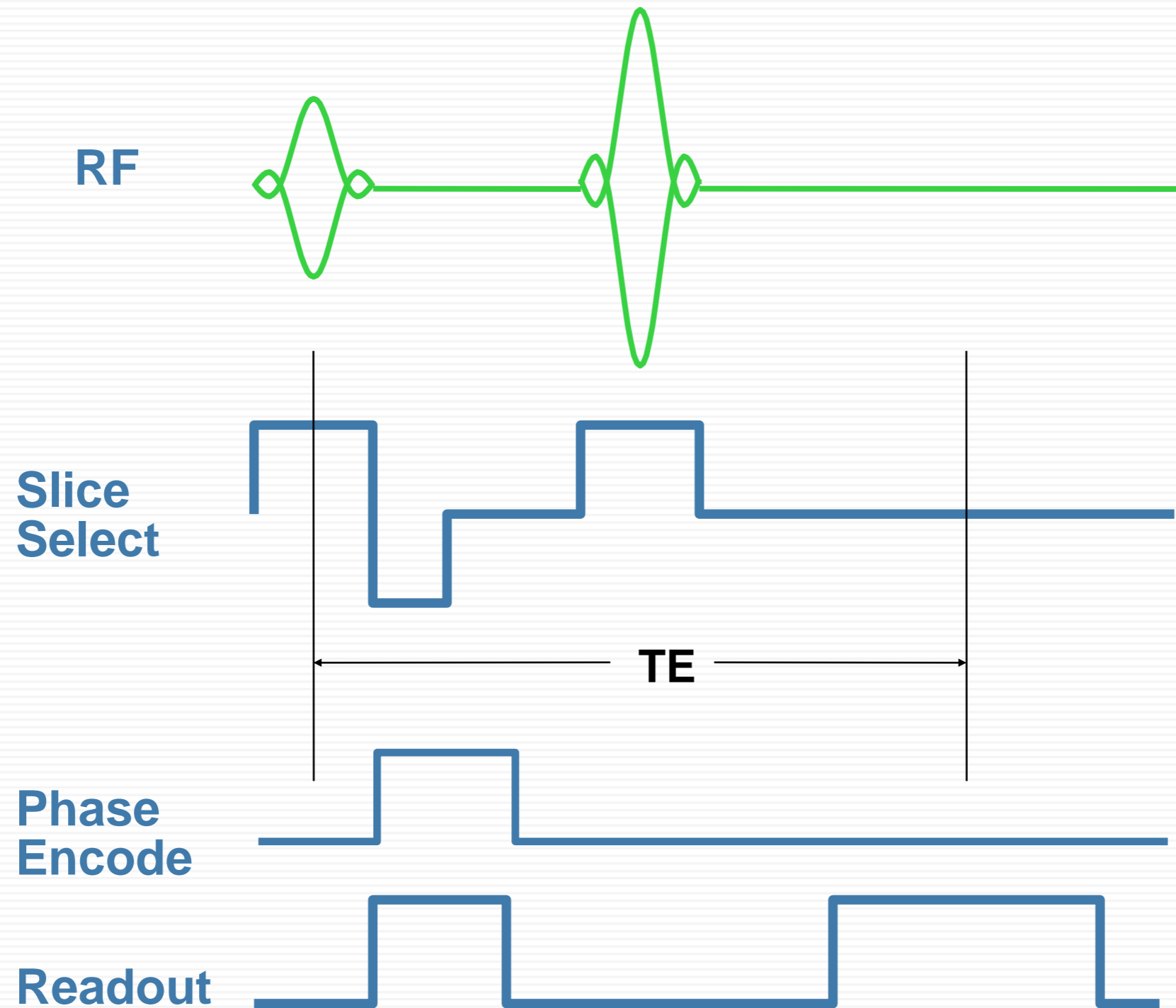
Contrast and Flip Angle

Large Flip Angles	Short	Long
Long	Proton Density	T2* Weighted
Short	T1 Weighted	

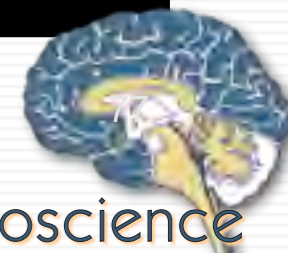
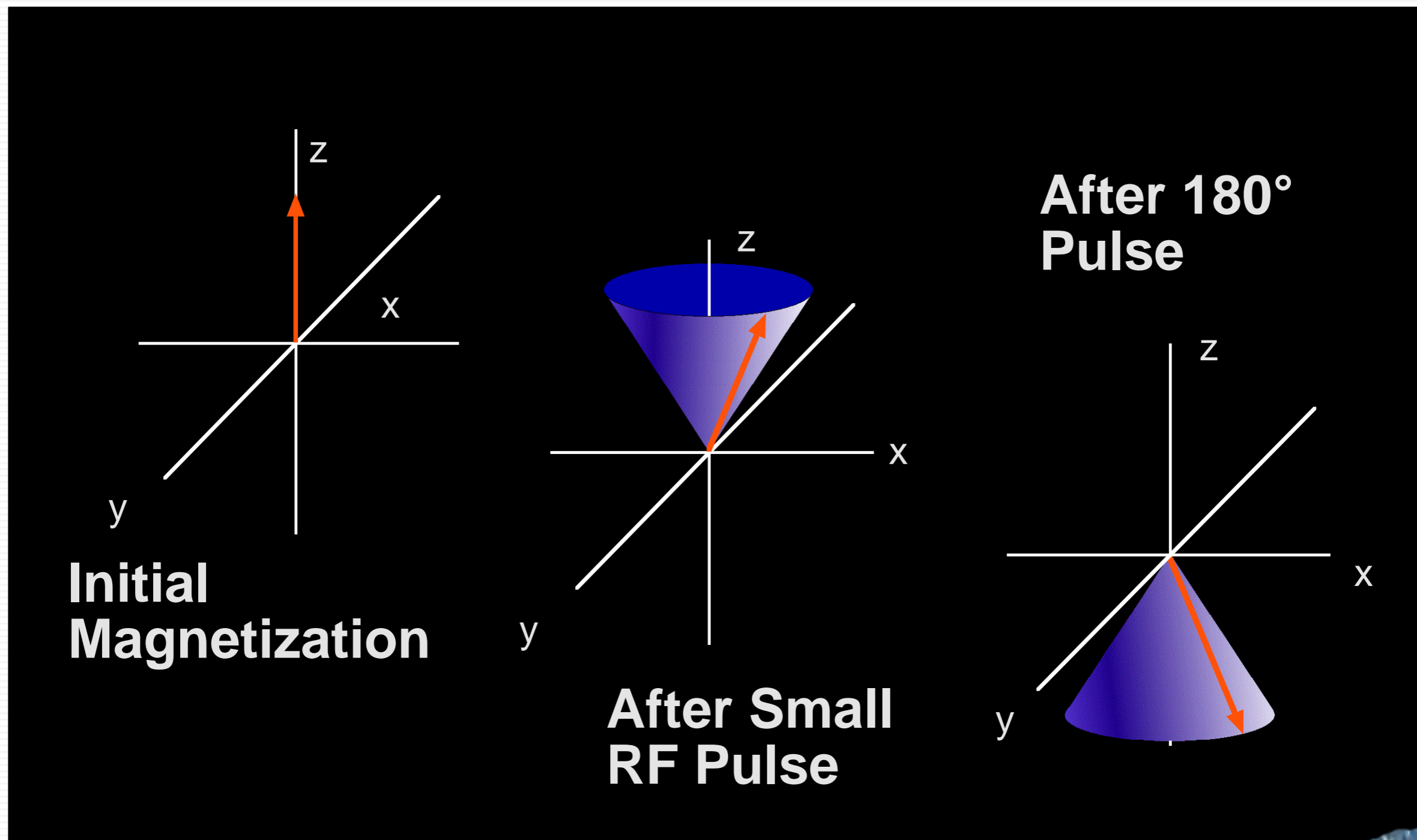
Small Flip Angles	Short	Long
Long	Proton Density	T2* Weighted
Short	Proton Density	T2* Weighted



Spin Echo Sequence



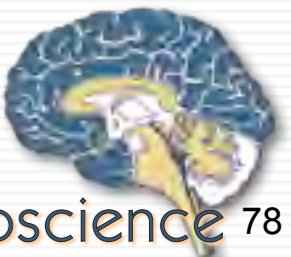
A 180° Pulse is not used in FLASH imaging



T2 and T2*

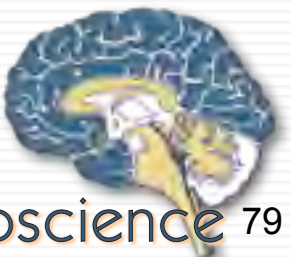
T2: Transverse Magnetization Decay
from Spin-Spin Interactions

T2*: Transverse Magnetization Decay
from Local Magnetic Field
Variations



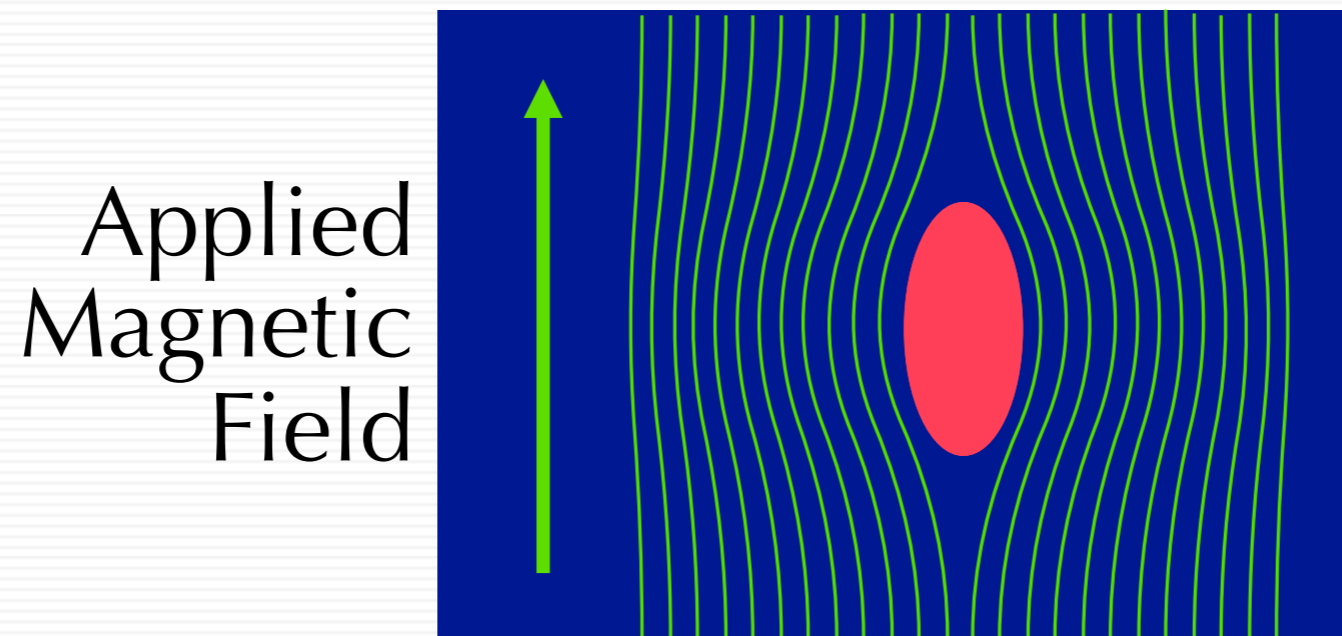
Magnetic Susceptibility

The Extent to Which a Substance Becomes “MAGNETIZED” when Placed Within a Magnetic Field

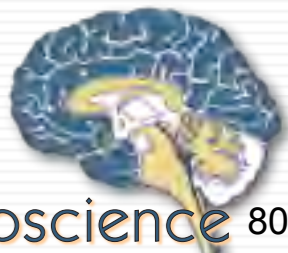


Magnetic Susceptibility

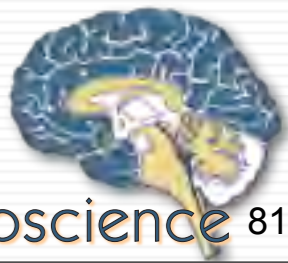
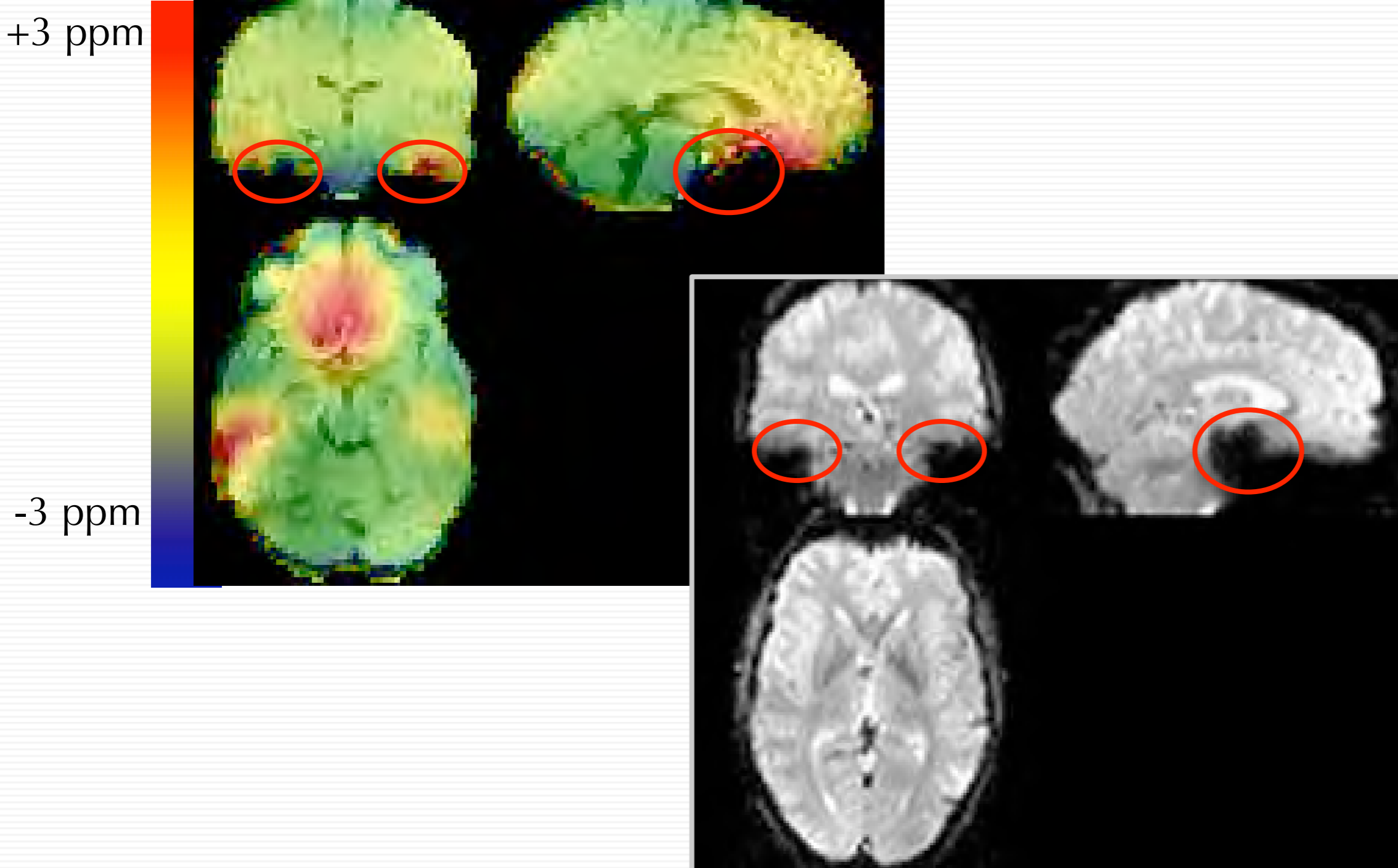
The Extent to Which a Substance Becomes “MAGNETIZED” when Placed Within a Magnetic Field



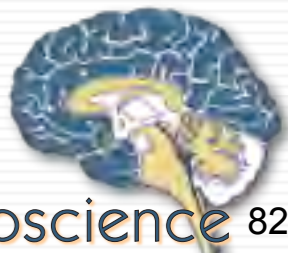
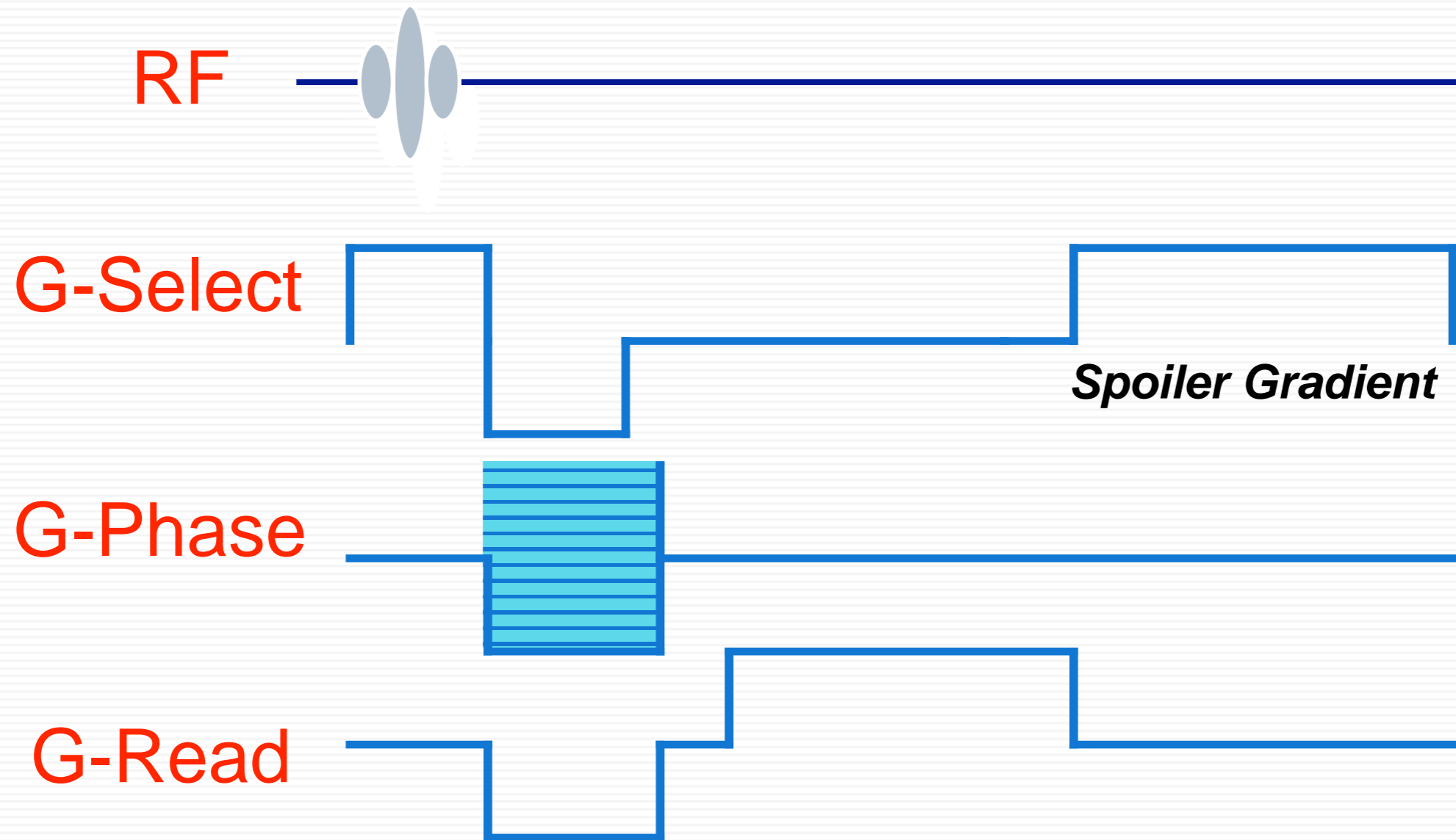
Objects with Susceptibility Different than Air Distort the Magnetic Field



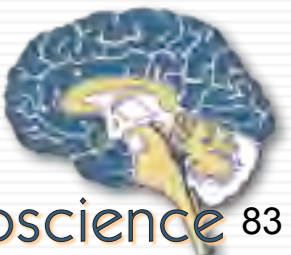
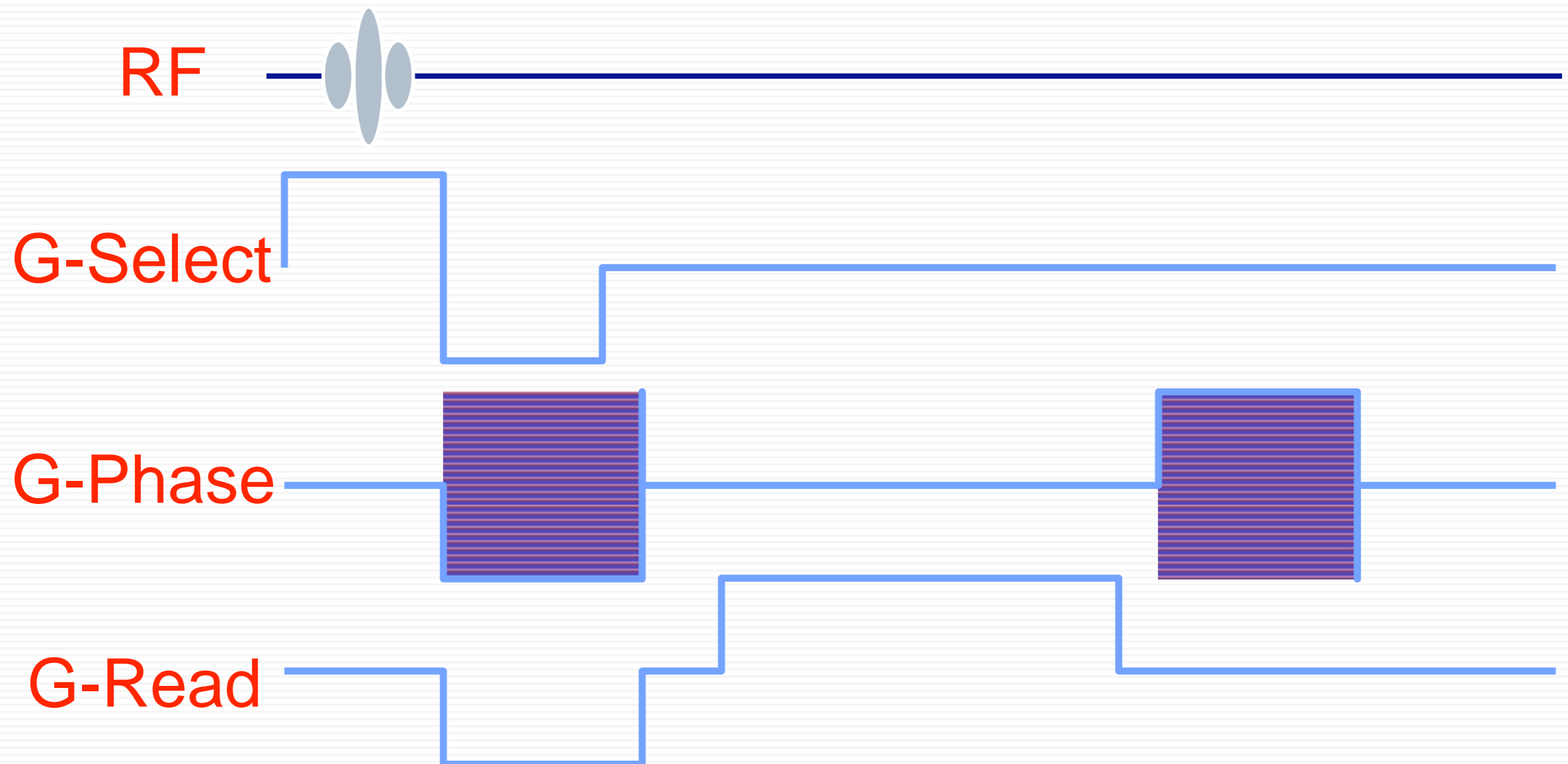
Local field Variations Result in Signal Loss



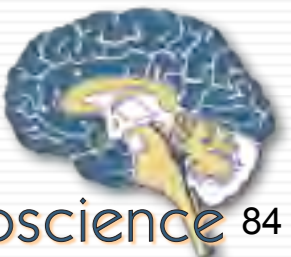
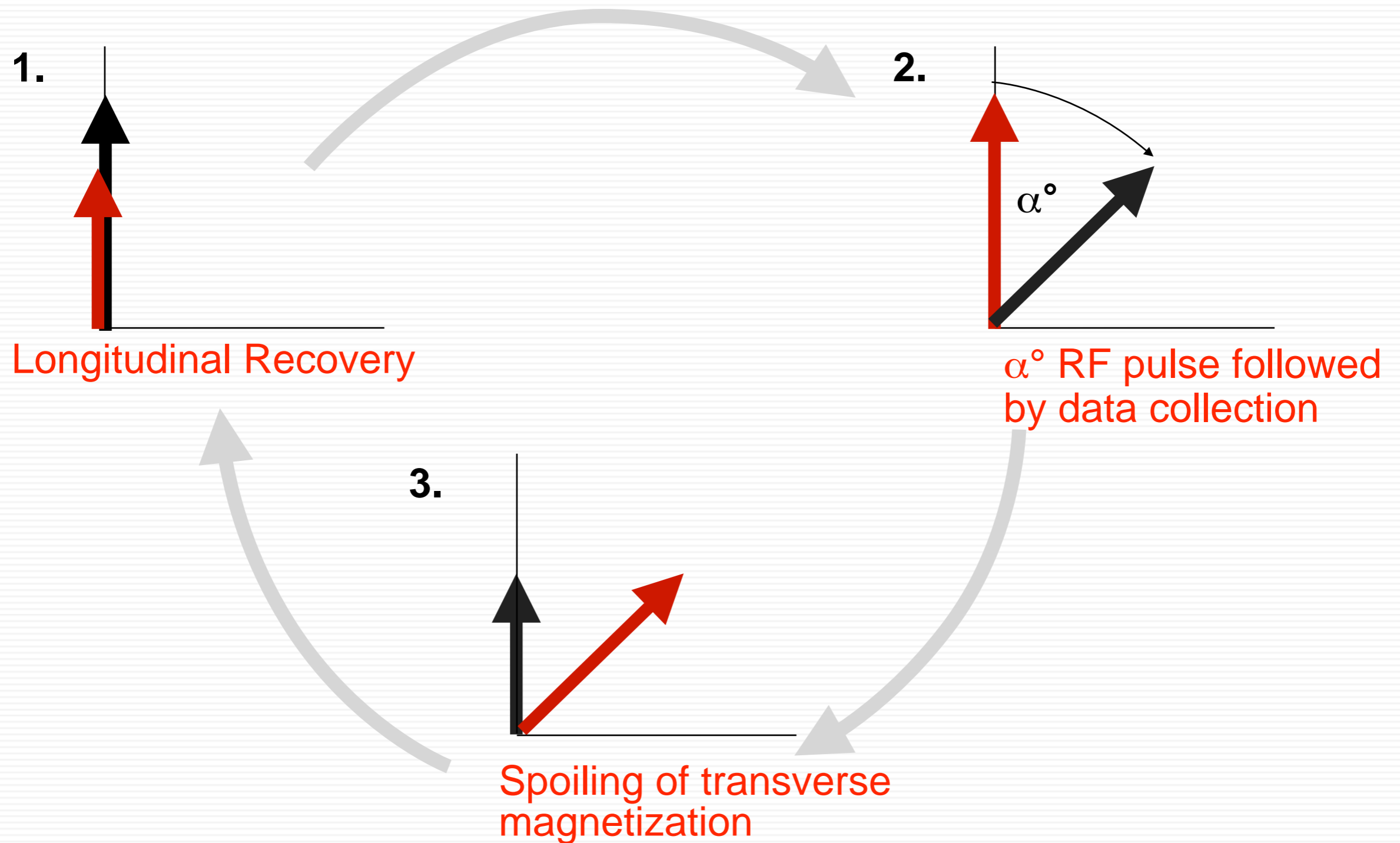
FLASH Timing Diagram



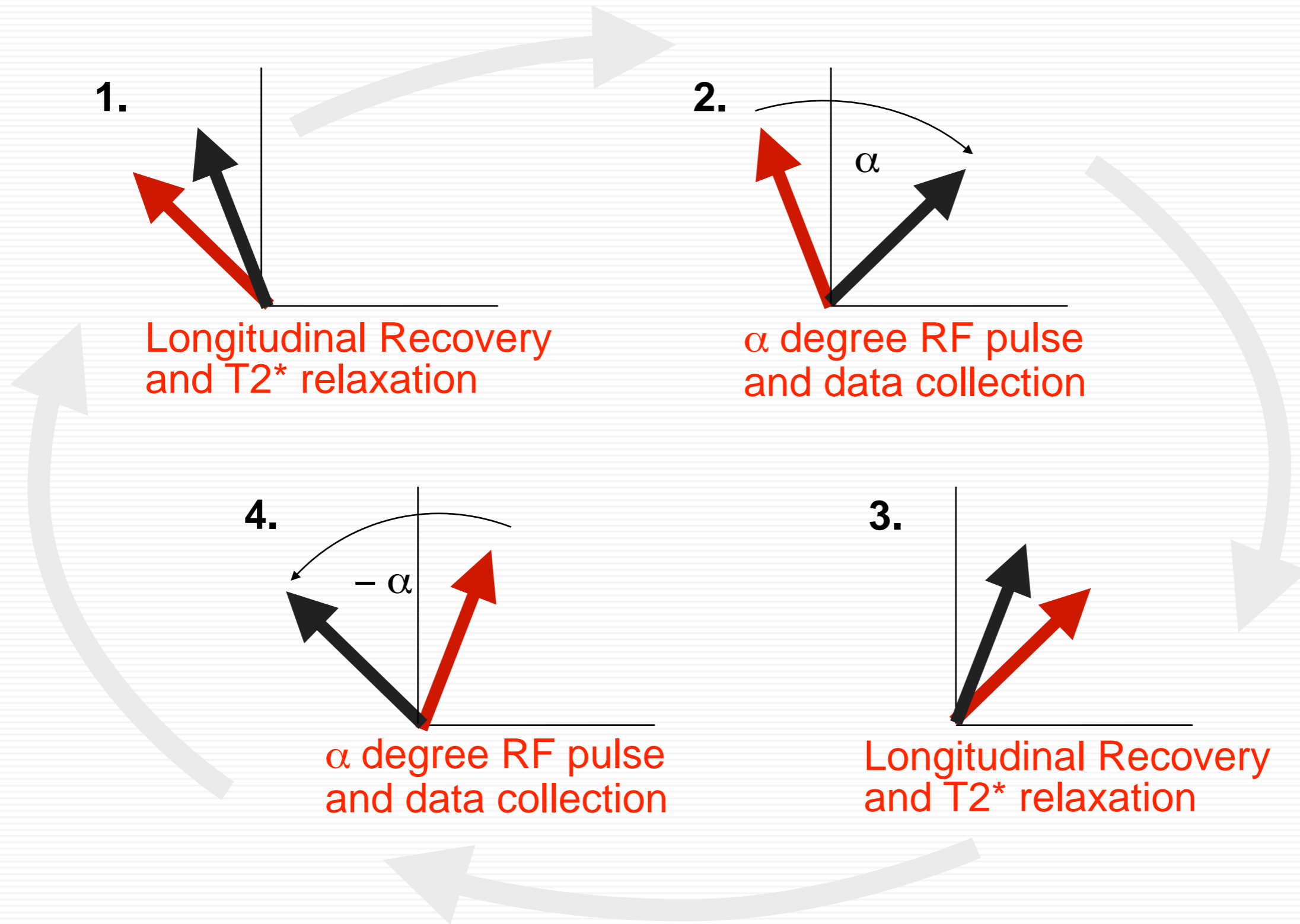
FISP (GRASS) Timing Diagram



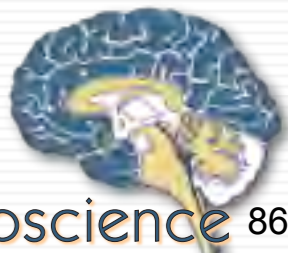
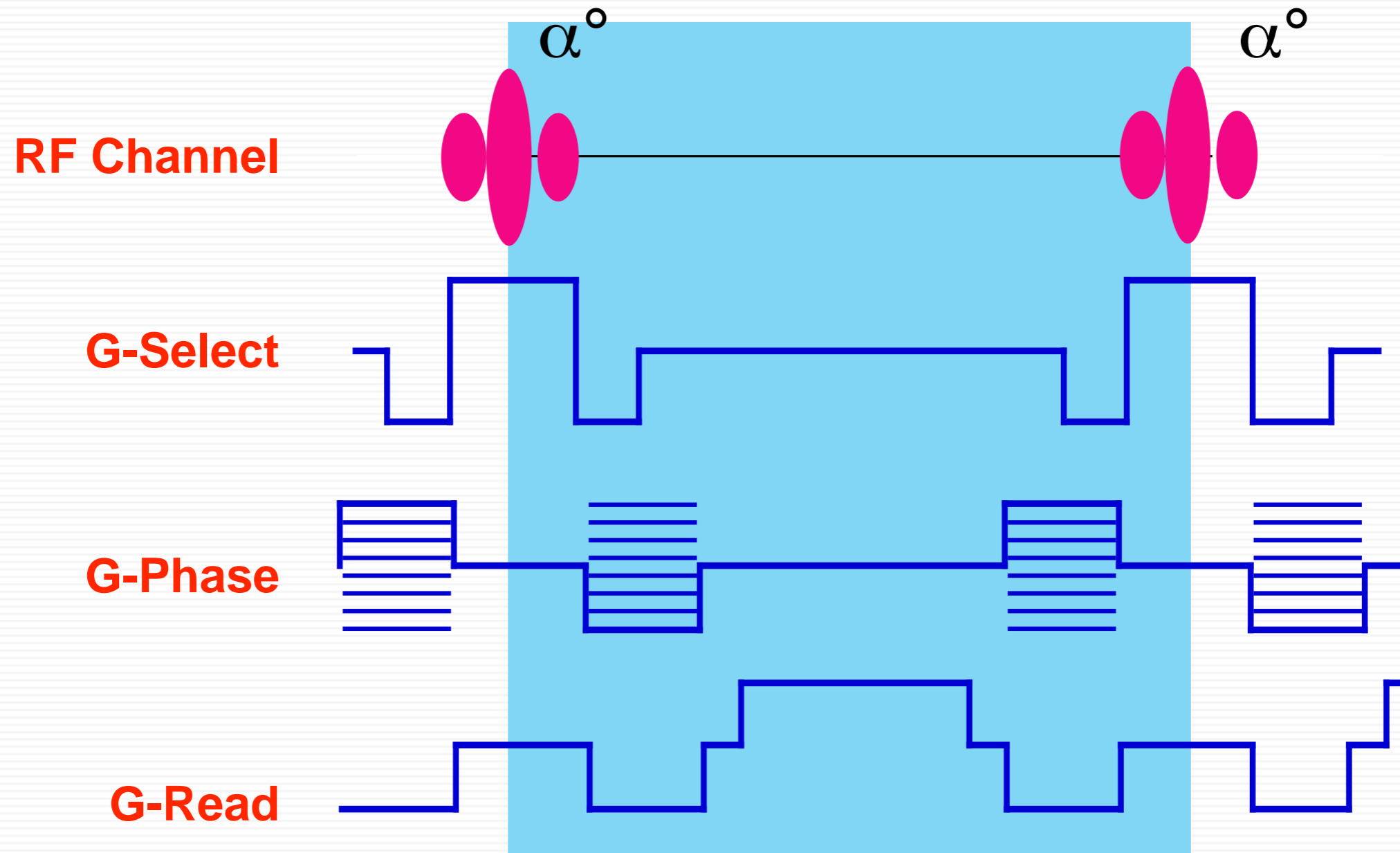
the FLASH Magnetization Cycle



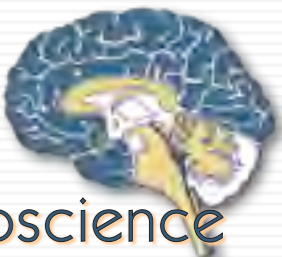
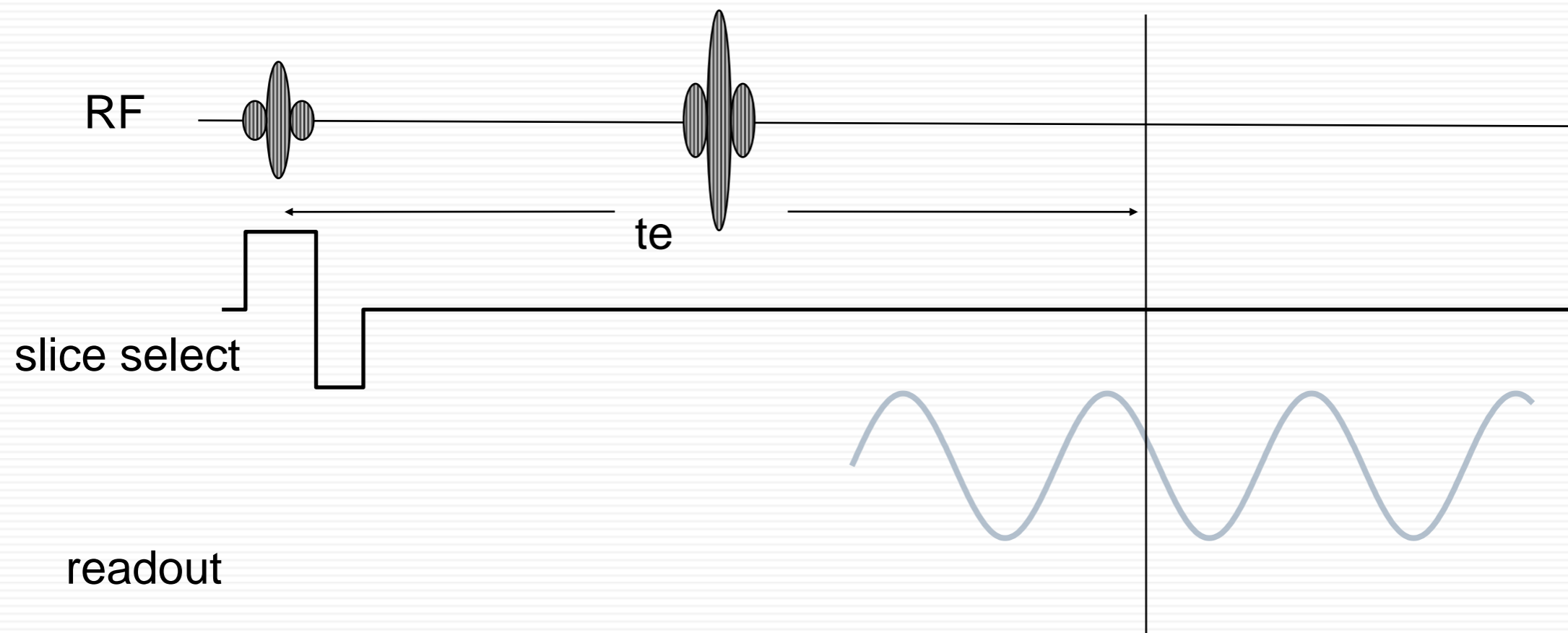
The SSFP Magnetization Cycle



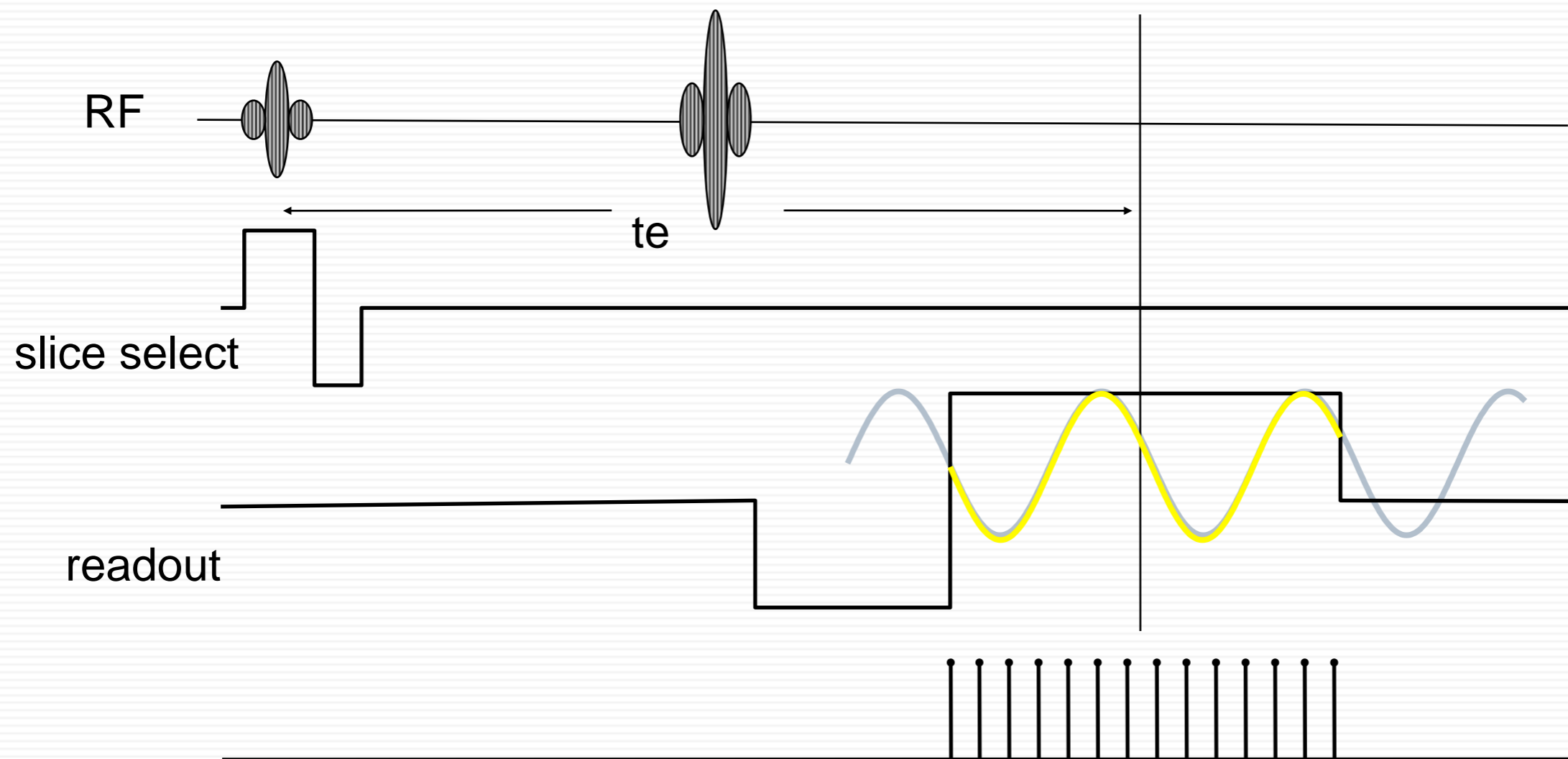
SSFP Sequence



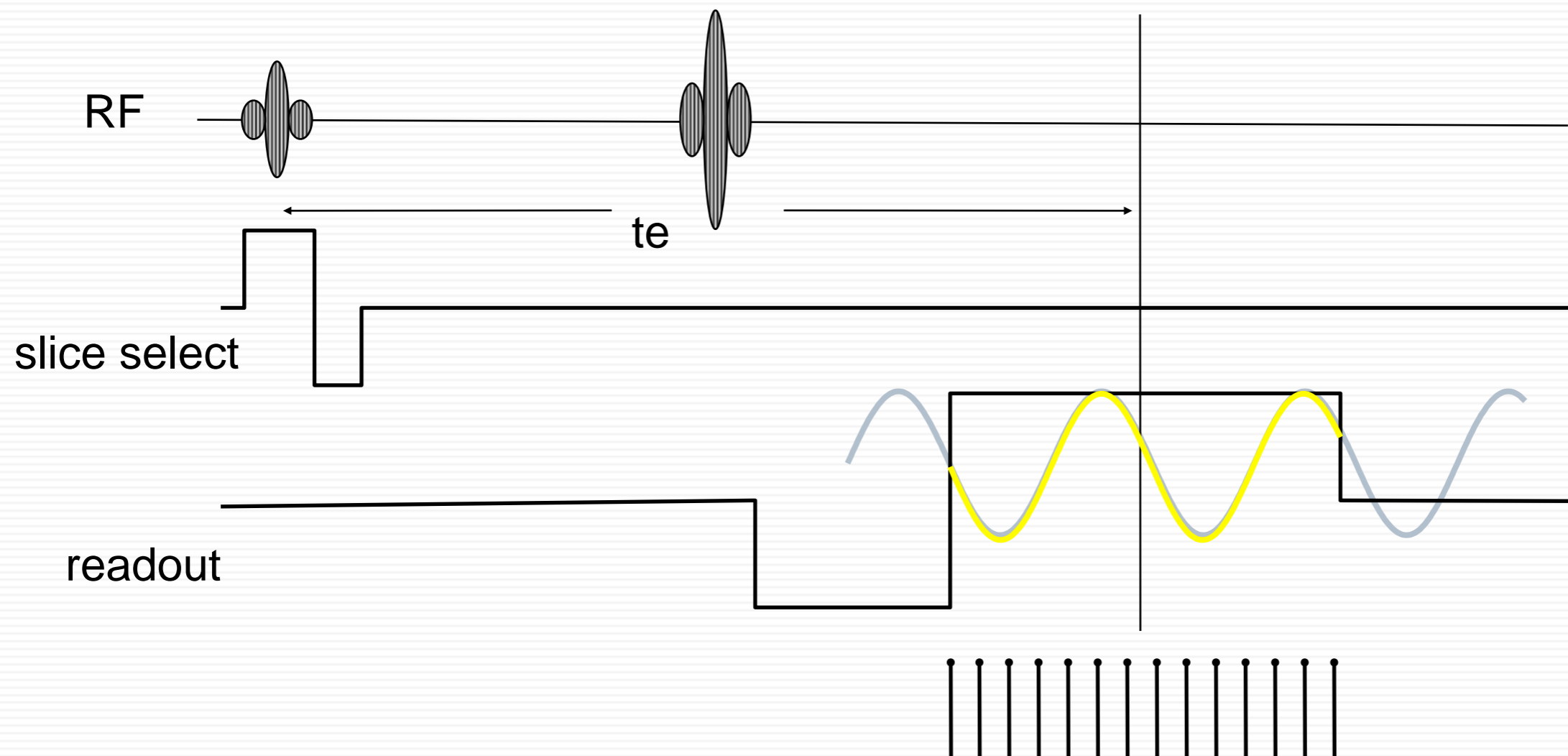
Phase Maps



Phase Maps



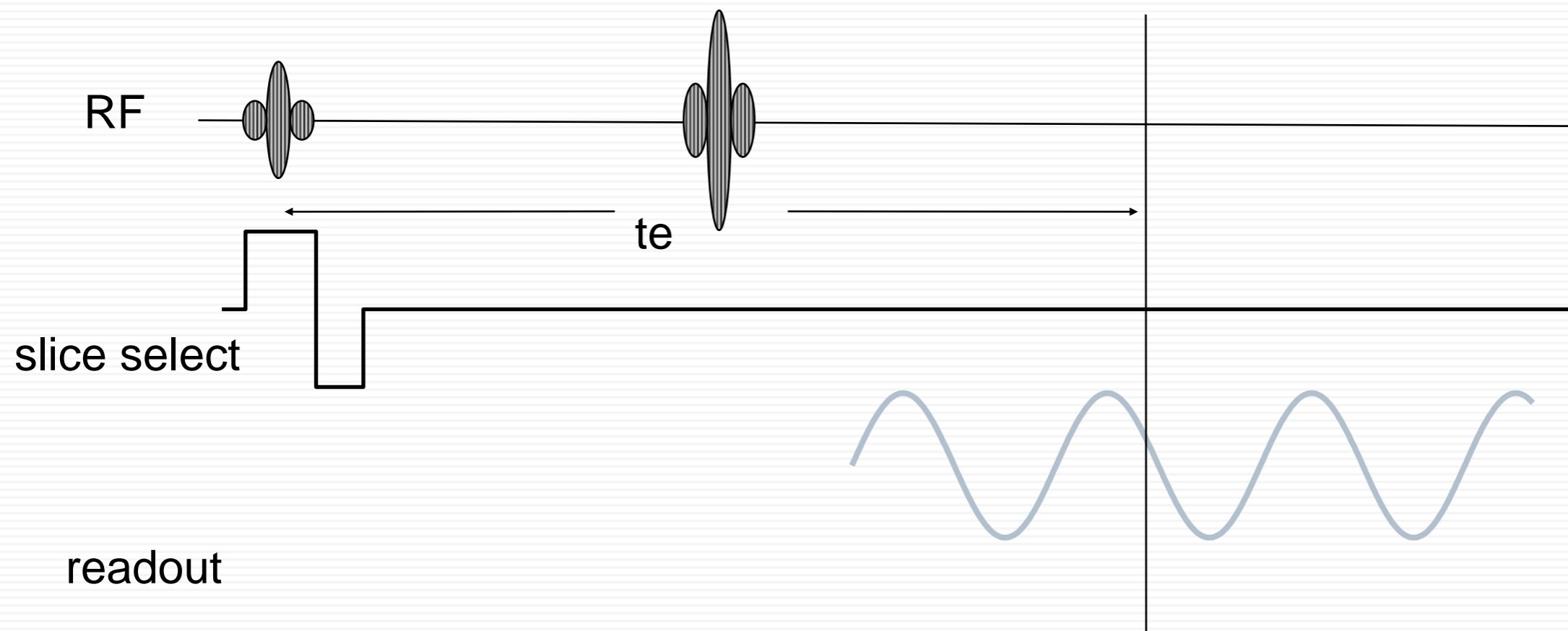
Phase Maps



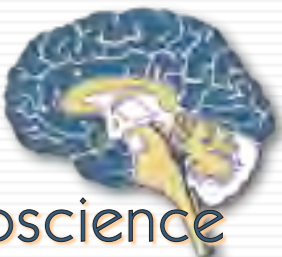
- Time shift in data collection amounts to a phase offset
- Spins precessing at different rates (different magnetic fields) will acquire different phase shifts



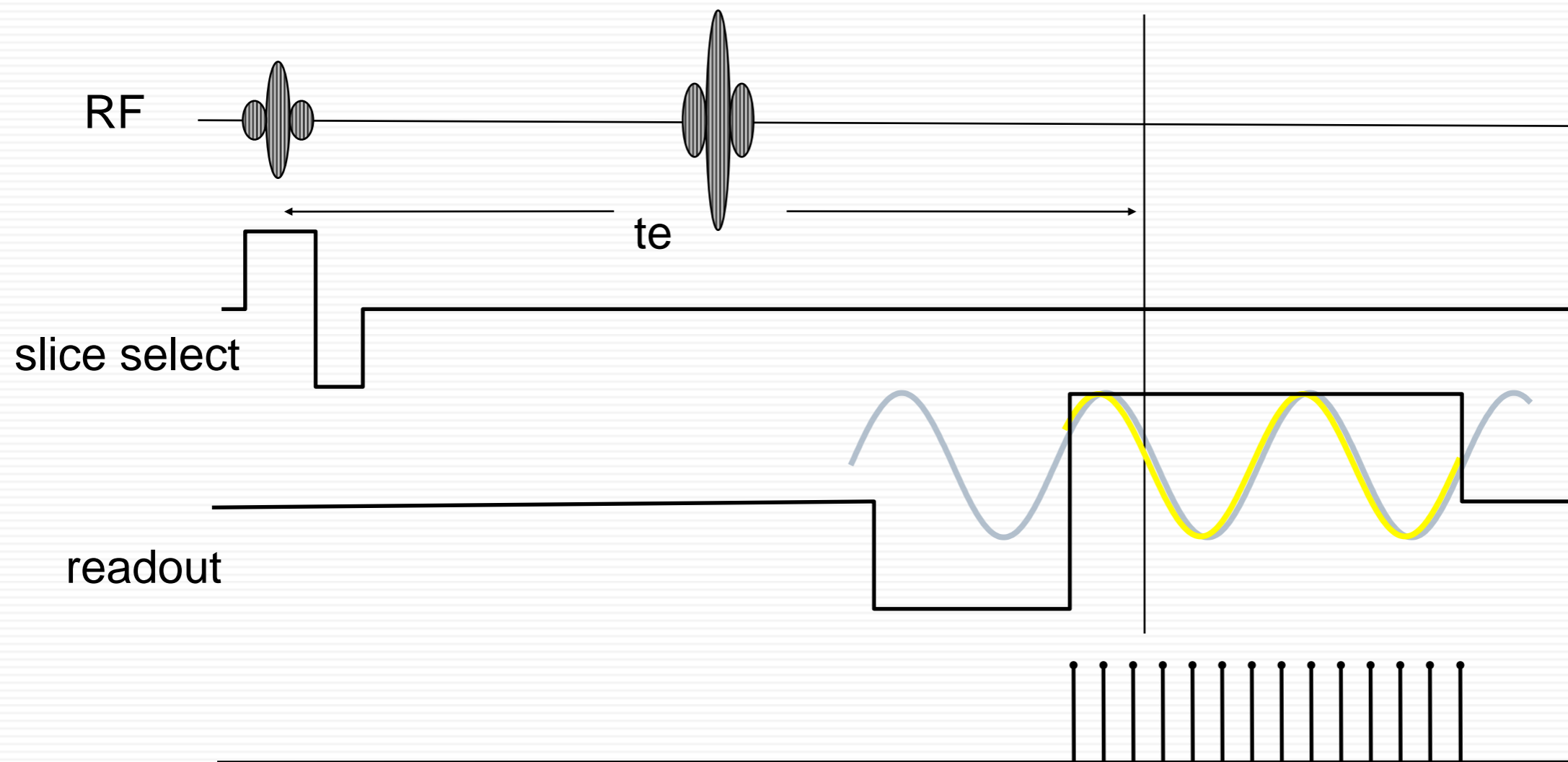
Phase Maps



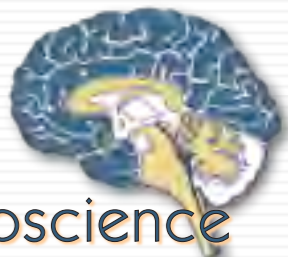
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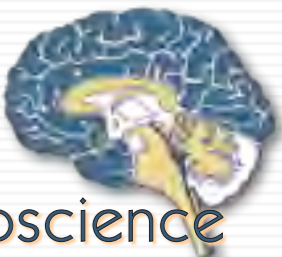
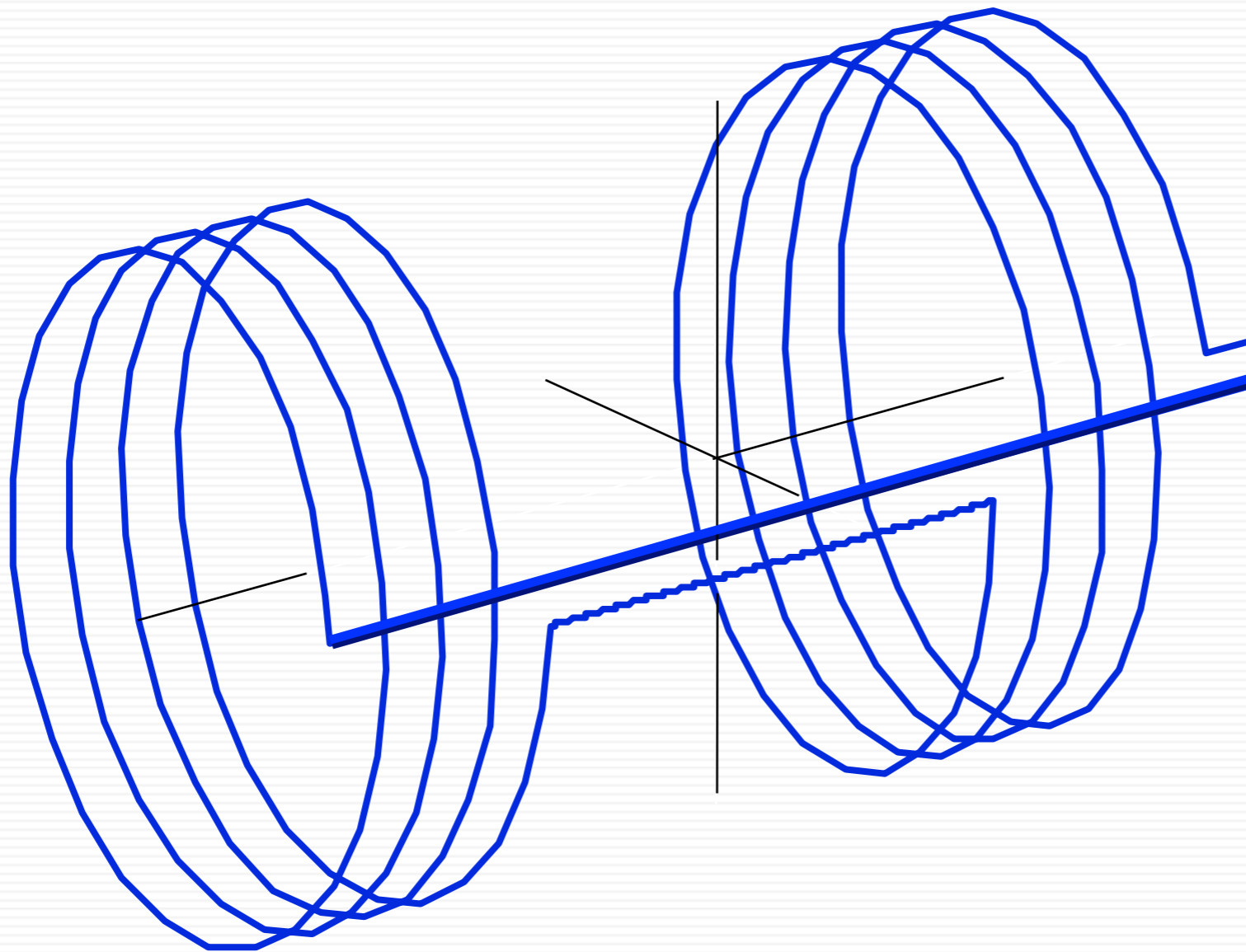
Phase Maps



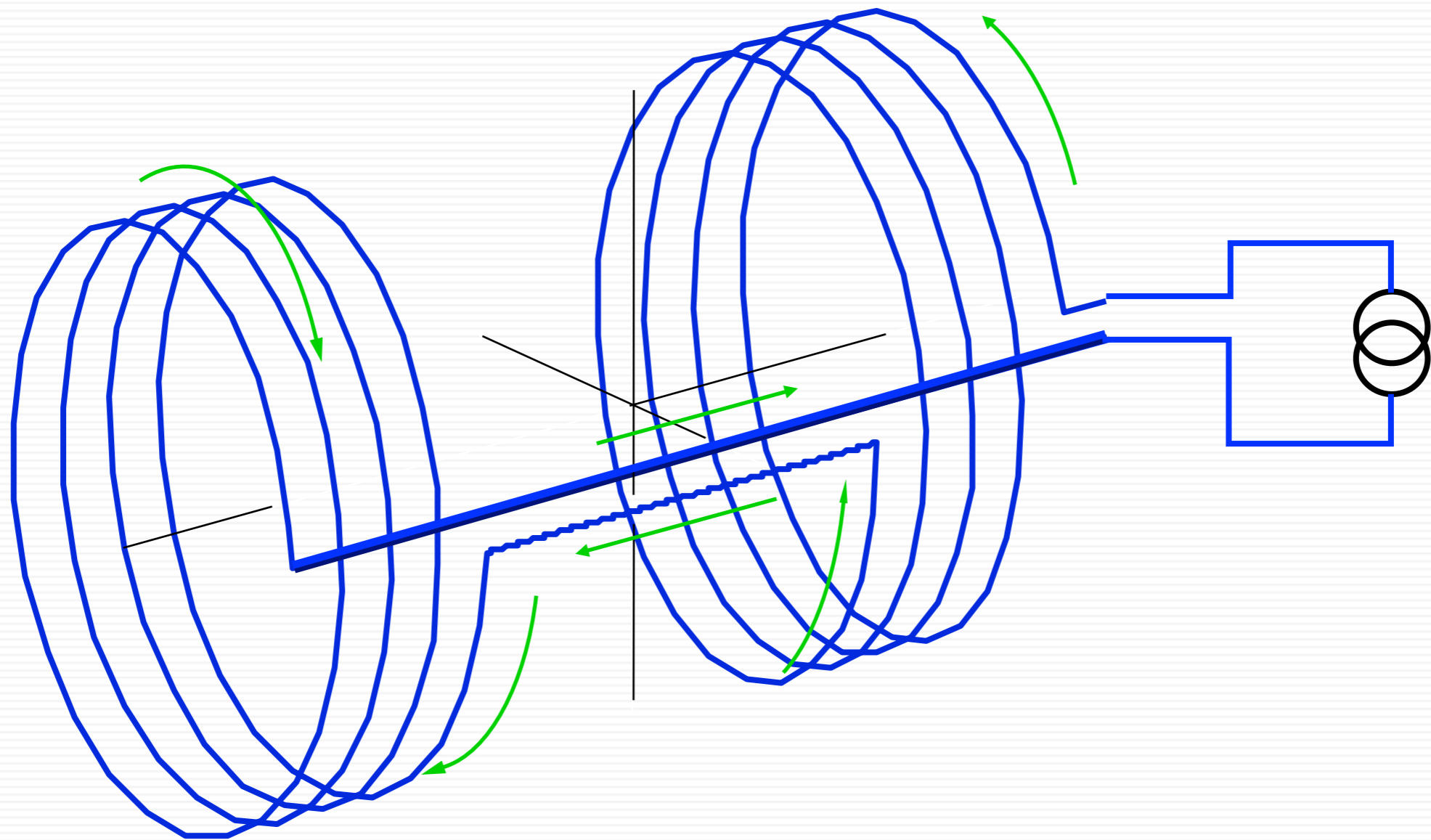
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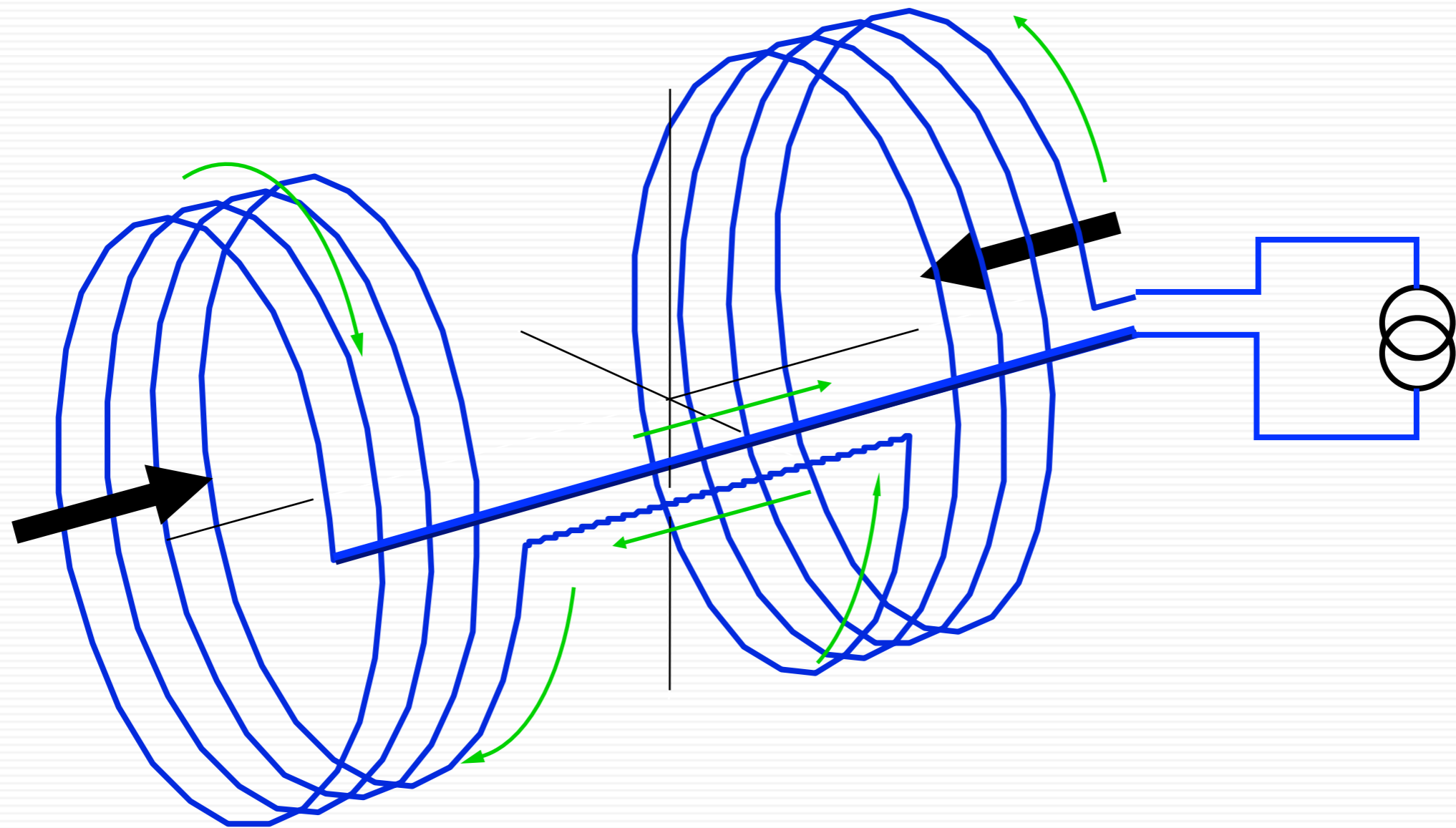
MR Field Gradient Coil



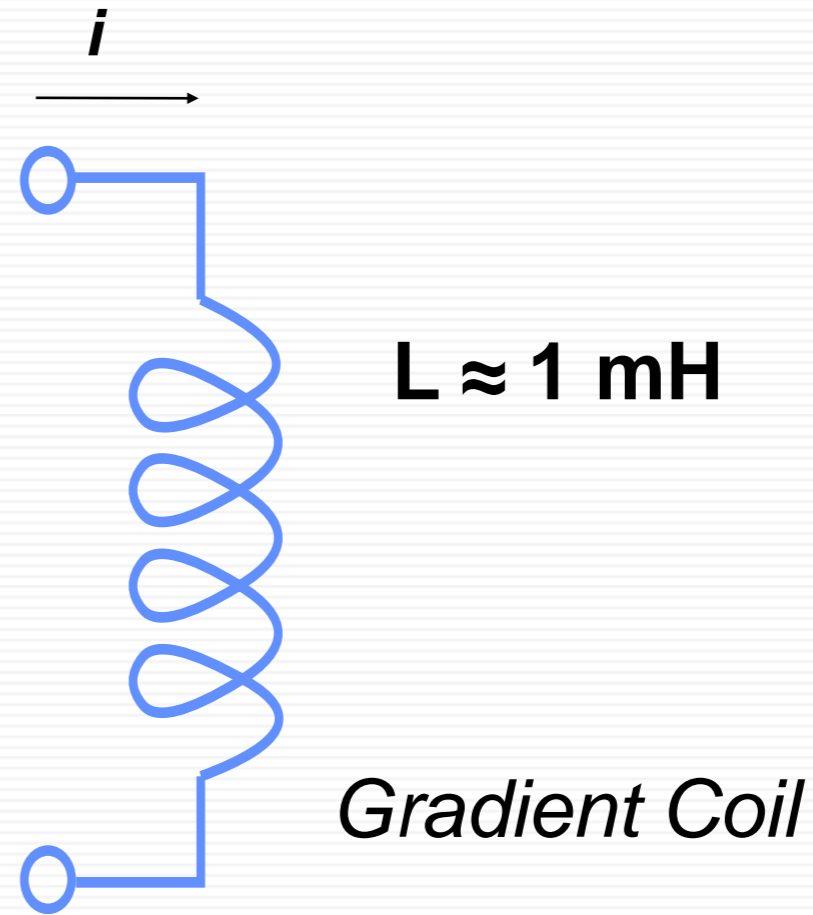
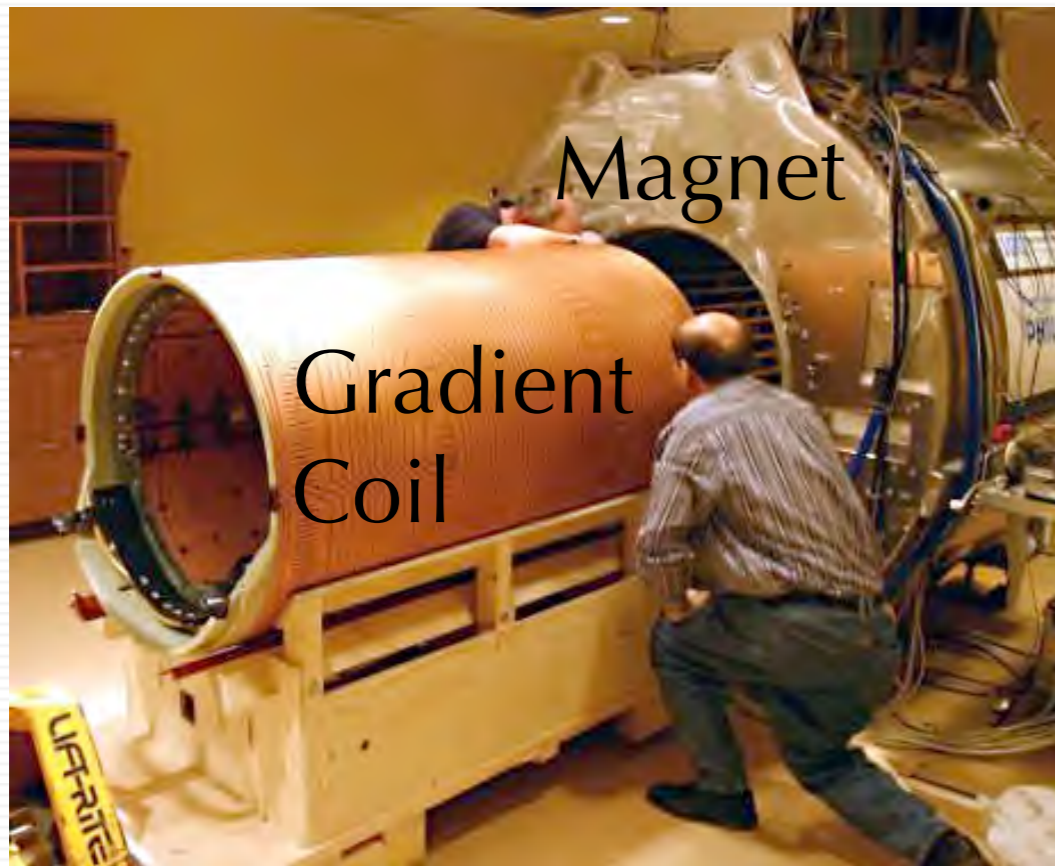
MR Field Gradient Coil



MR Field Gradient Coil

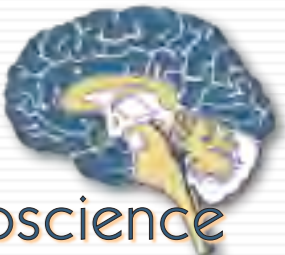


Gradient Coil Characteristics

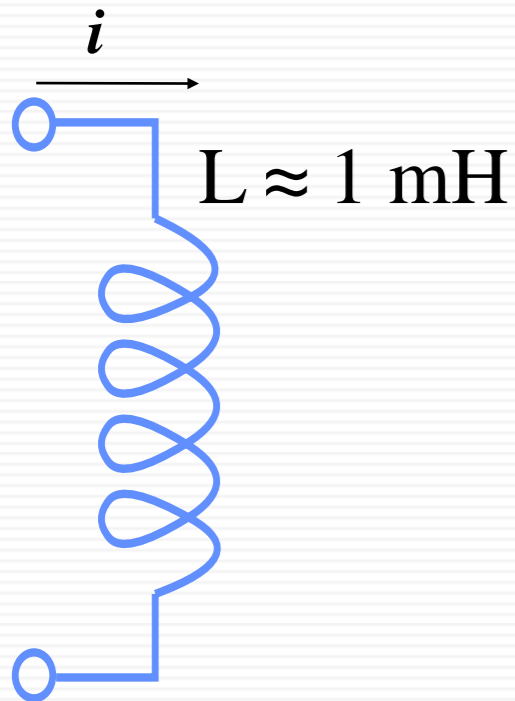


$$\text{Gradient Strength} = k i$$

$$k \approx 1 \text{ Gauss/cm} / 100 \text{ Amps}$$



Rise Time, Current and Voltage



$$\frac{di}{dt} = \frac{V_L}{1 \text{ mH}}$$

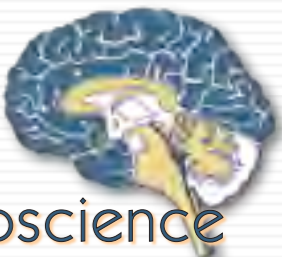


For: 250 Amps in 100 μsec
 $V_L = 2500 \text{ Volts}$

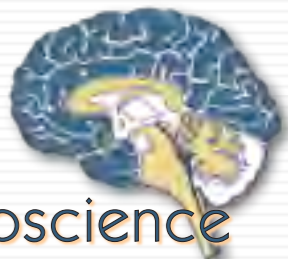
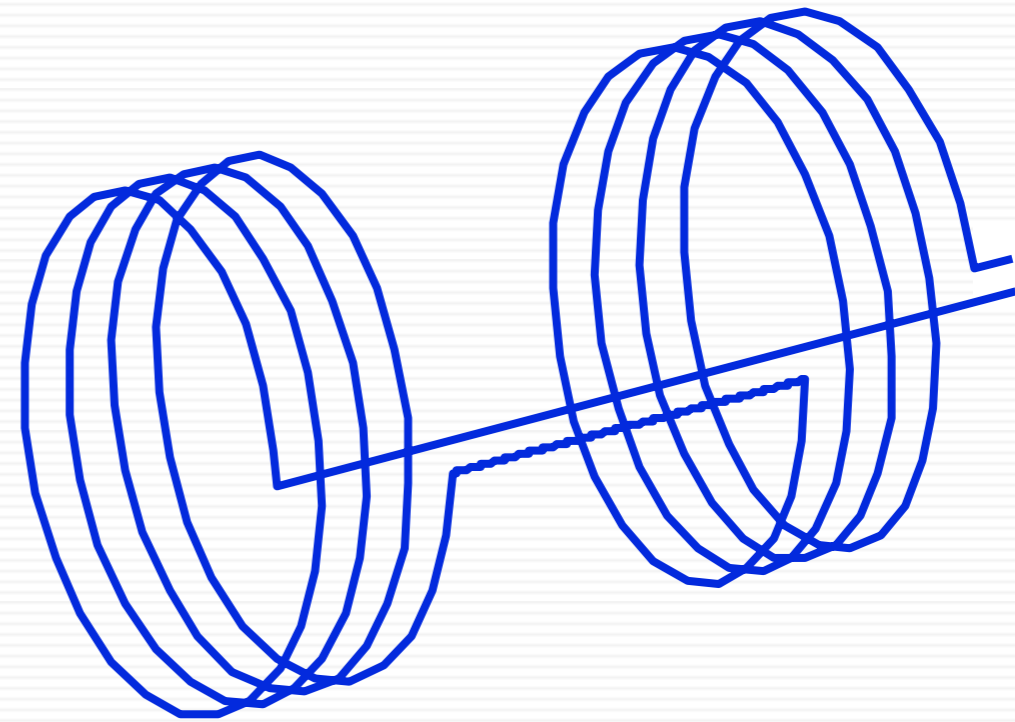
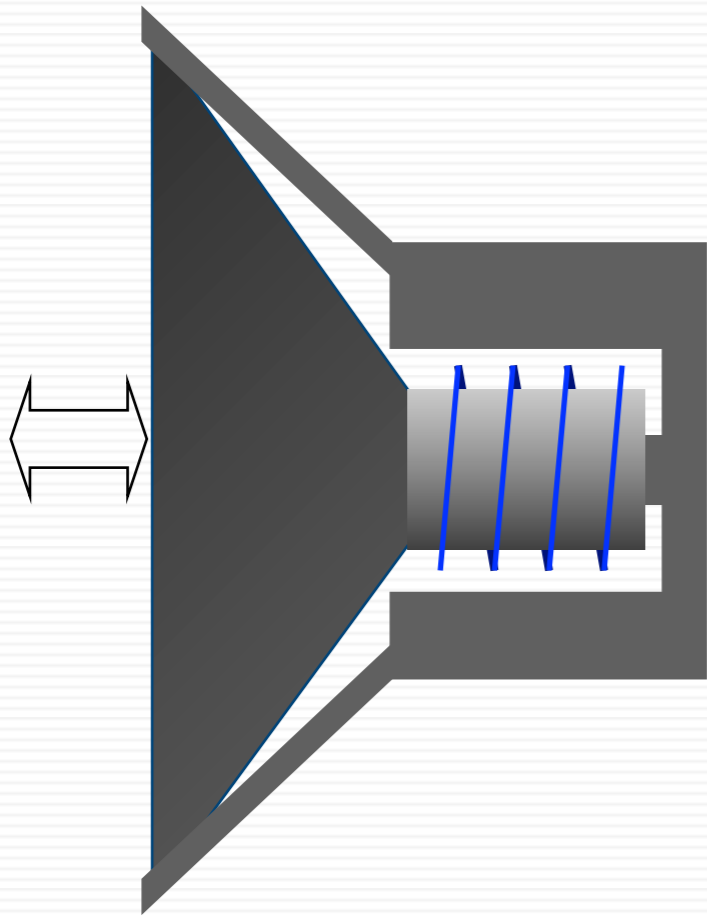
Power = 2500 Volts x 250 Amps
= $6.25 \times 10^5 \text{ Watts}$

Gradient Rise Time strongly affects:

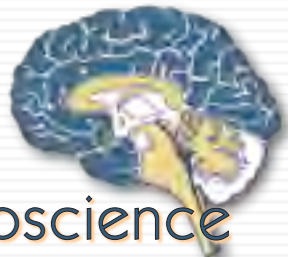
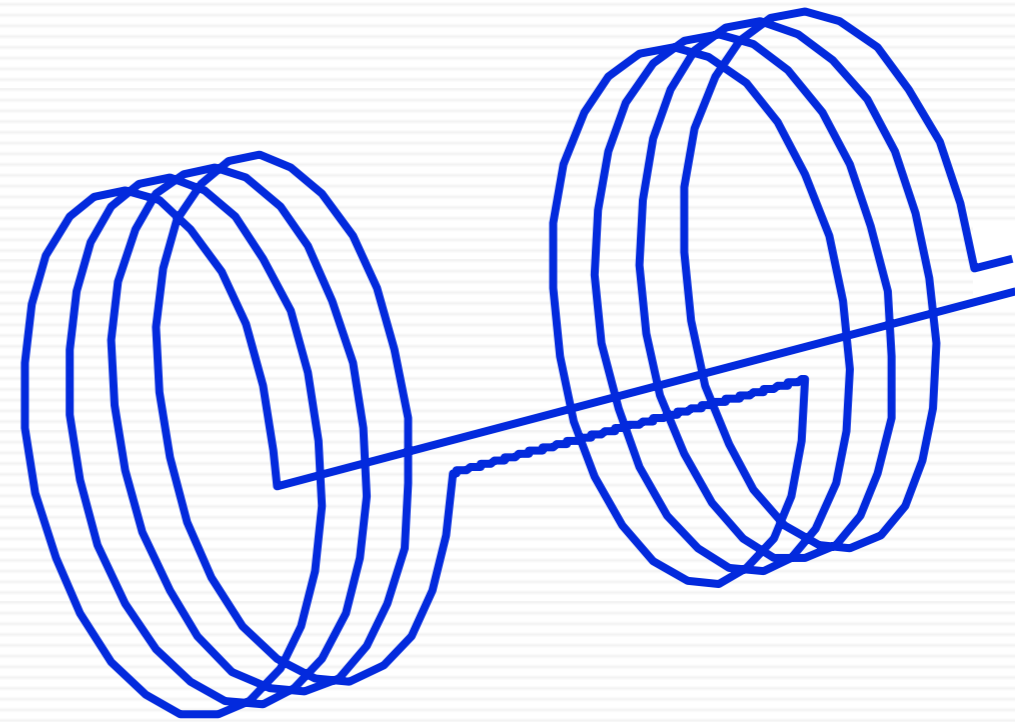
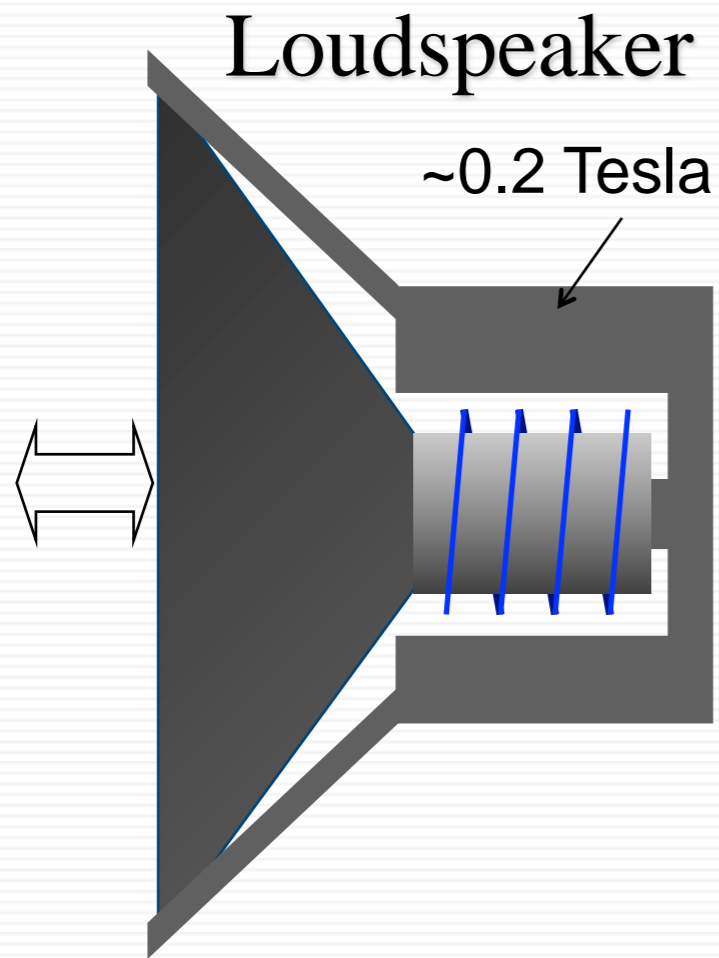
- ✓ Minimum TE
- ✓ Minimum Echo Spacing
- ✓ Echo Planar Bandwidth



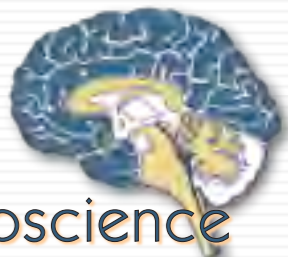
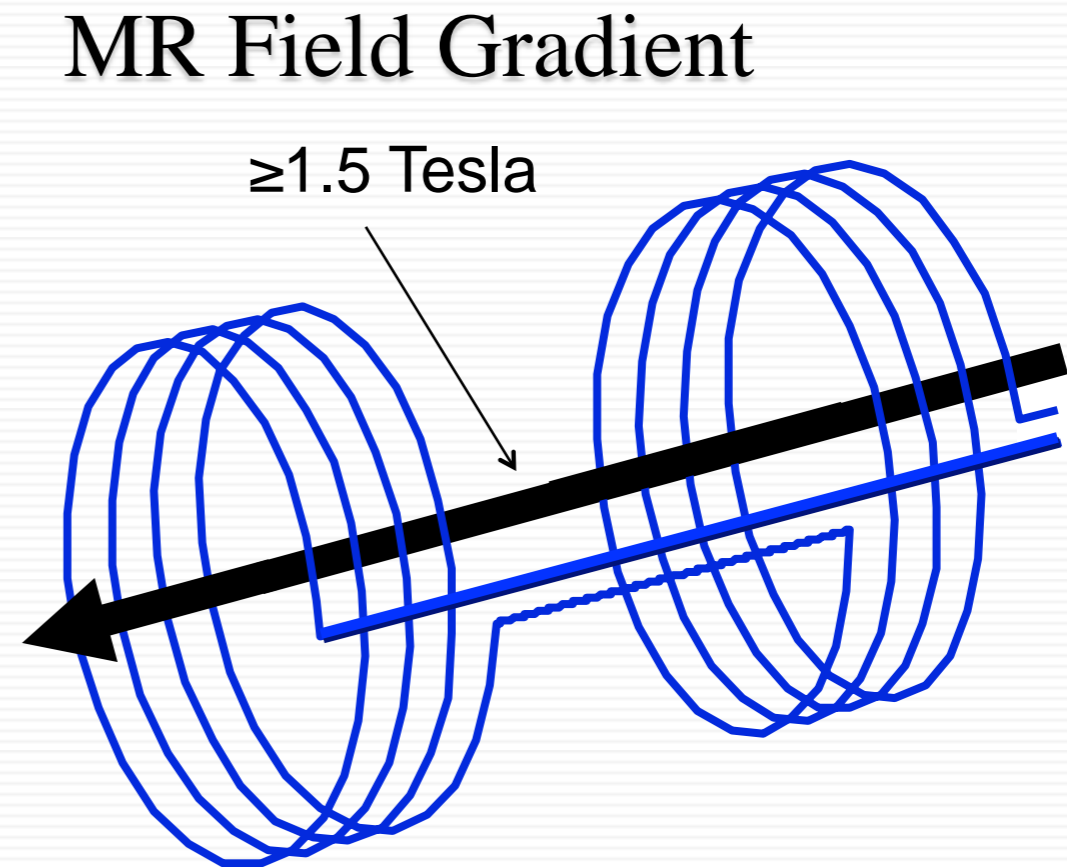
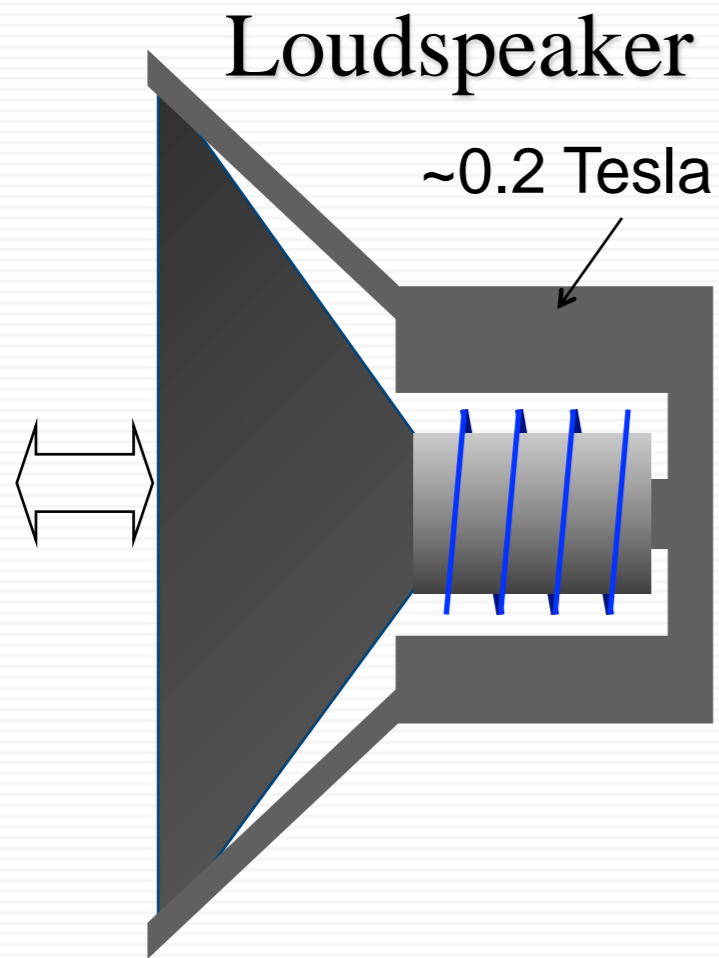
Why is MRI So Noisy?



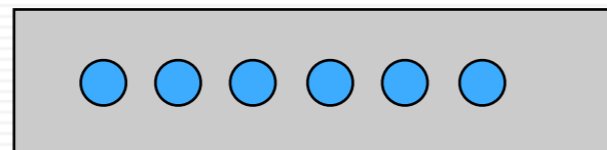
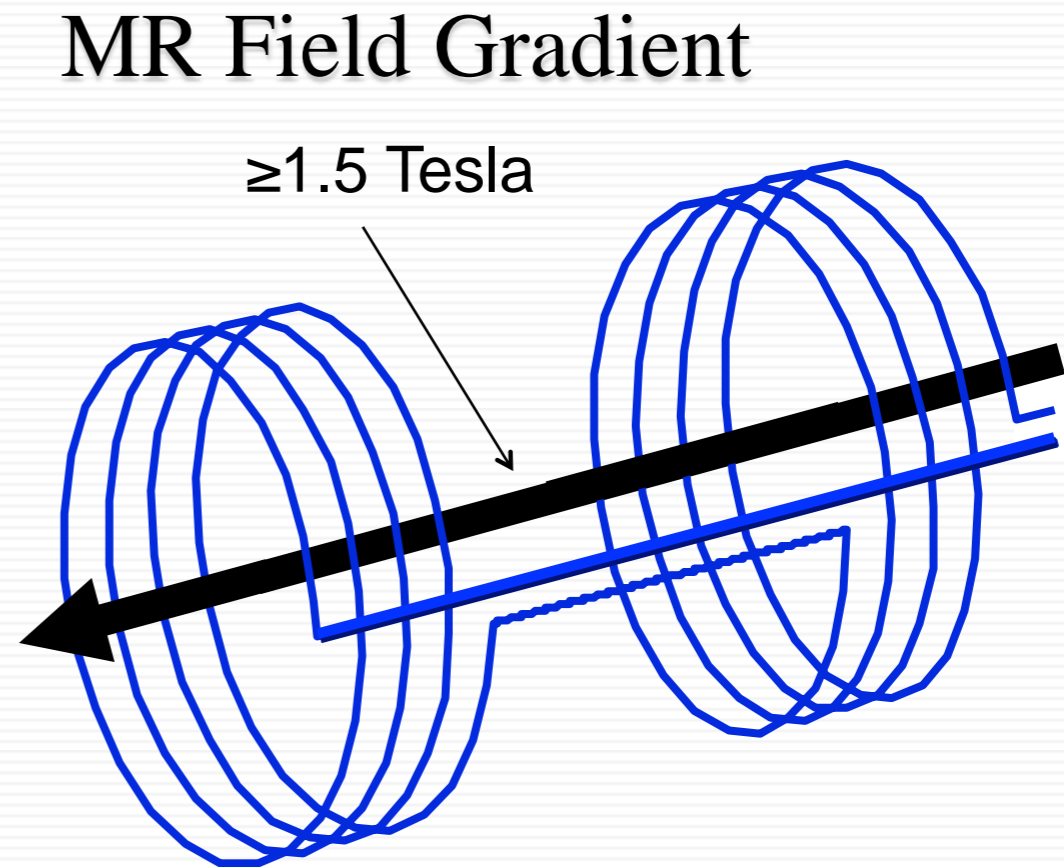
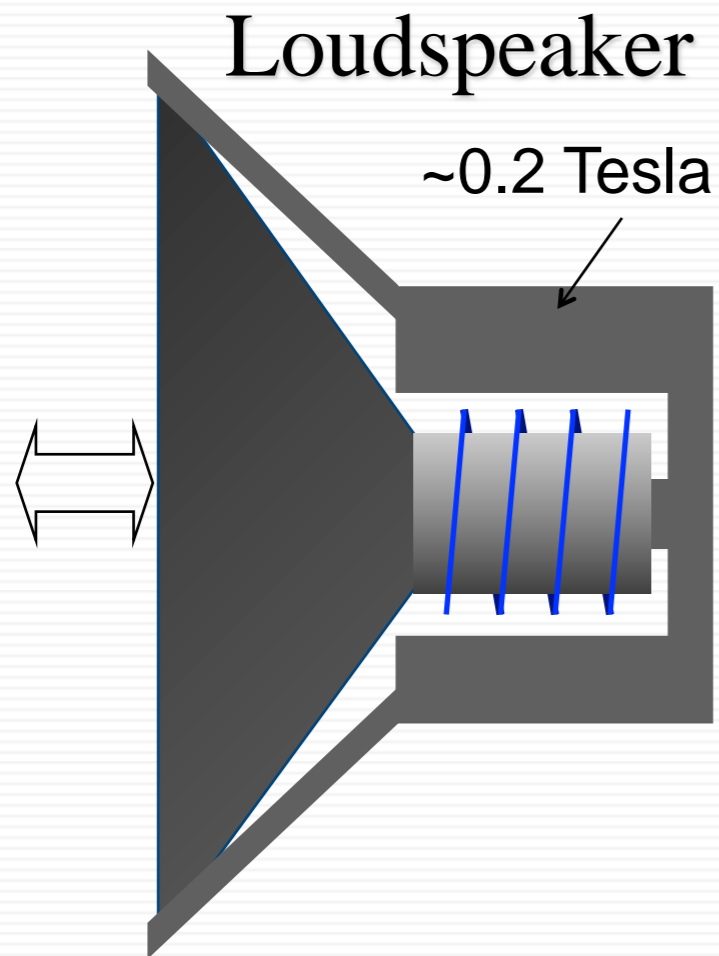
Why is MRI So Noisy?



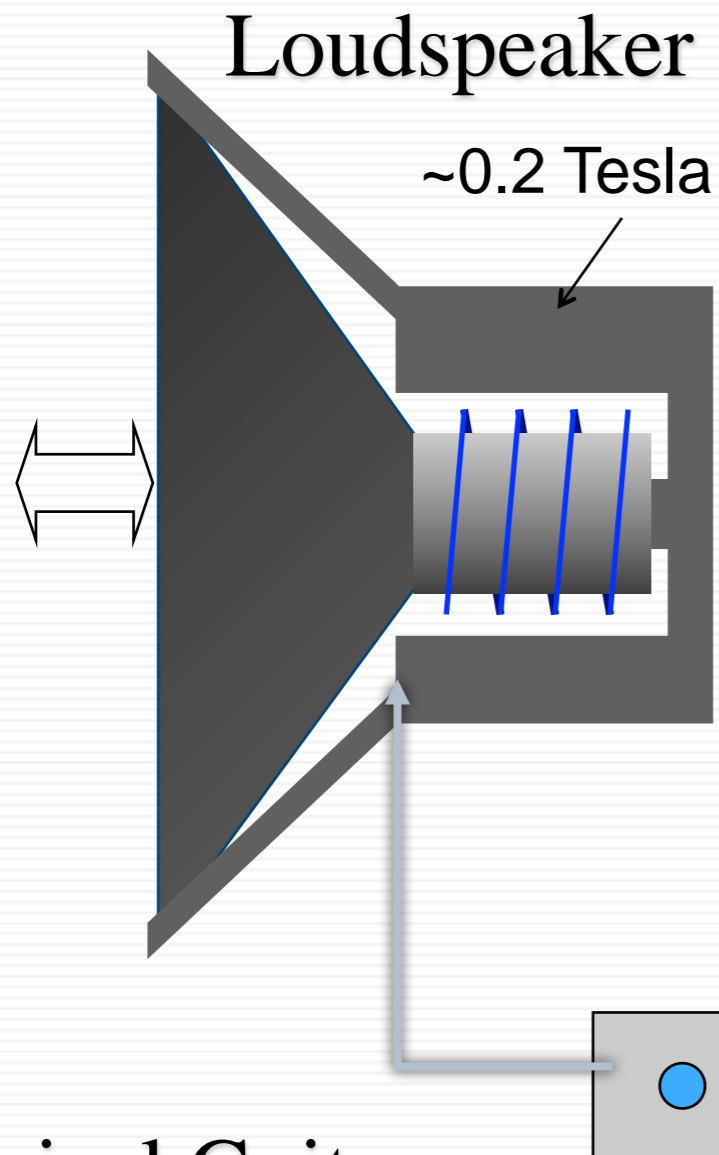
Why is MRI So Noisy?



Why is MRI So Noisy?

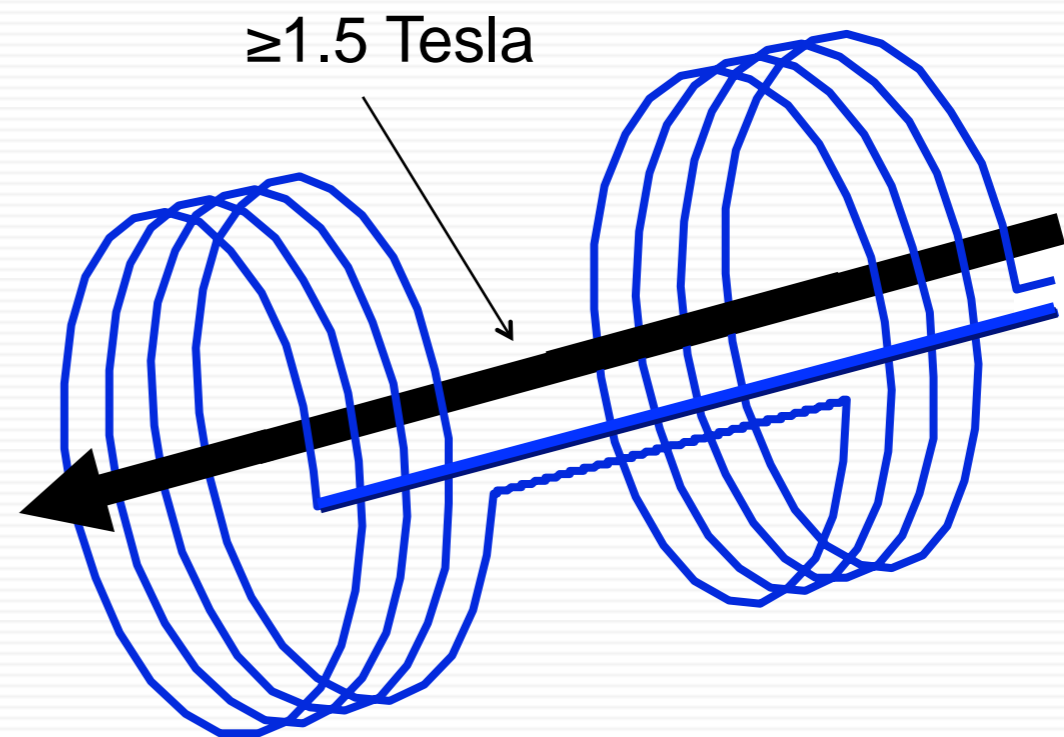


Why is MRI So Noisy?

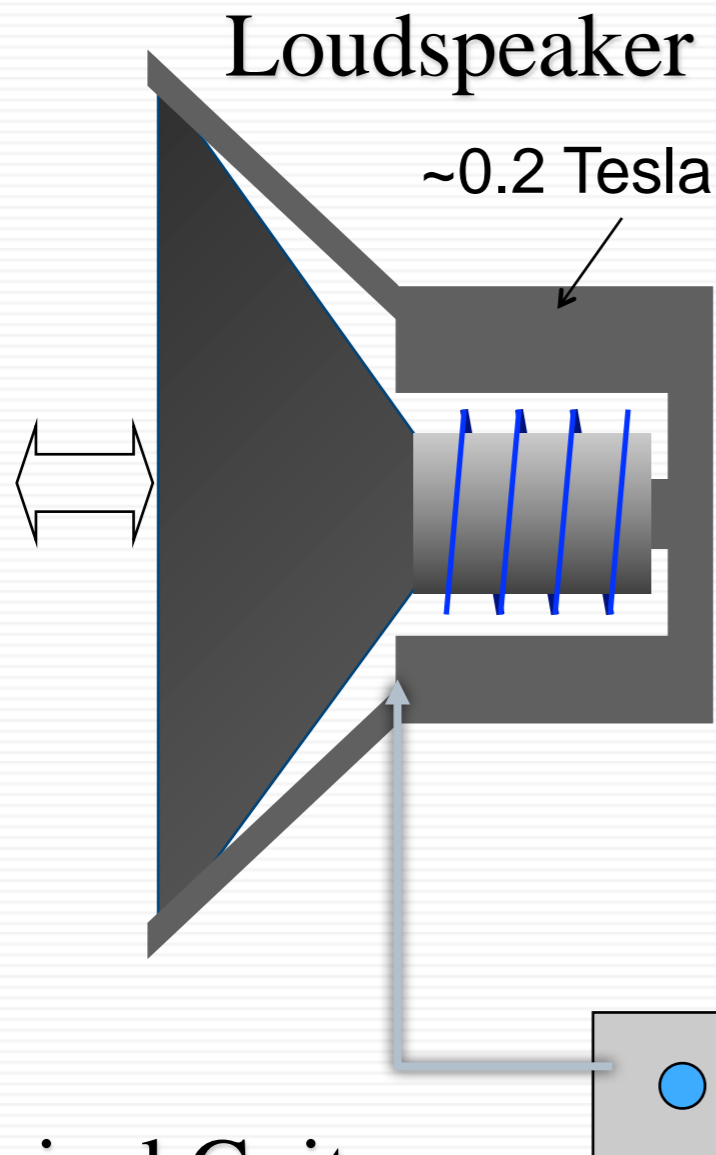


Typical Guitar
Amplifier: **100** Watts

MR Field Gradient



Why is MRI So Noisy?



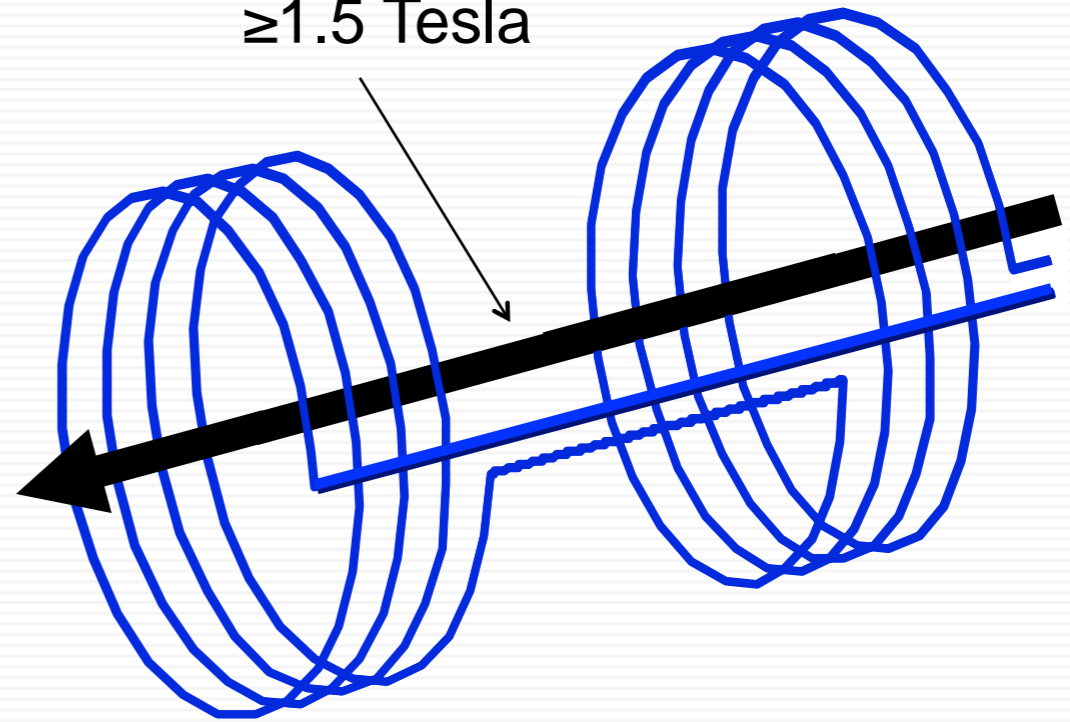
Loudspeaker

~0.2 Tesla

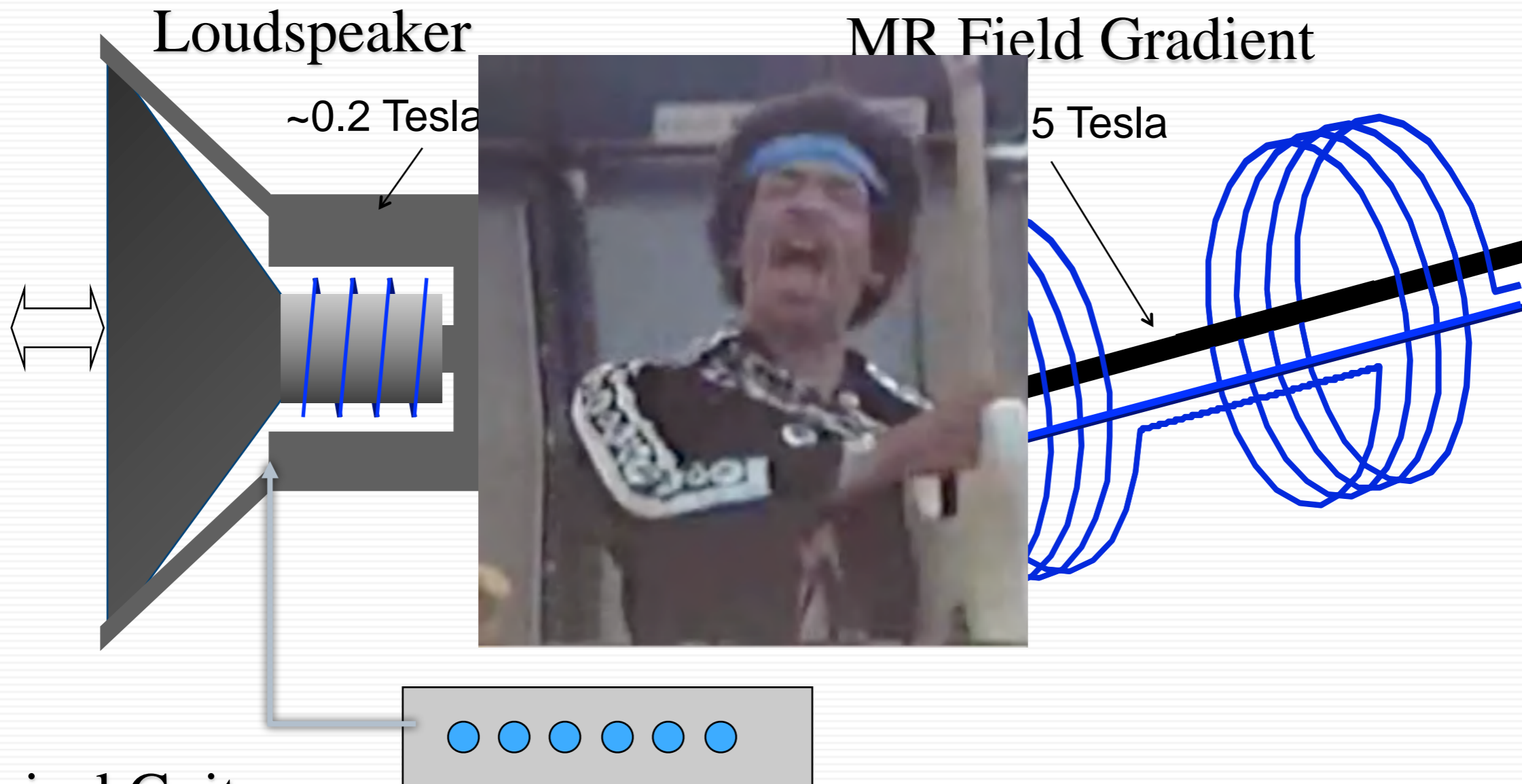
Typical Guitar
Amplifier: **100** Watts

MR Field Gradient

≥1.5 Tesla



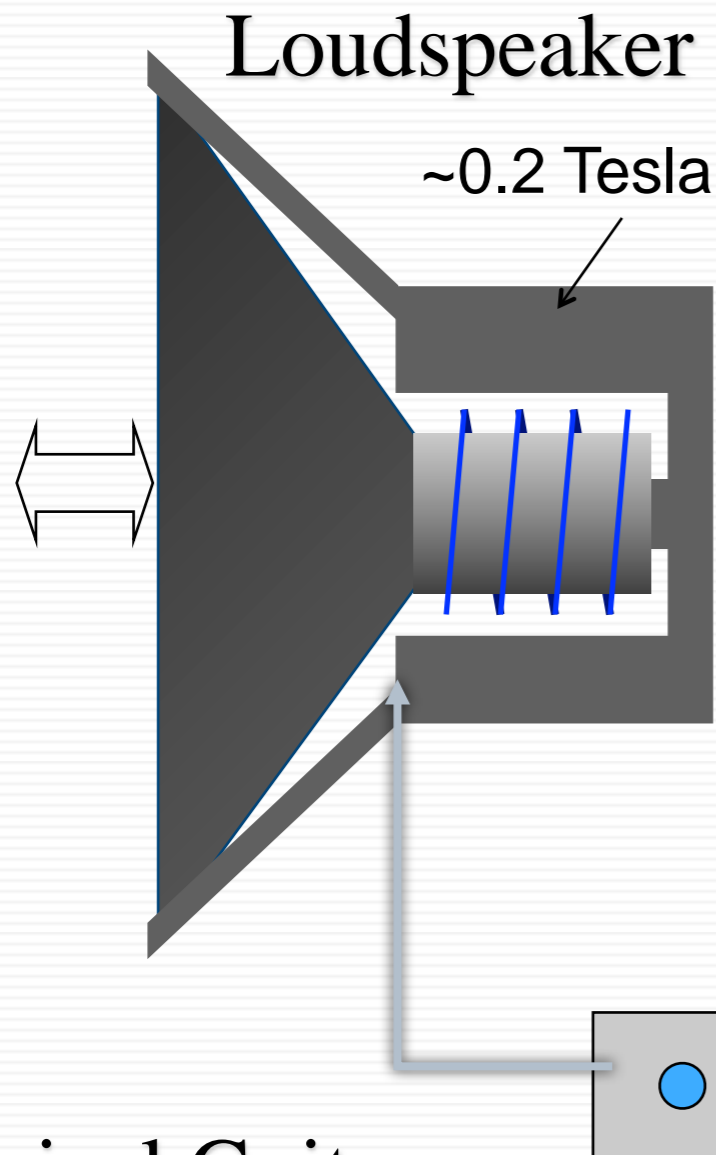
Why is MRI So Noisy?



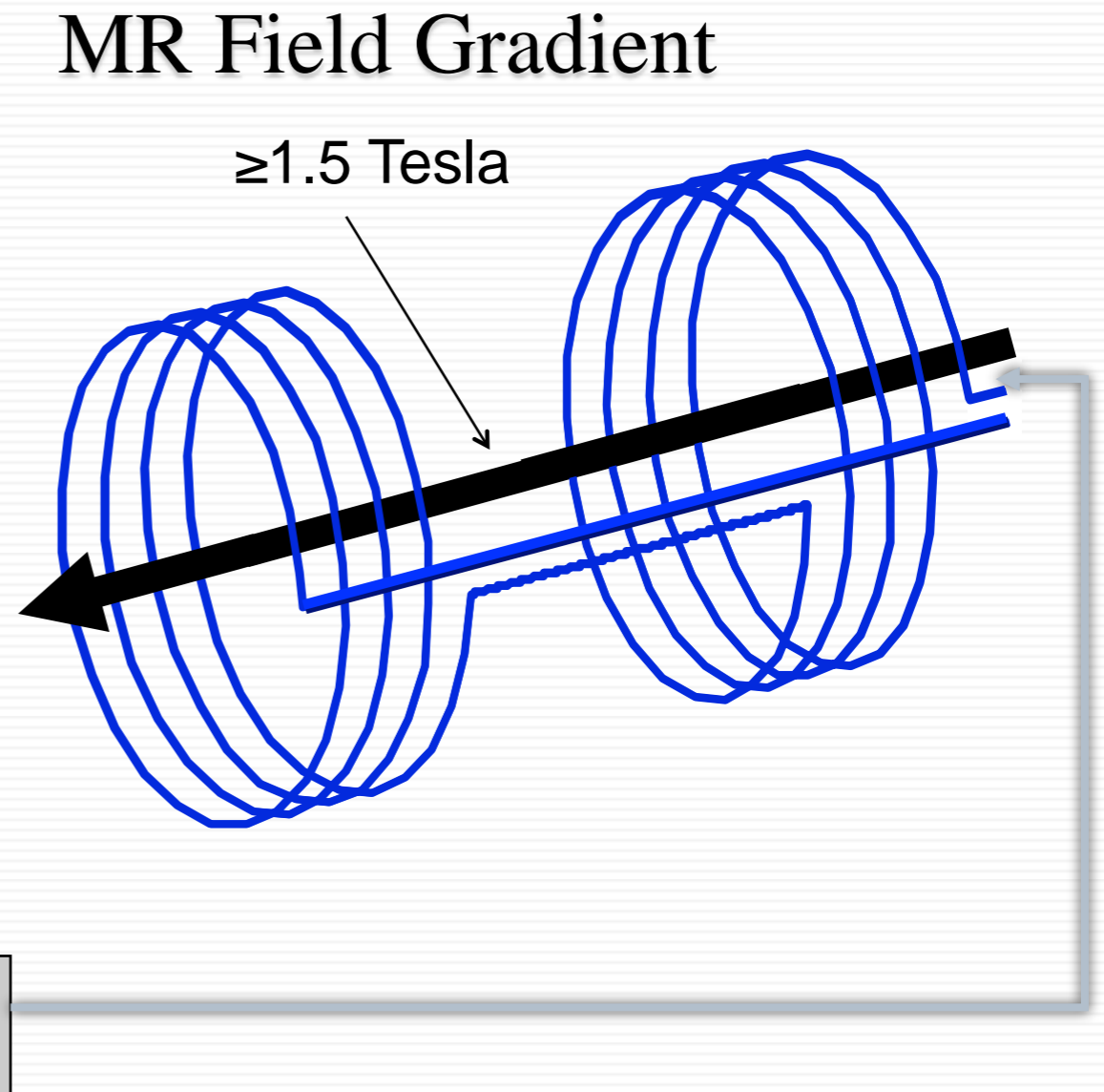
Typical Guitar
Amplifier: **100** Watts



Why is MRI So Noisy?



Typical Guitar
Amplifier: **100** Watts



Ultra-fast (echo-planar)
gradient Amplifier: **865,000**
Watts

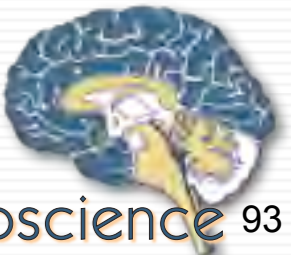
The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
- The “Pulse Sequence” Rules Everything (3)

Seventh Inning Stretch

- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)

- Image Quality and Artifacts (48)

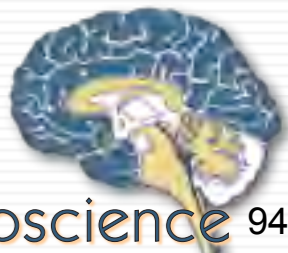


Brain "Activation" Leads to:

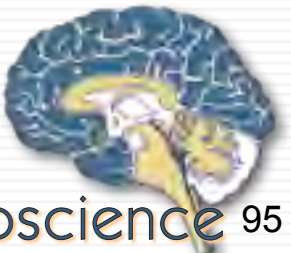
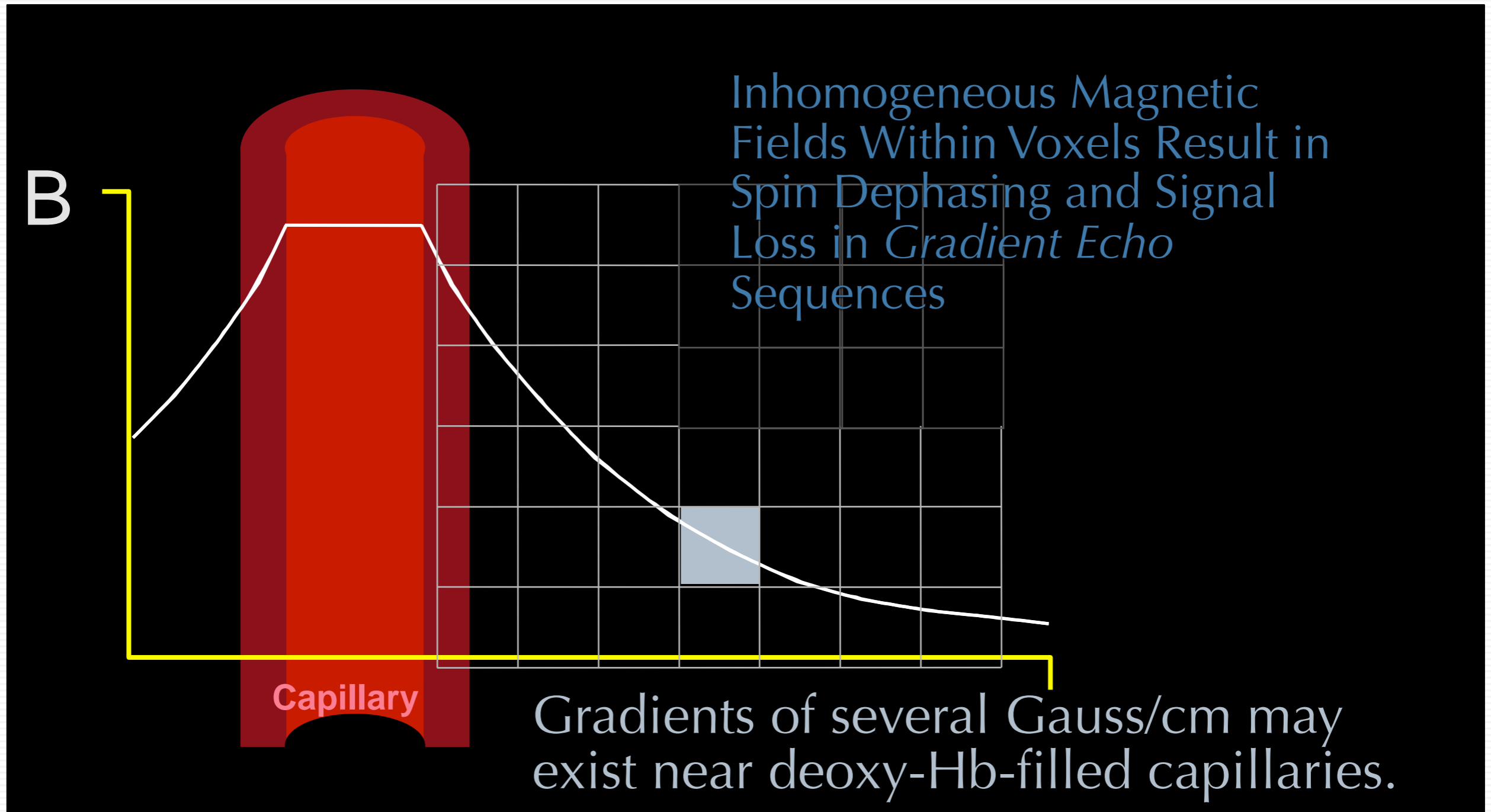
CBF	Increased	$+\Delta R1$	
CBV	Increased	$+\Delta R2$ (C+)	
O_2 Utilization	Increased slightly?		
Venous $[O_2]$	Increased	$-\Delta R2^*$	← "BOLD"
Glucose Utilization	Increased	? Lactate	

$$R1 = 1/T1$$

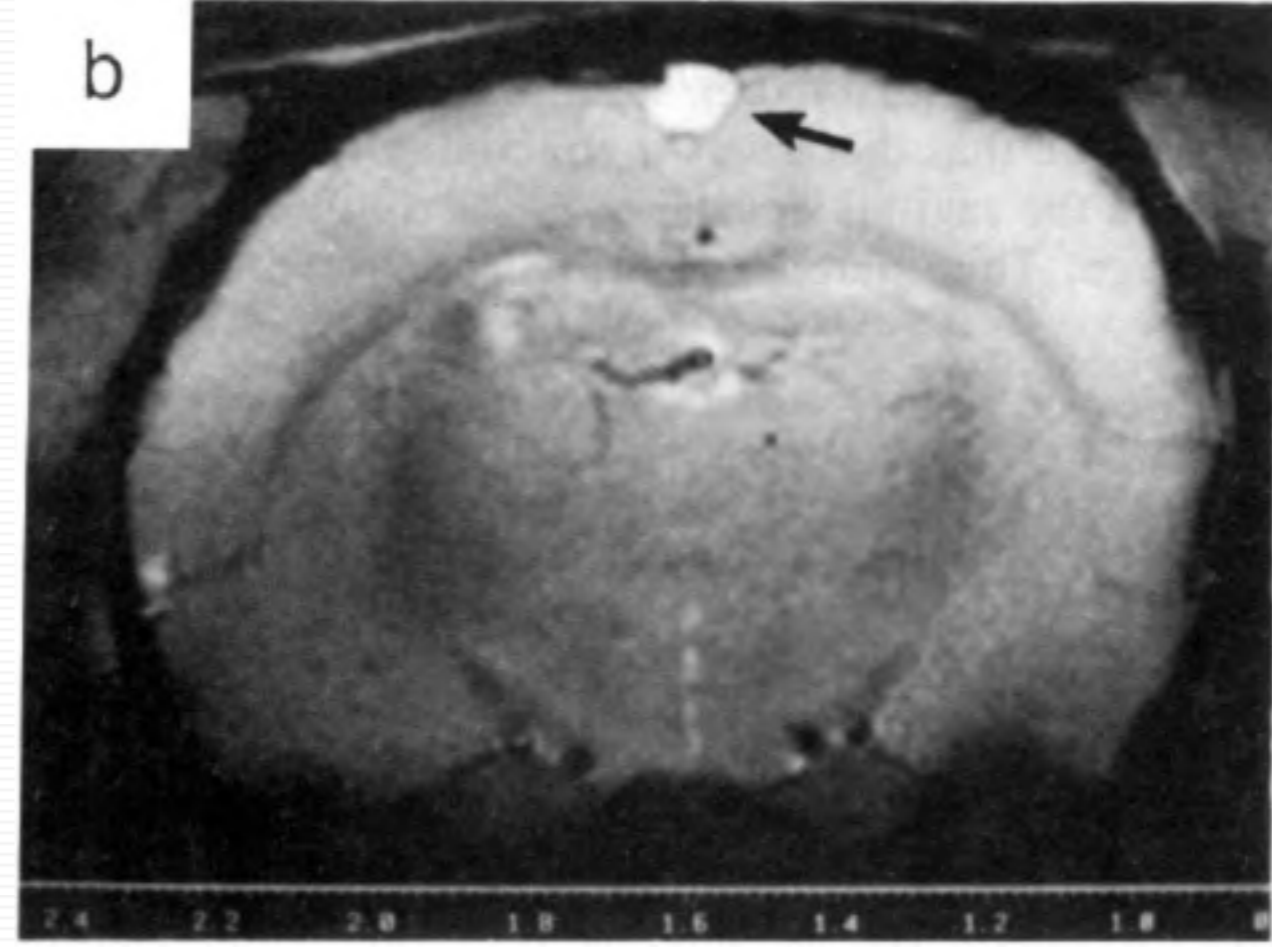
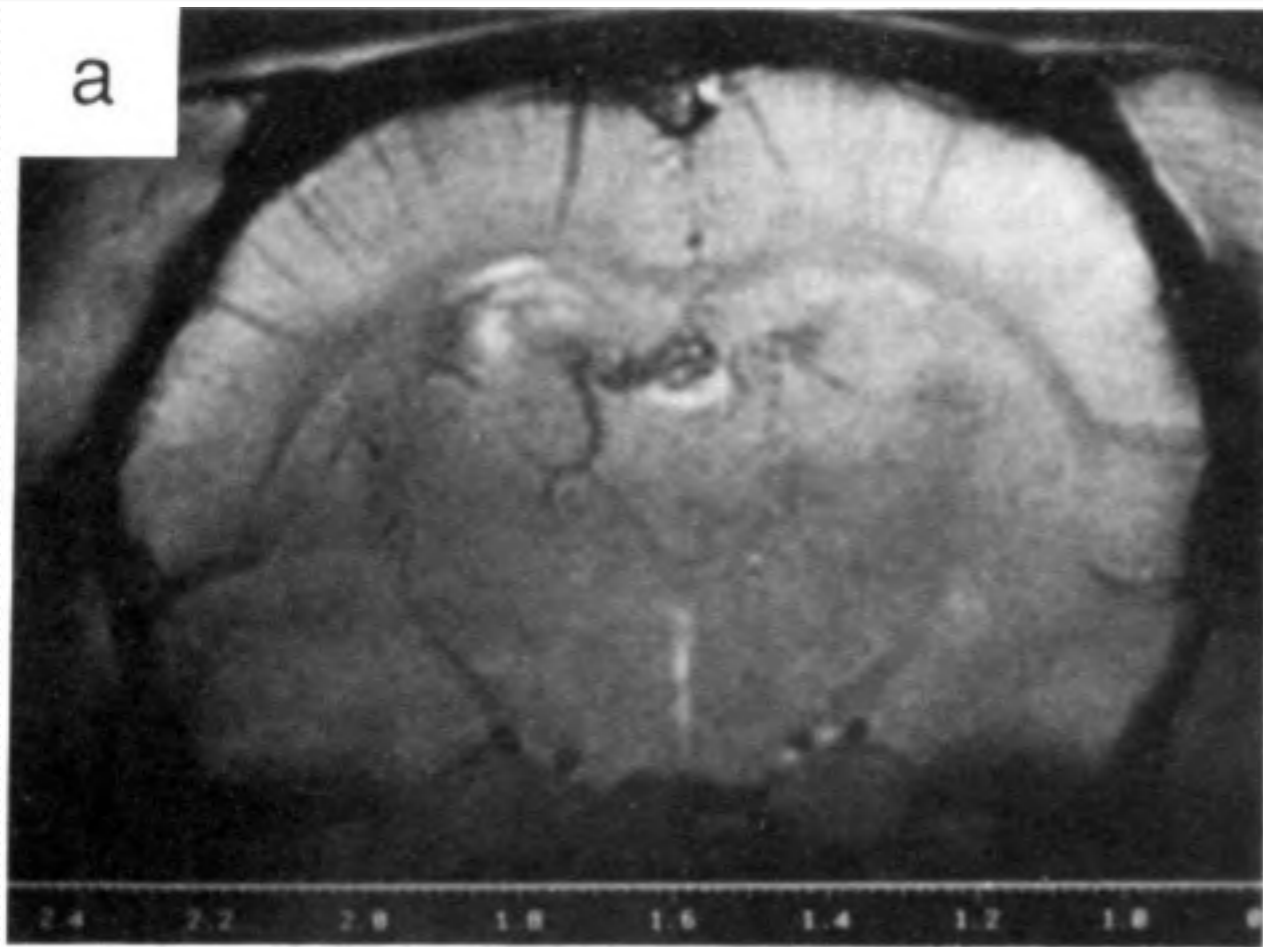
$$R2 = 1/T2$$



Signal Losses from Spin Dephasing



BOLD

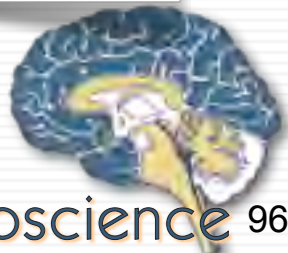


Effect of blood CO₂ level on BOLD contrast.

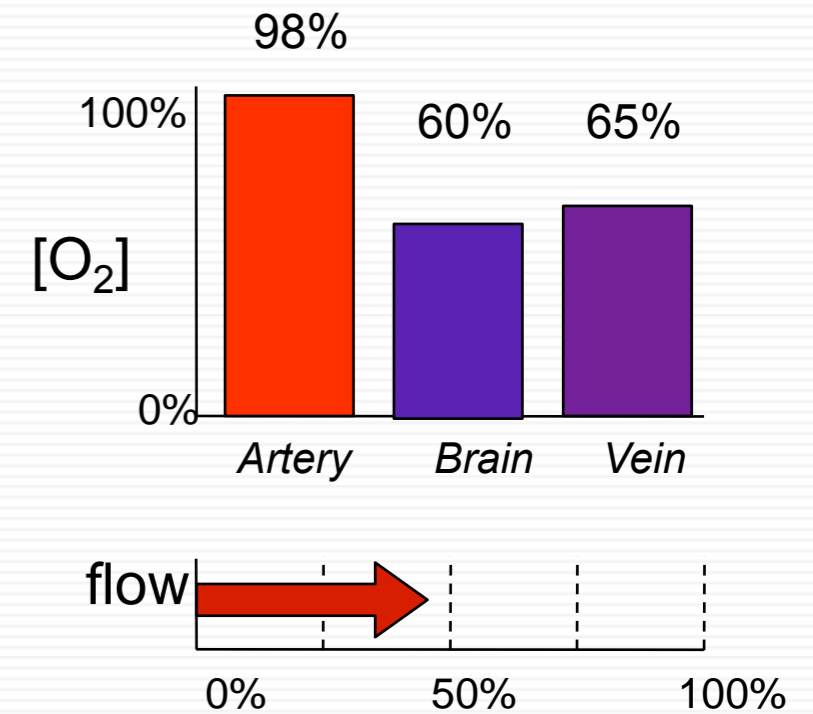
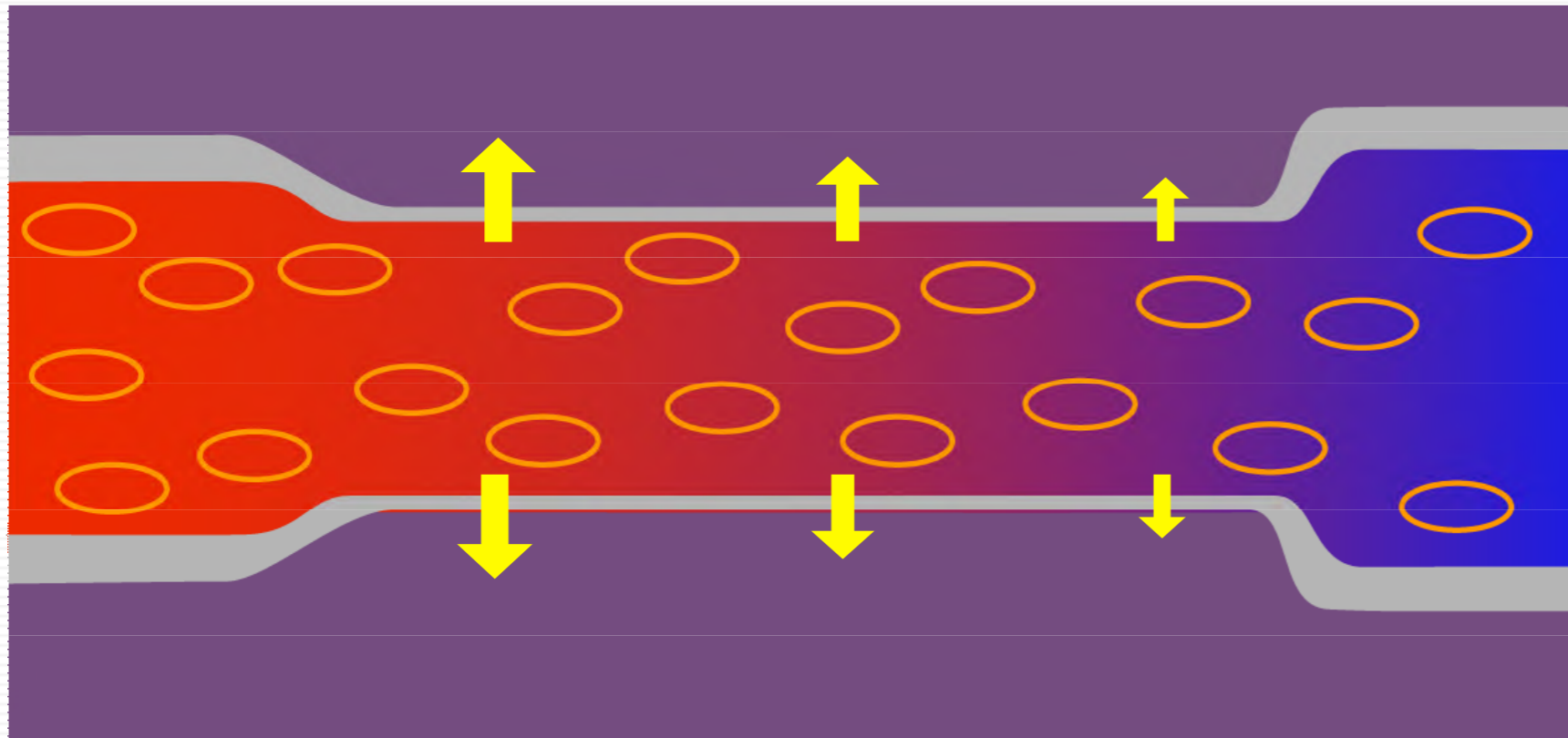
(a) Coronal slice brain image showing BOLD contrast from a rat anesthetized with urethane. The gas inspired was 100% O₂.

(b) The same brain but with 90% O₂/10%CO₂ as the gas inspired. BOLD contrast is greatly reduced.

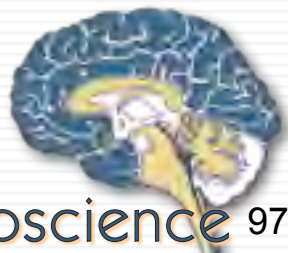
S Ogawa, *et al.*,
PNAS, **87**(24):9868,1990



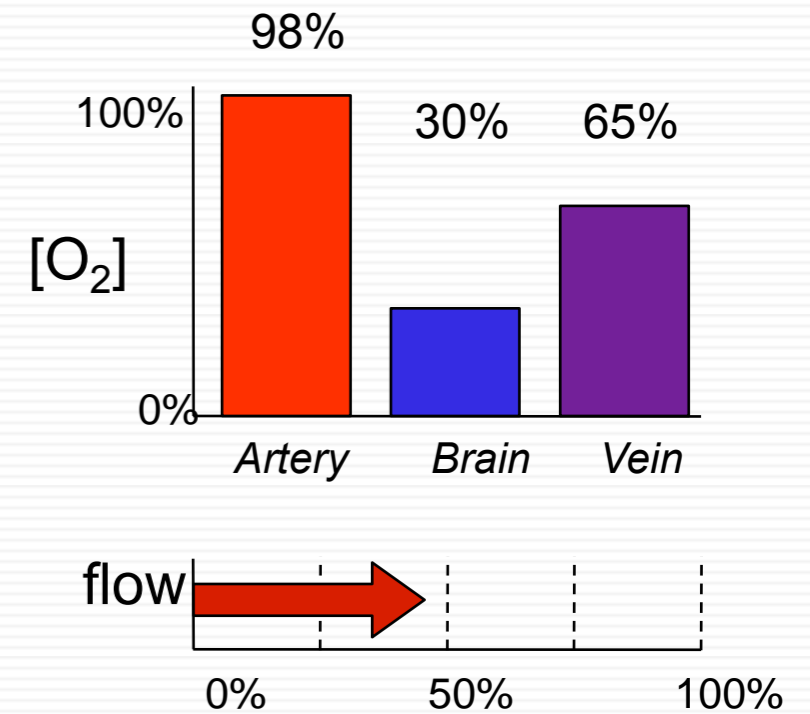
Why Does Venous O₂ Increase? ⁽¹⁾



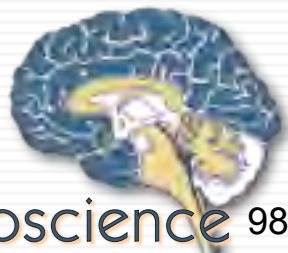
Under normal conditions oxygen diffuses down its concentration gradient from the capillary to the brain parenchyma



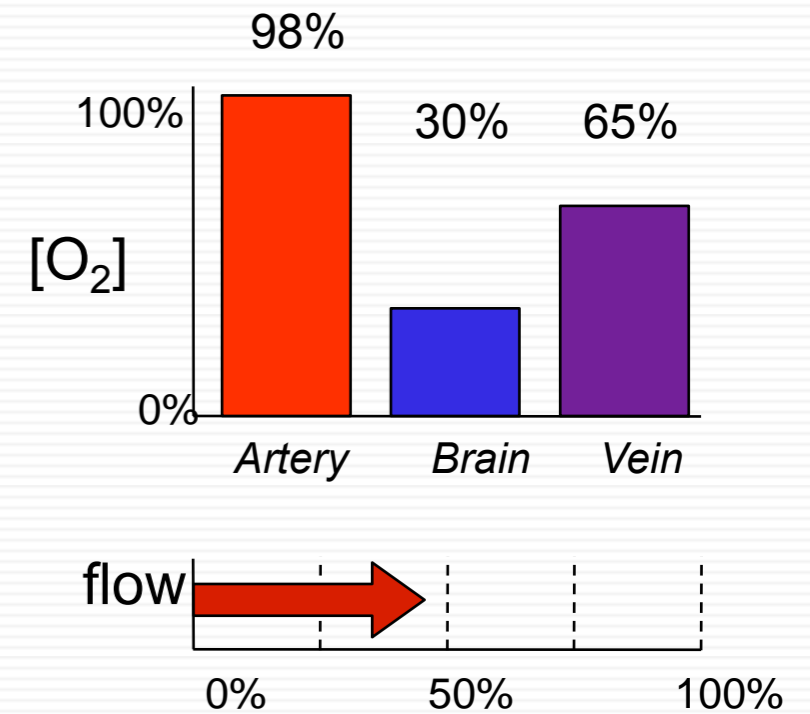
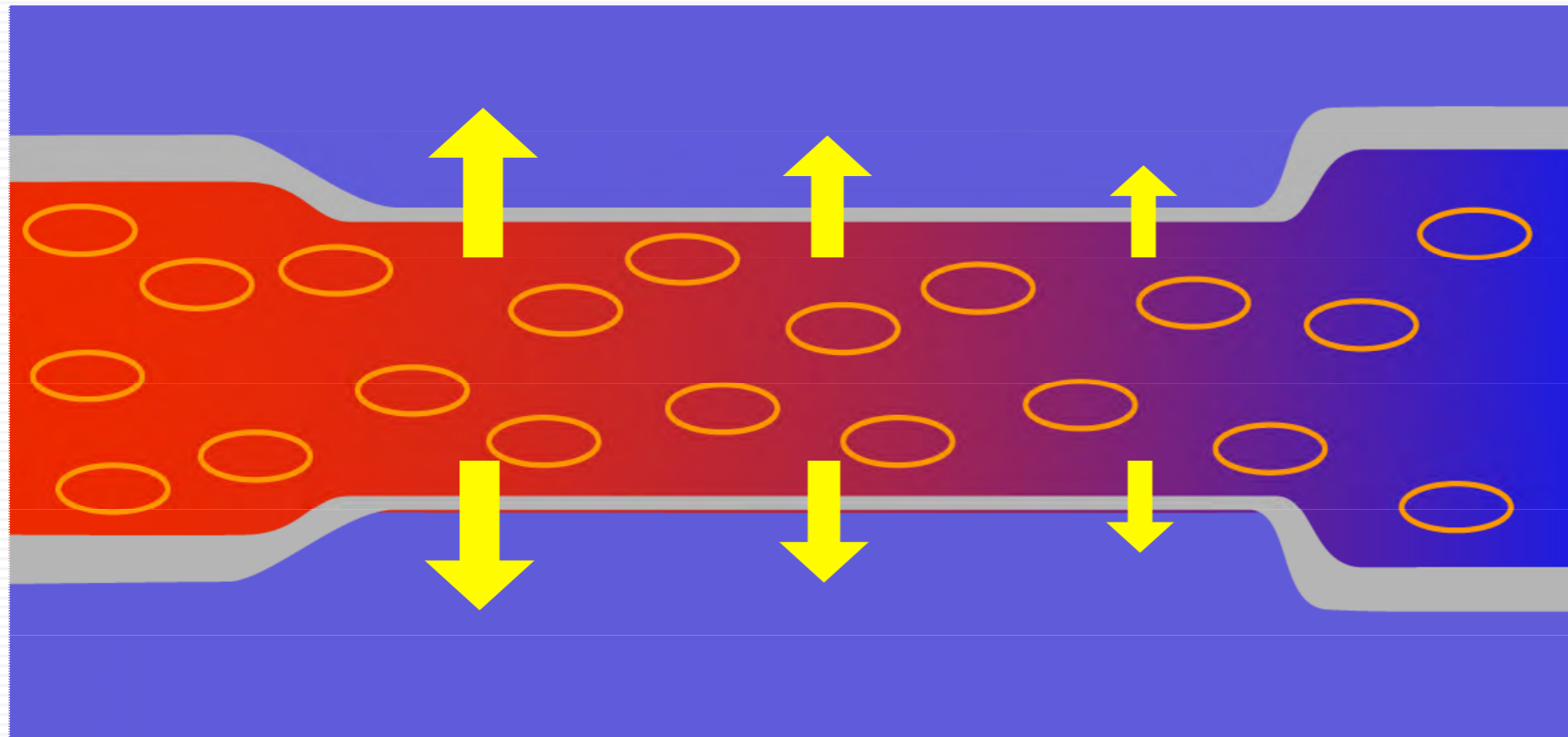
Why Does Venous O₂ Increase? ⁽²⁾



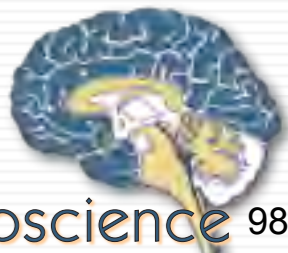
As the brain becomes more active, the oxygen consumption increases, increasing the transmural oxygen gradient.



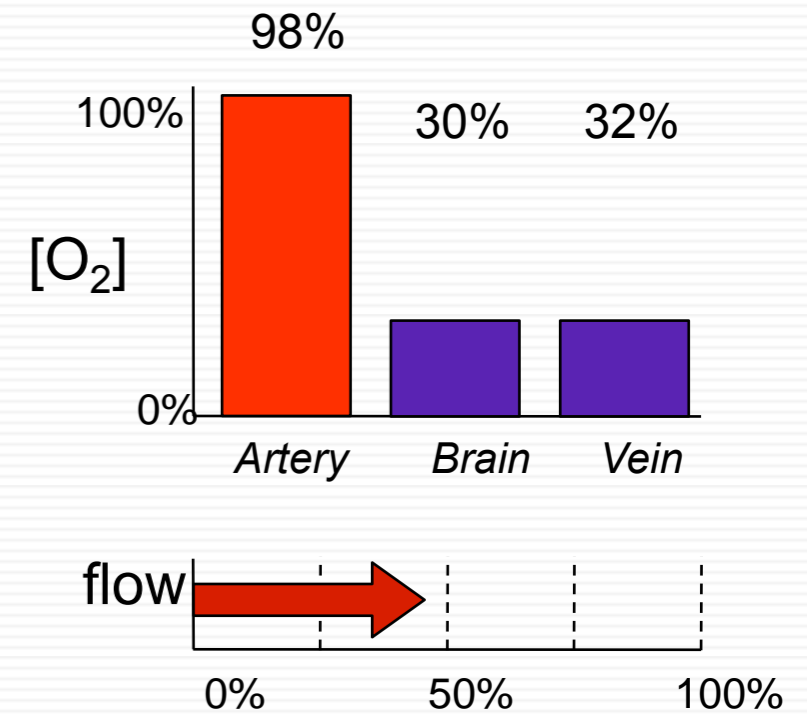
Why Does Venous O₂ Increase? ⁽²⁾



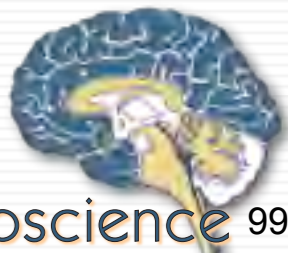
As the brain becomes more active, the oxygen consumption increases, increasing the transmural oxygen gradient.



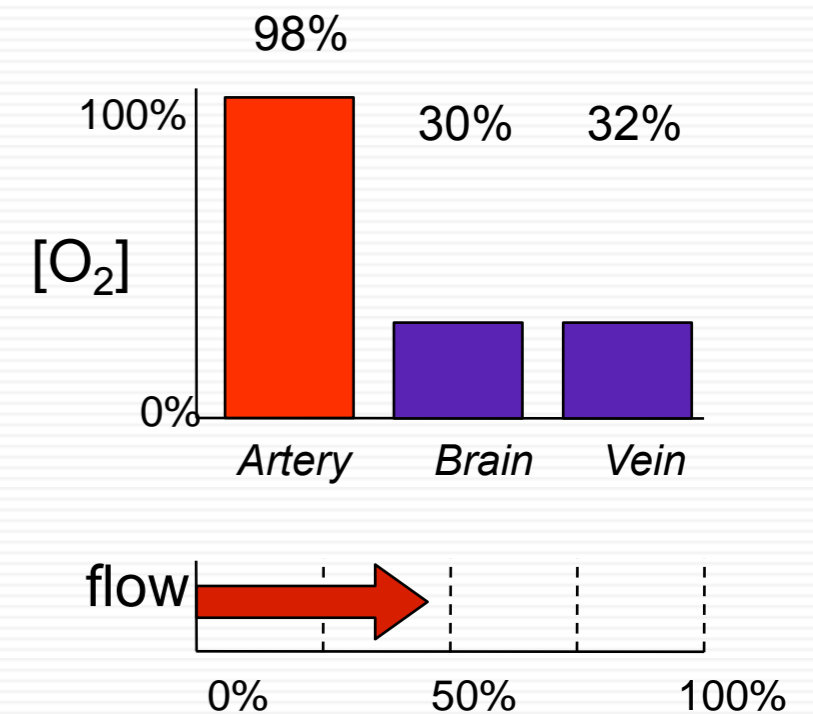
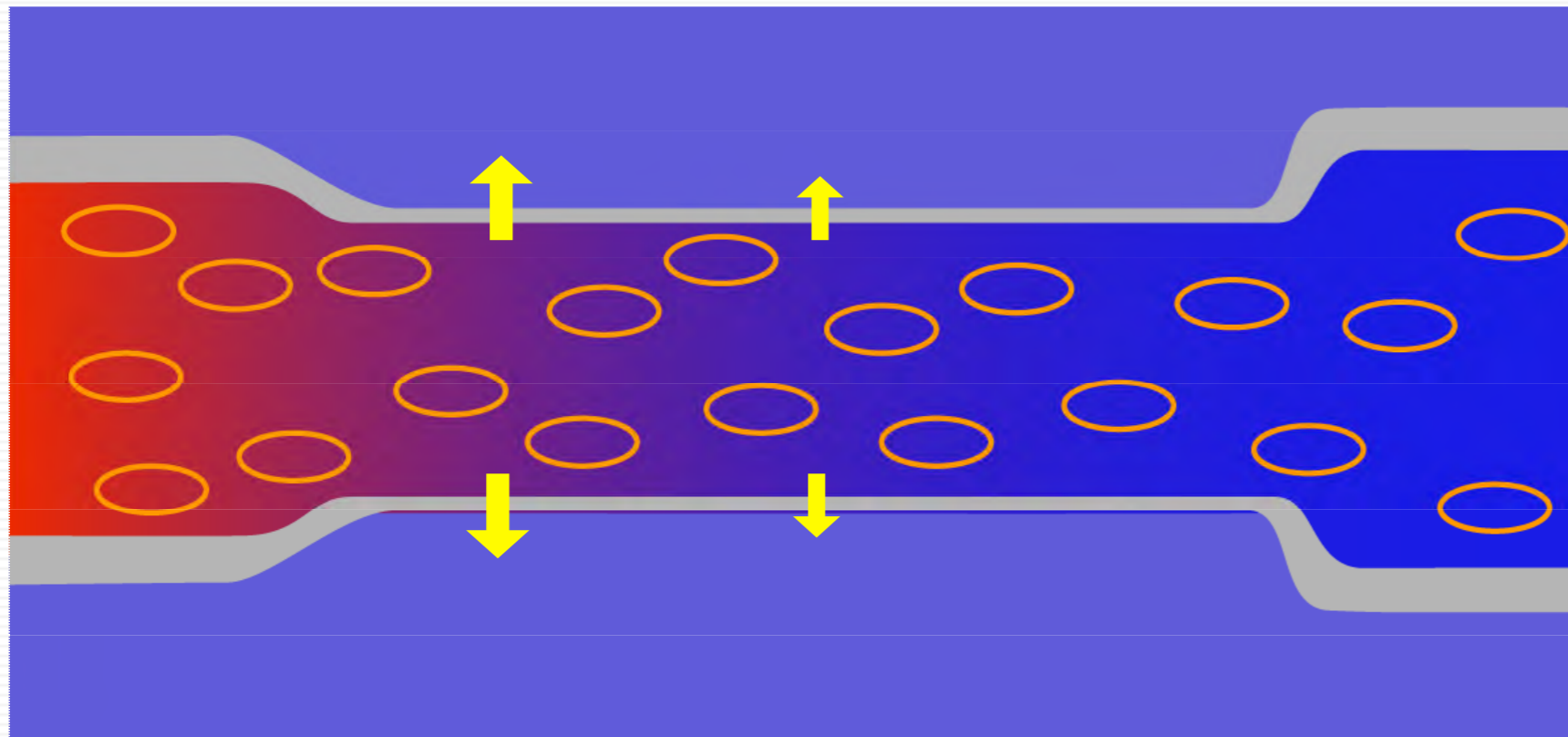
Why Does Venous O₂ Increase? ⁽³⁾



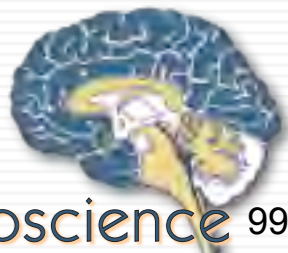
As oxygen flows across the capillary lumen it is depleted in the capillary and no further oxygen can be delivered



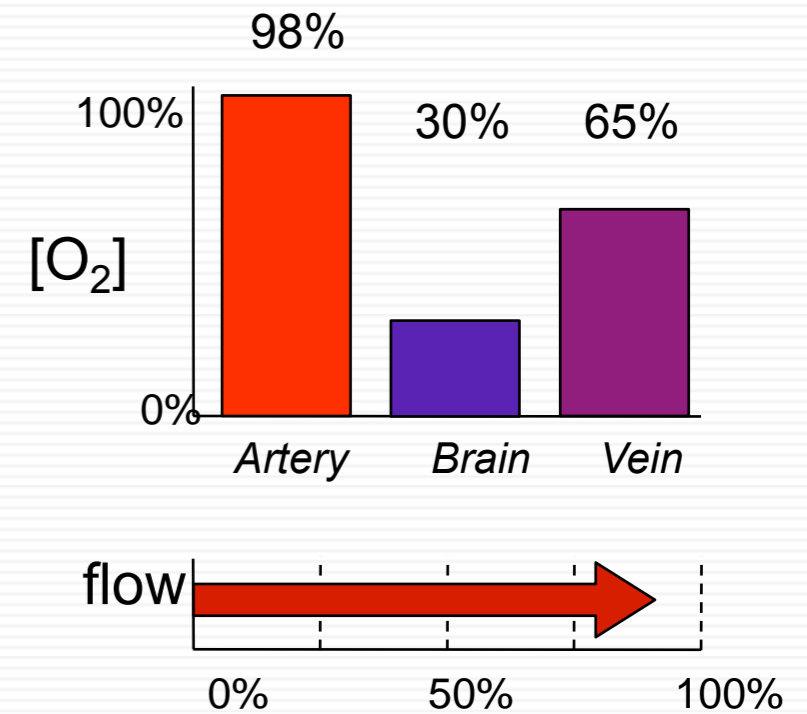
Why Does Venous O₂ Increase? ⁽³⁾



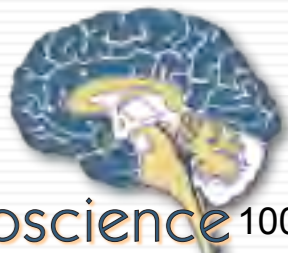
As oxygen flows across the capillary lumen it is depleted in the capillary and no further oxygen can be delivered



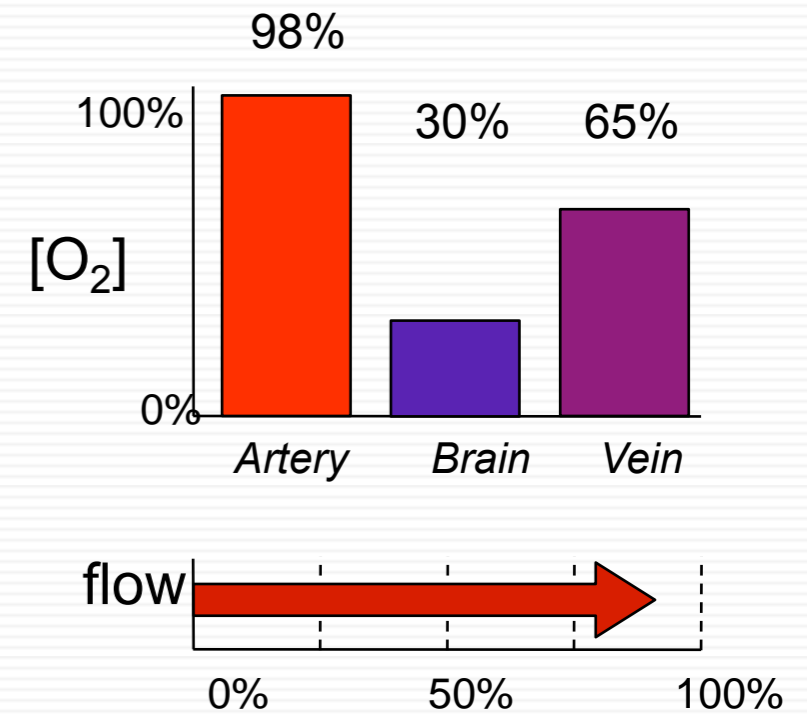
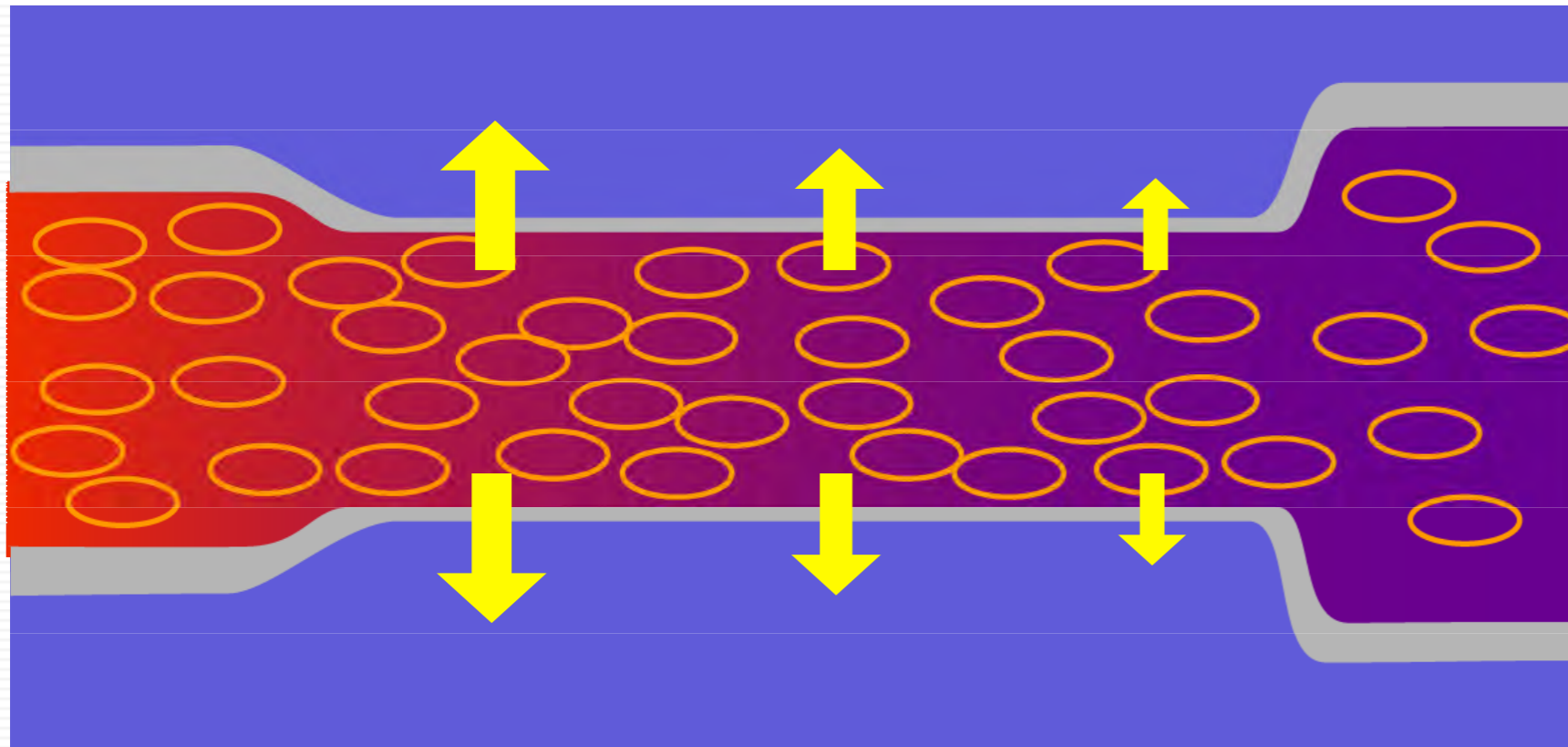
Why Does Venous O₂ Increase? ⁽⁴⁾



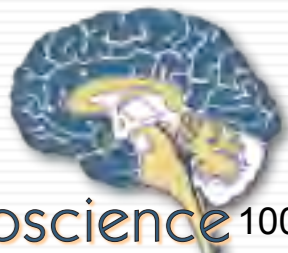
The vascular system responds by increasing blood flow so that more oxygenated blood is available throughout the capillary



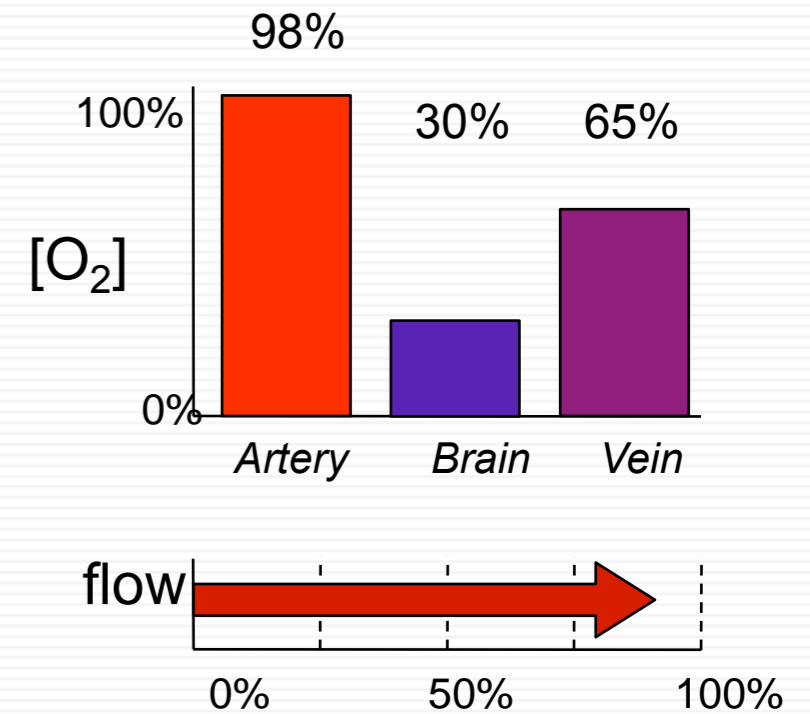
Why Does Venous O₂ Increase? ⁽⁴⁾



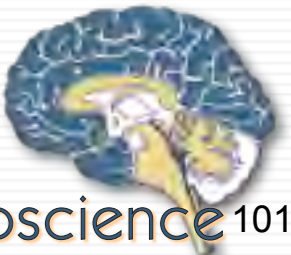
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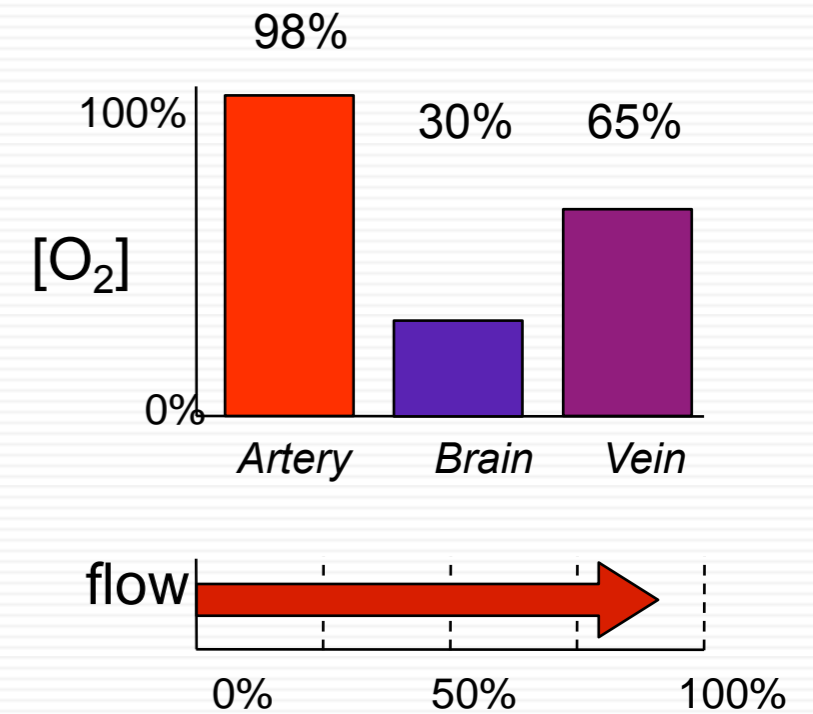
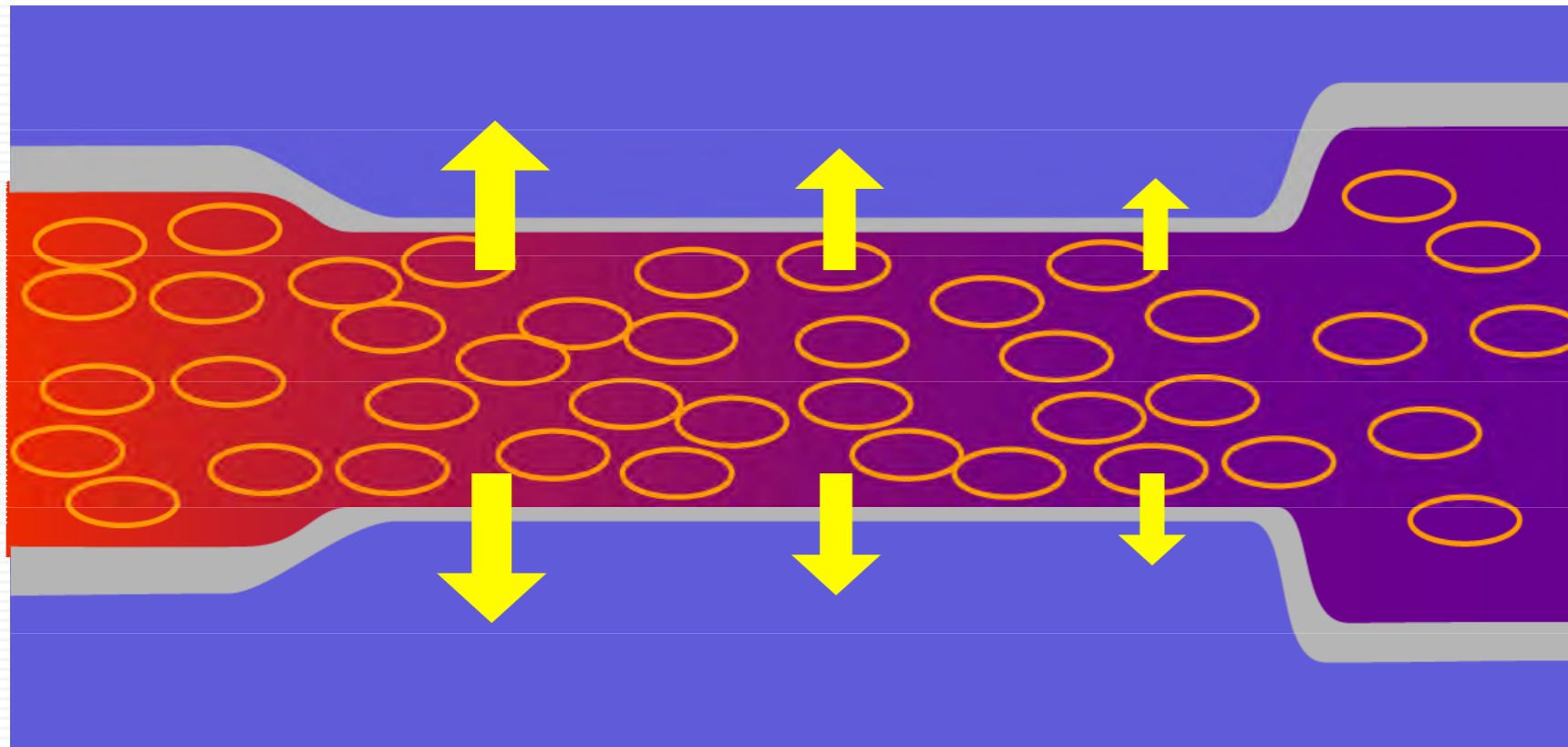
Why Does Venous O₂ Increase? ⁽⁵⁾



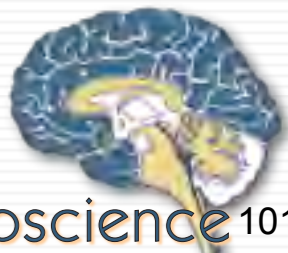
Because the blood flow is increased more oxygenated blood passes into the venous end of the capillary



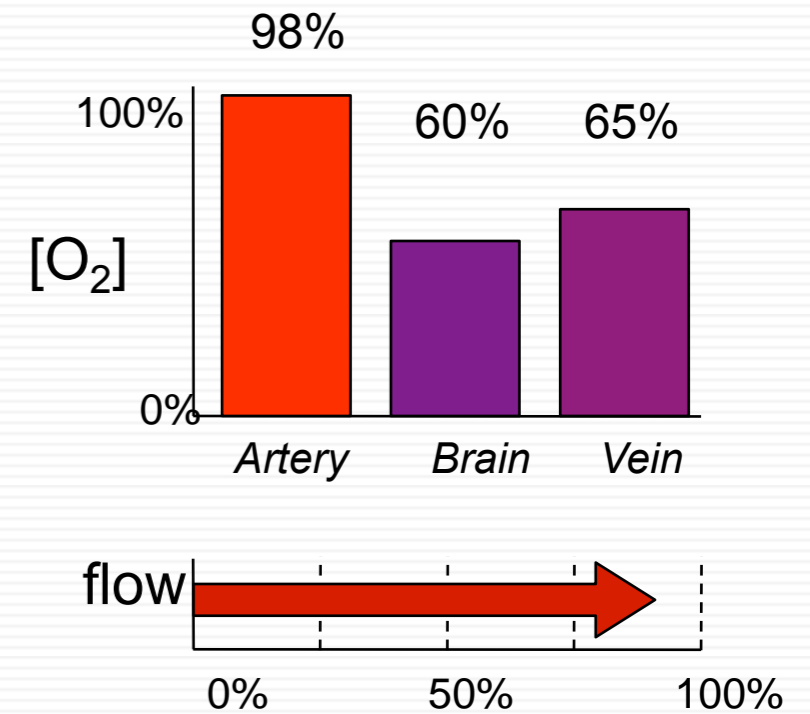
Why Does Venous O₂ Increase? ⁽⁵⁾



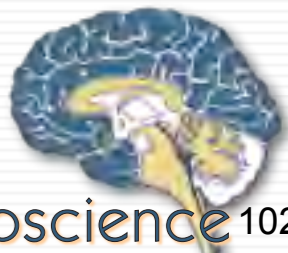
Because the blood flow is increased more oxygenated blood passes into the venous end of the capillary



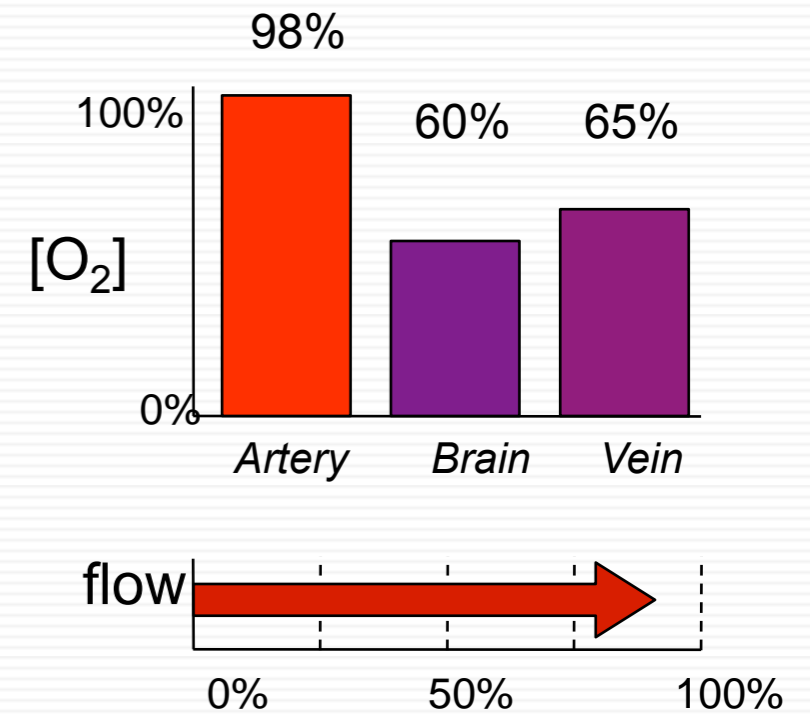
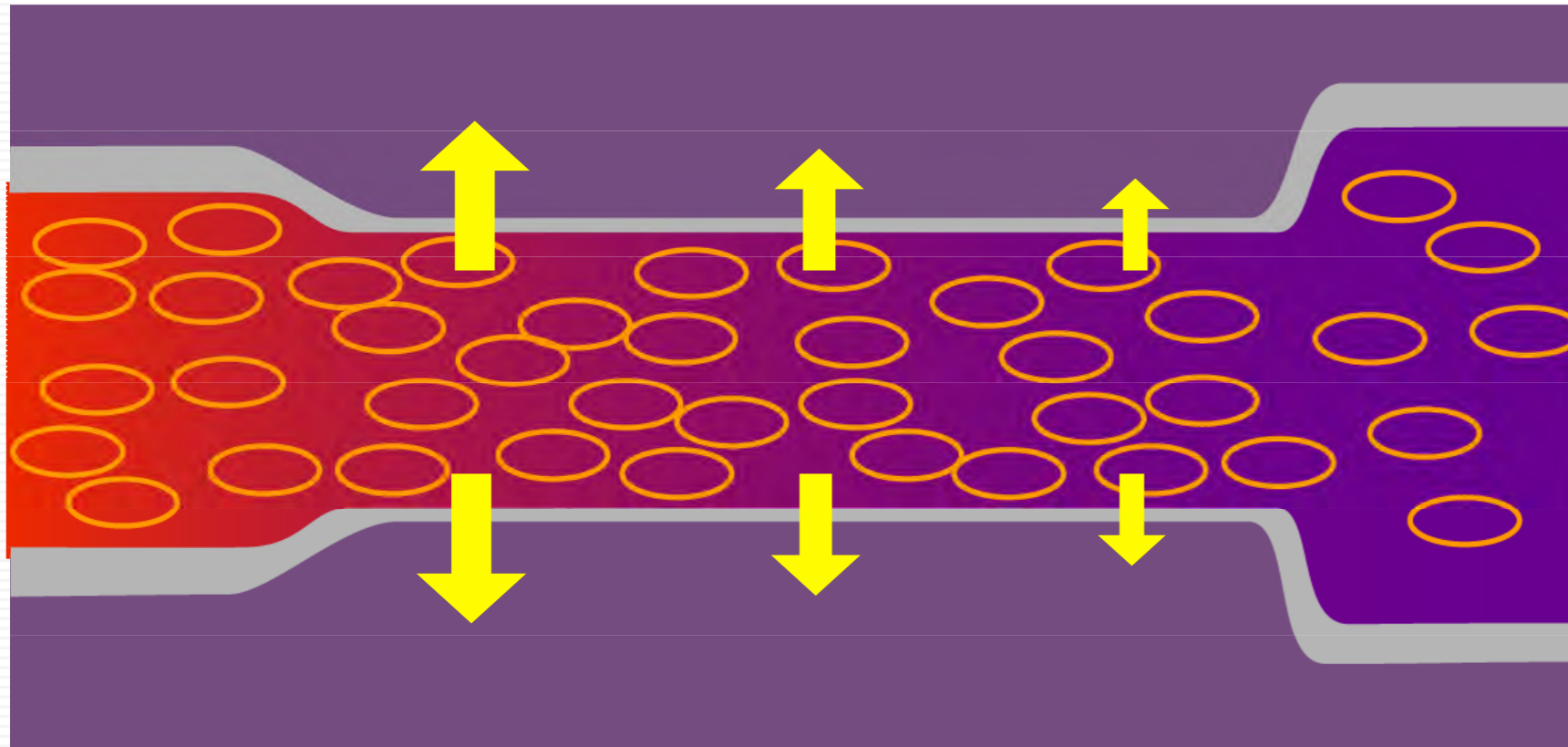
Why Does Venous O₂ Increase? ⁽⁶⁾



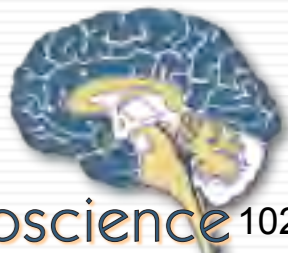
Because the blood flow is increased more oxygenated blood passes into the venous end of the capillary



Why Does Venous O₂ Increase? ⁽⁶⁾



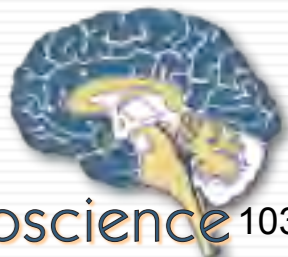
Because the blood flow is increased more oxygenated blood passes into the venous end of the capillary



BOLD Contrast & Field Strength

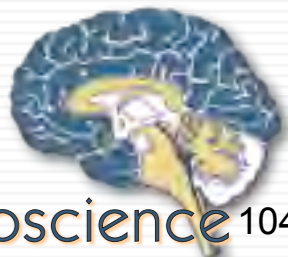
- BOLD Contrast arises from susceptibility differences
- The *absolute* field distortion (from BOLD) is proportional to the magnetic field strength
- The *absolute change* in MRI signal is proportional to *both* the field distortion and the signal strength.

BOLD *should* go as kB_0^2



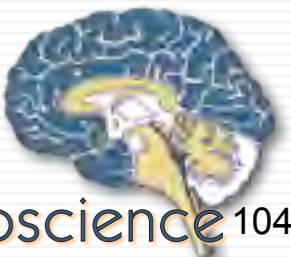
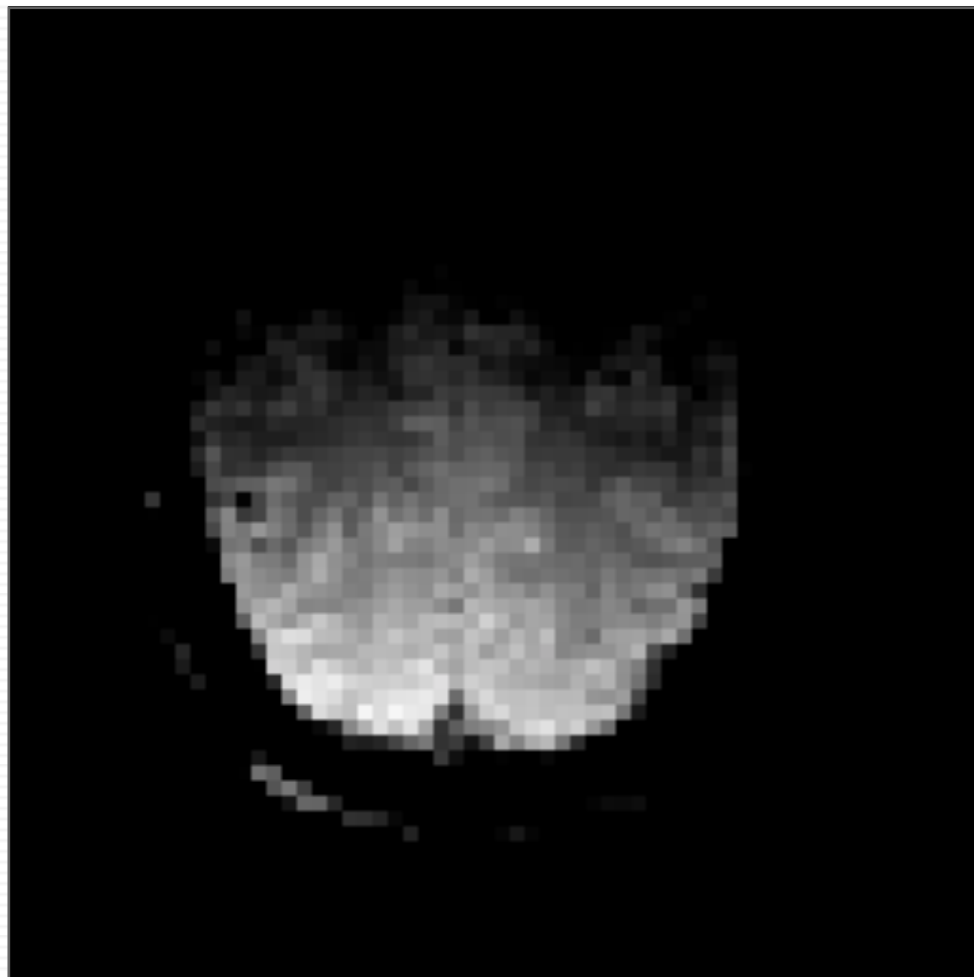
fMRI

explores intensity variations in MR signal



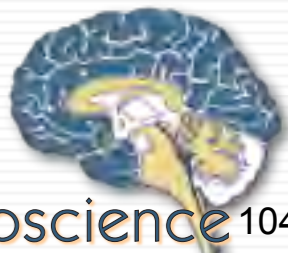
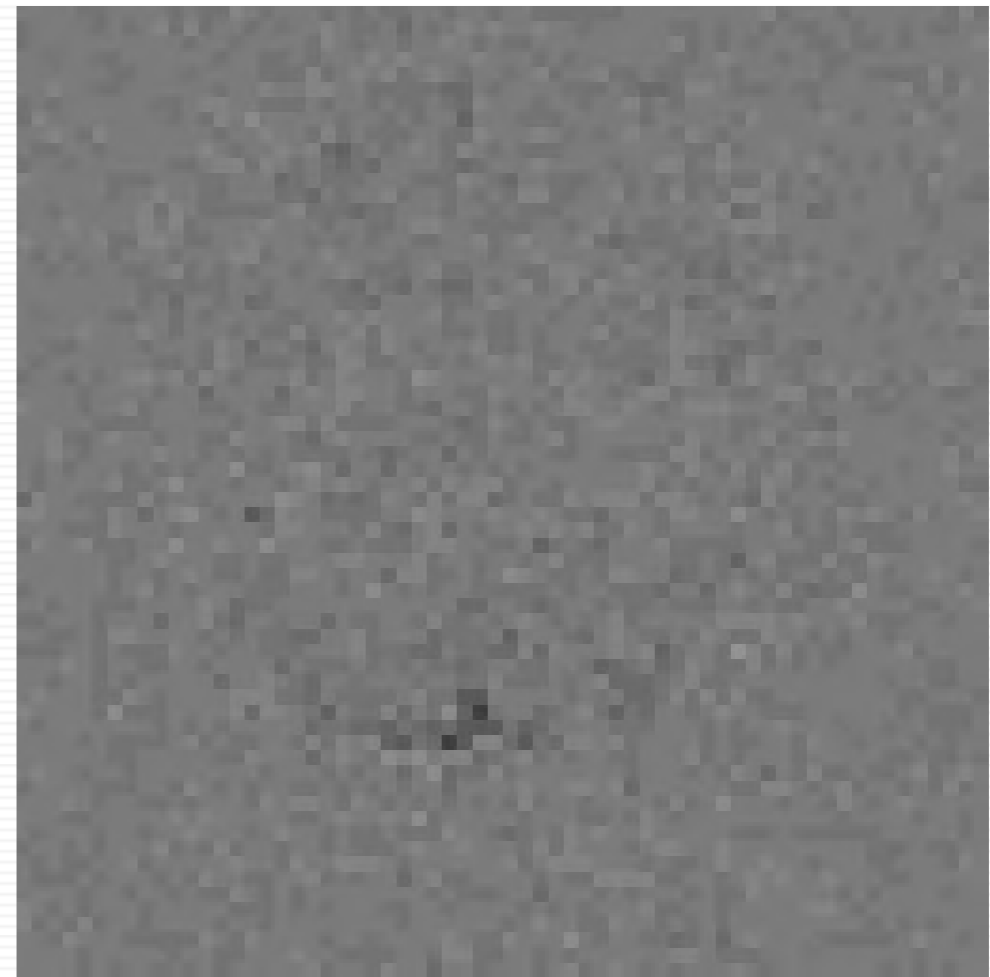
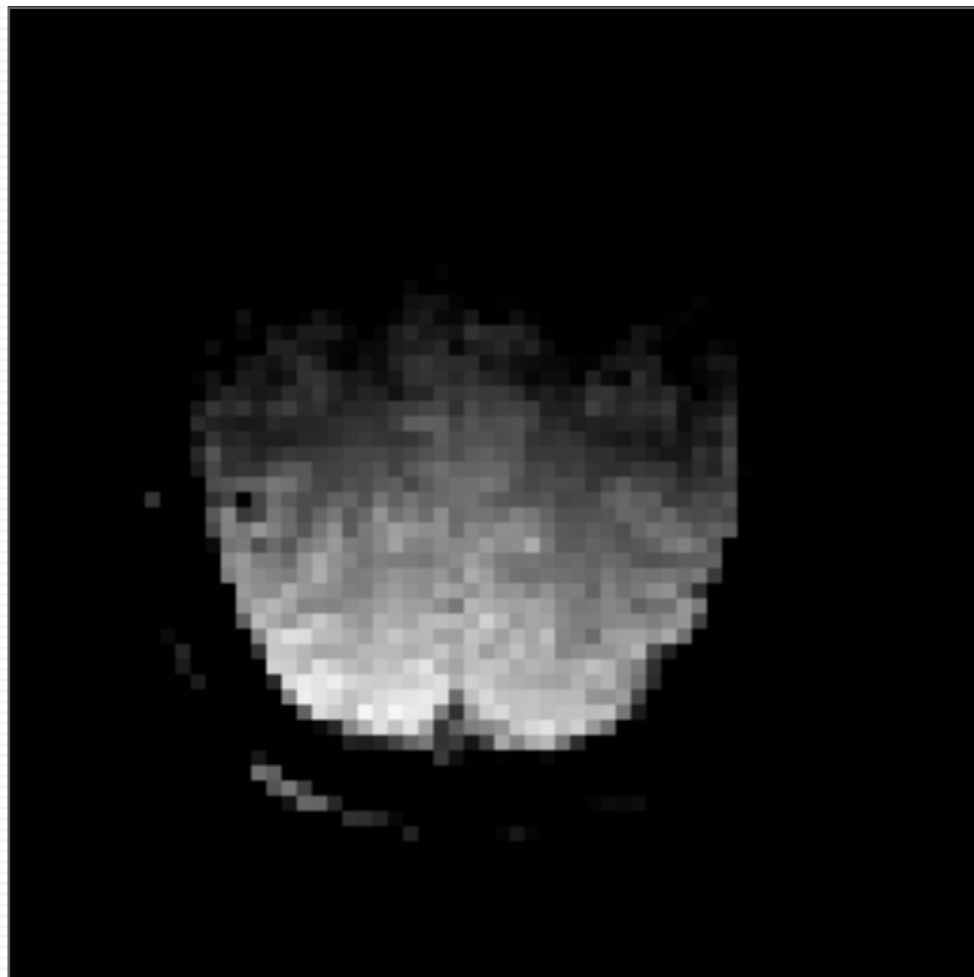
fMRI

explores intensity variations in MR signal



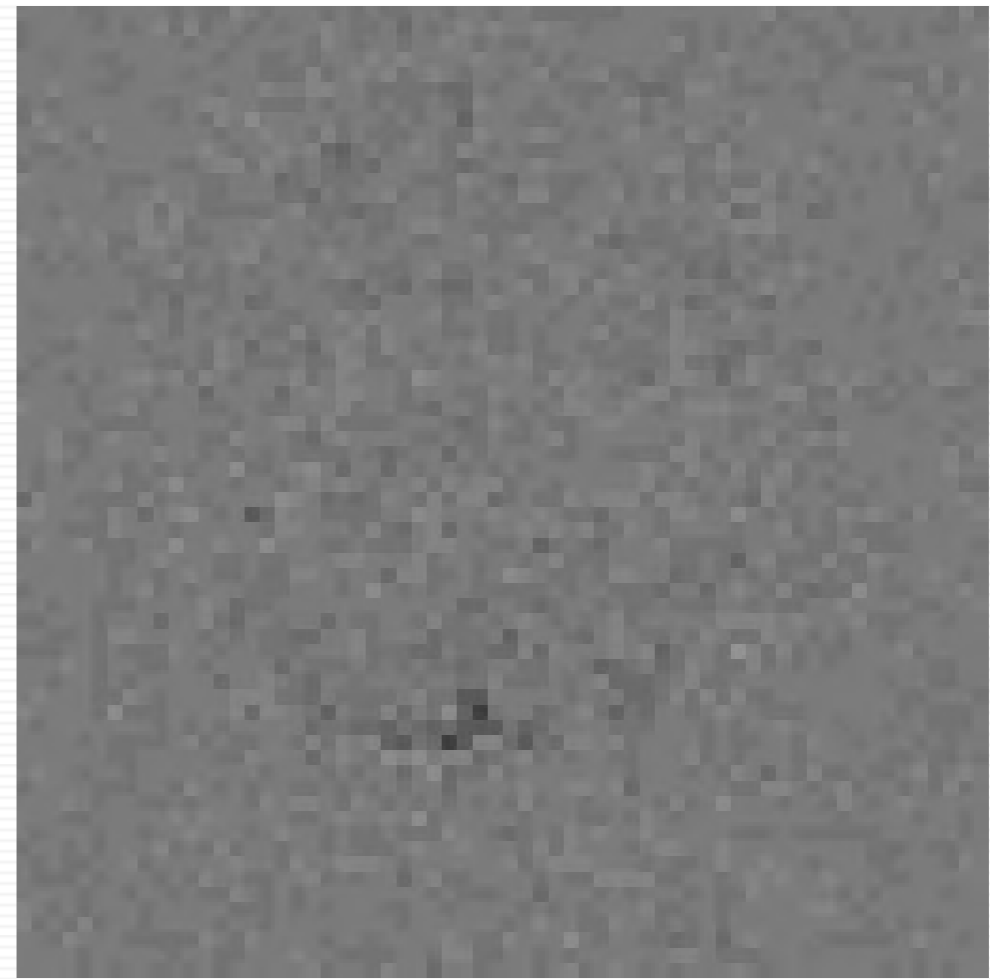
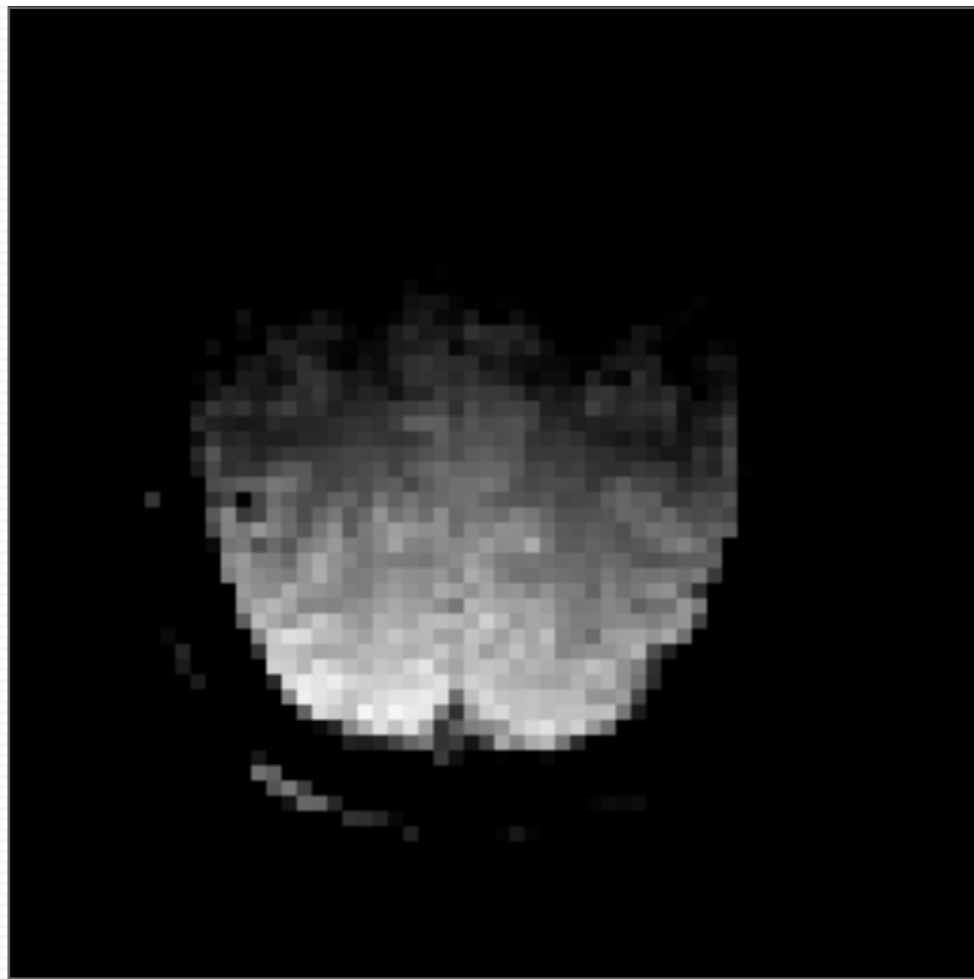
fMRI

explores intensity variations in MR signal

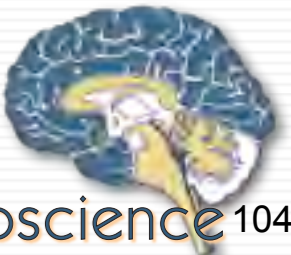


fMRI

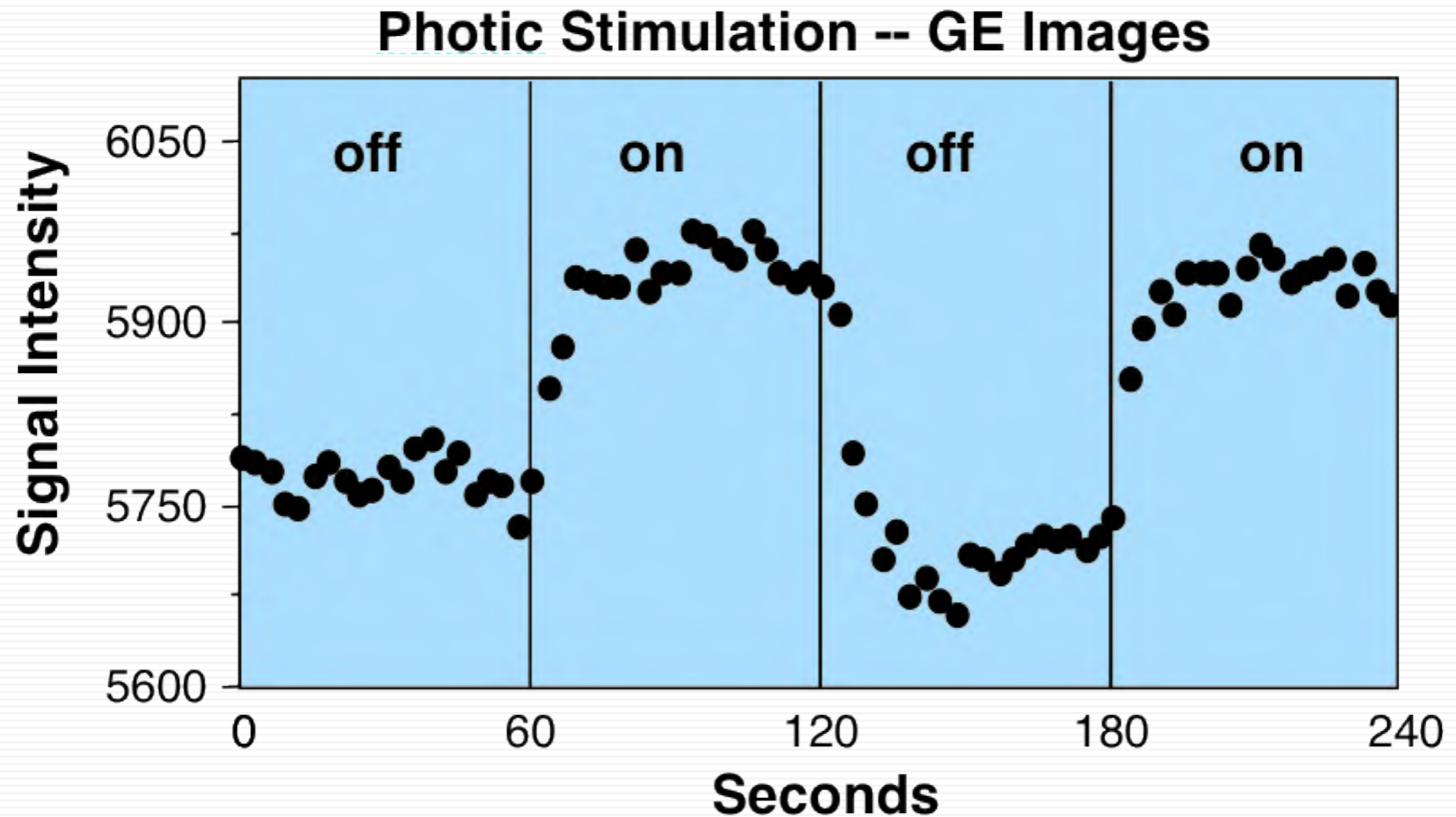
explores intensity variations in MR signal



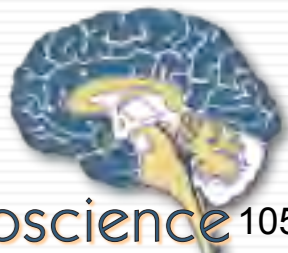
intensity variations reflect venous [O₂]



Gradient-Recalled Echo

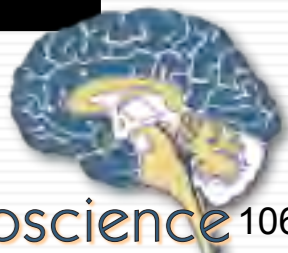
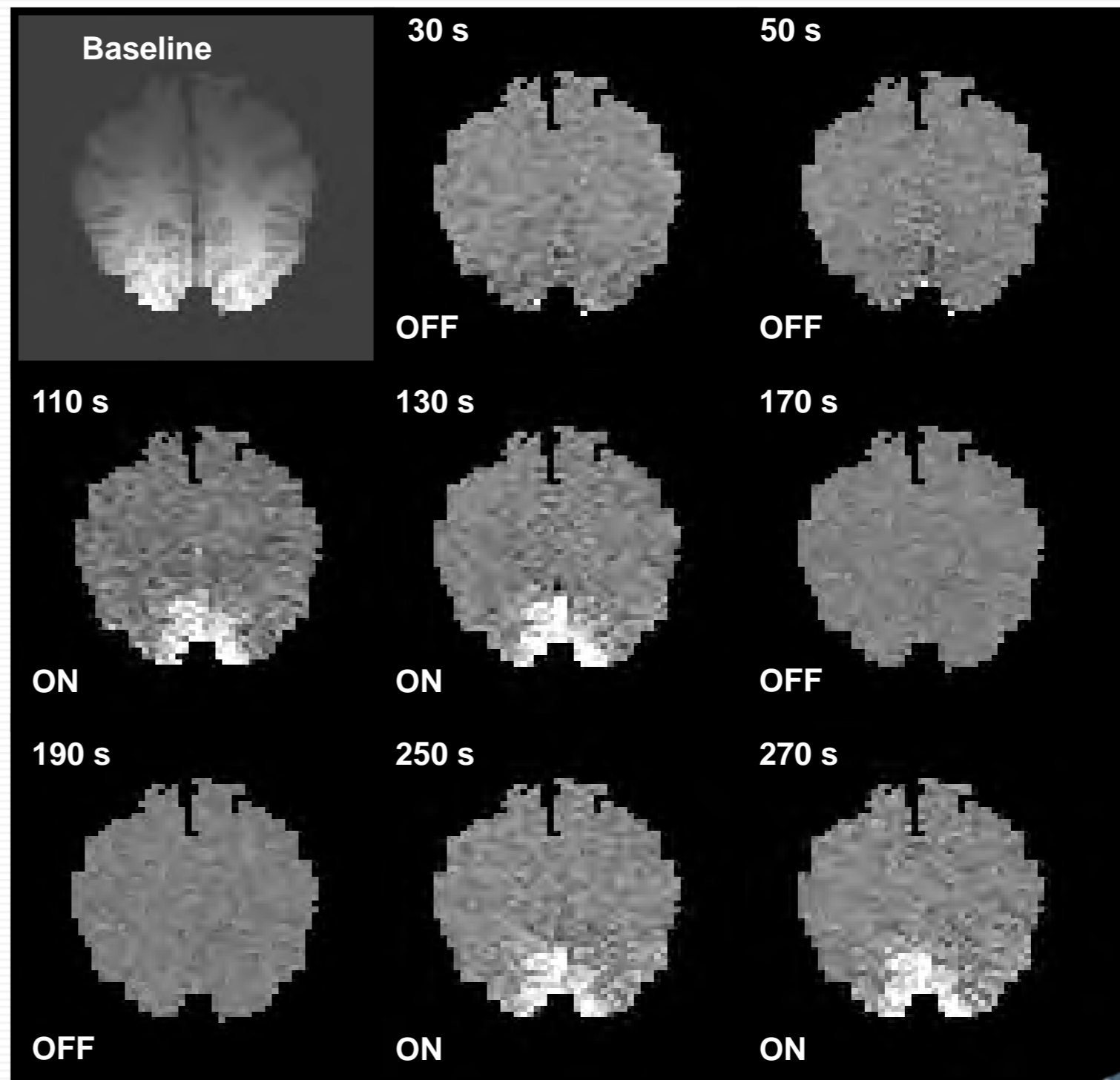


Ken Kwong



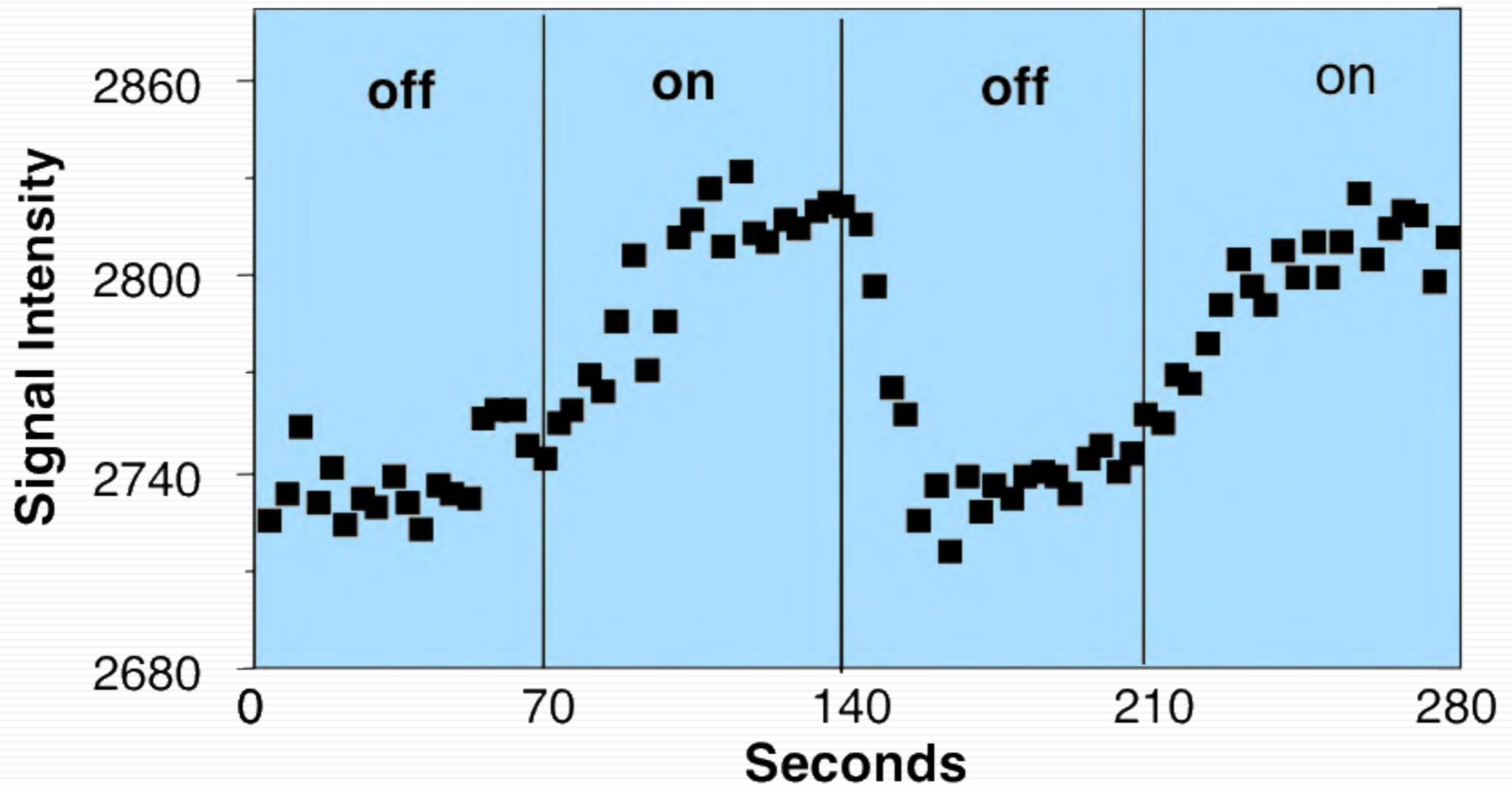
Ken Kwong

Inversion Recovery
TE=42 TR=3000
TI = 1100
Thickness=10

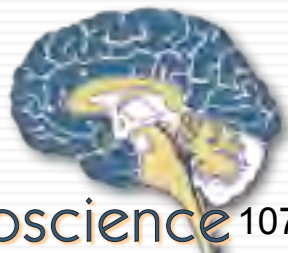


Inversion Recovery

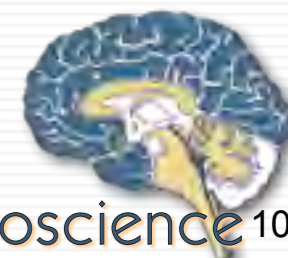
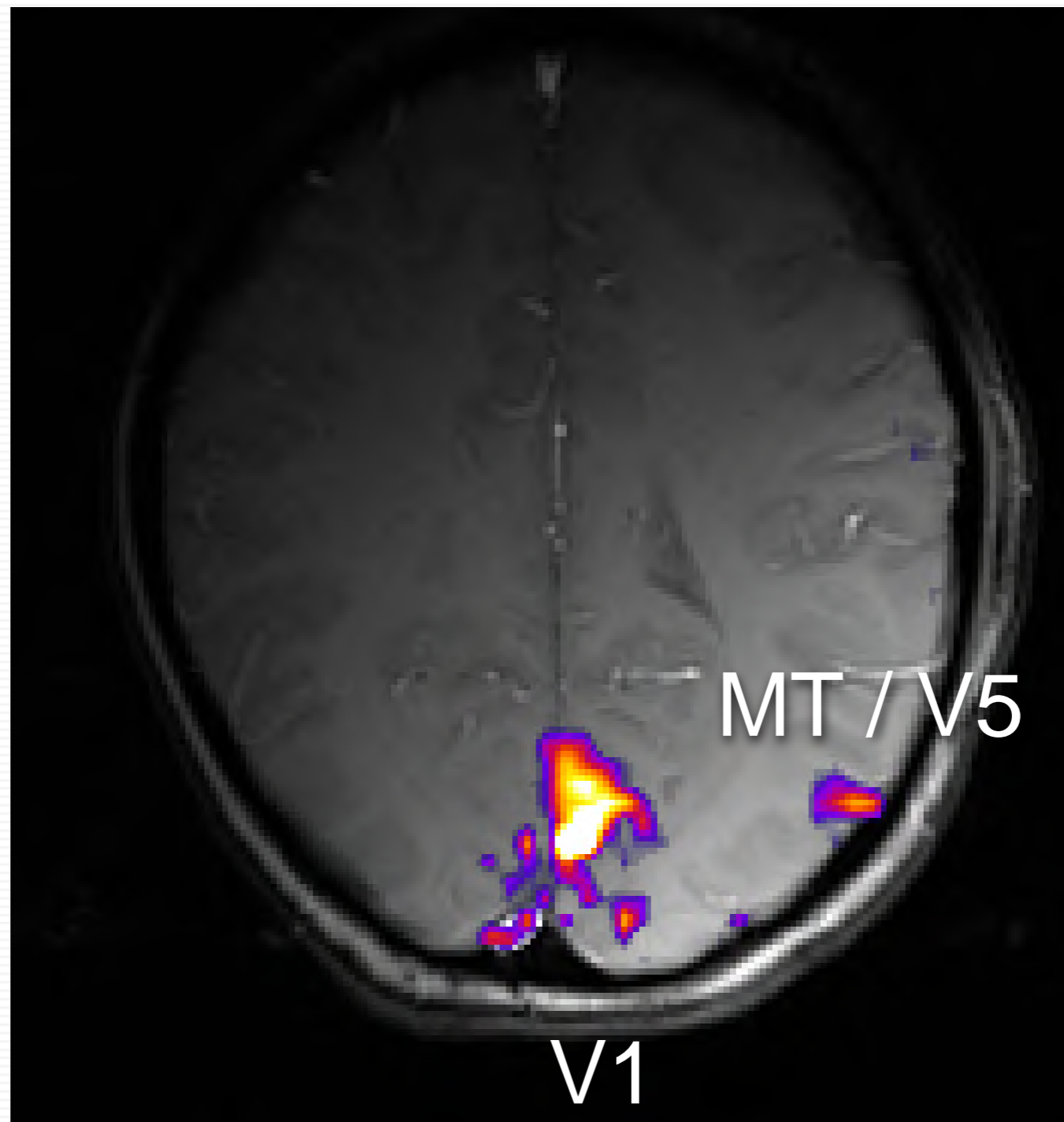
Photic Stimulation -- IR Images



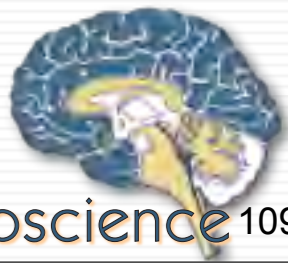
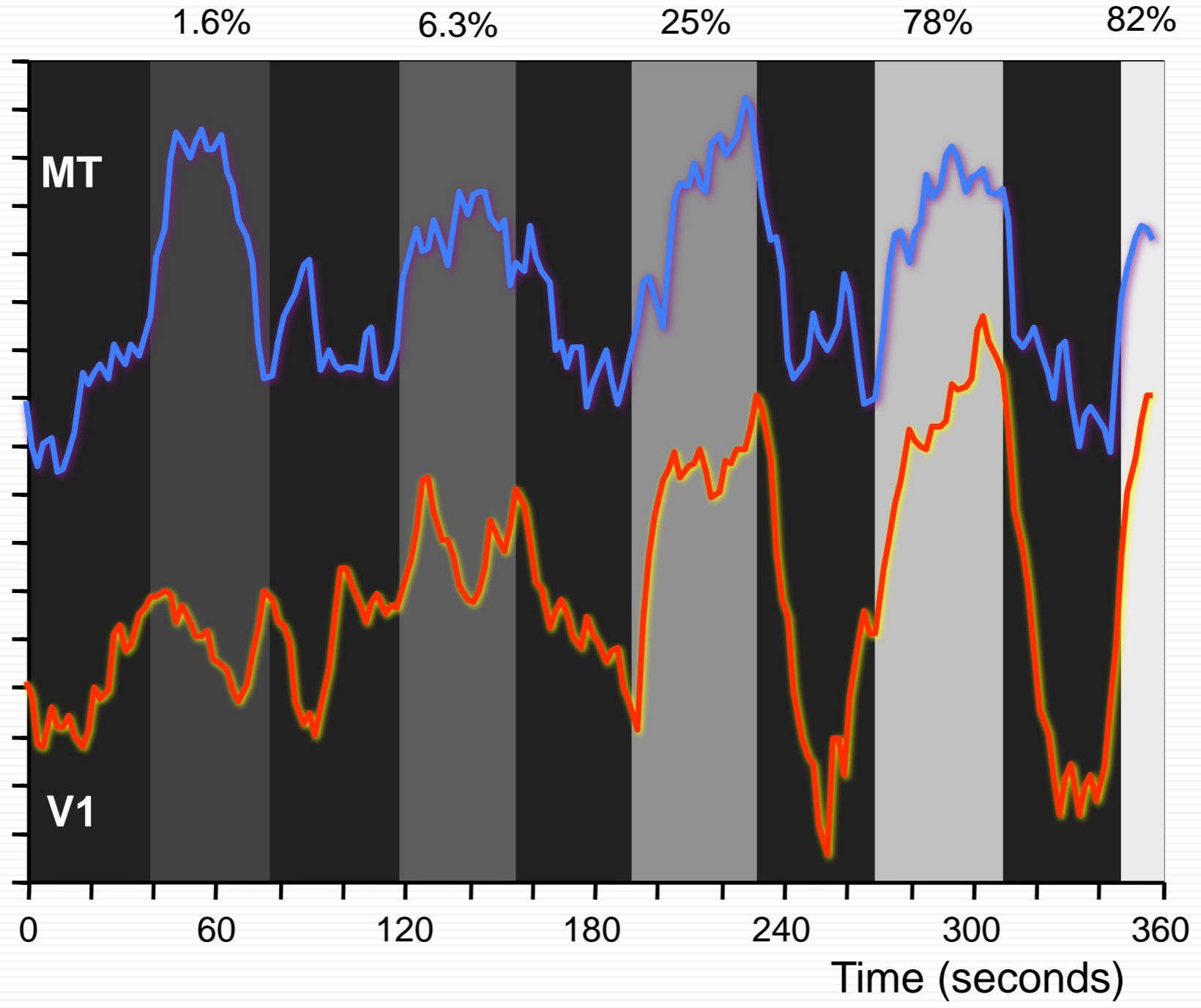
Ken Kwong



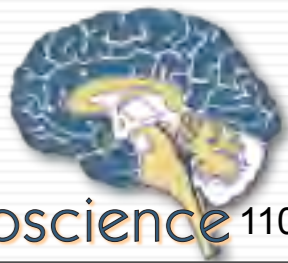
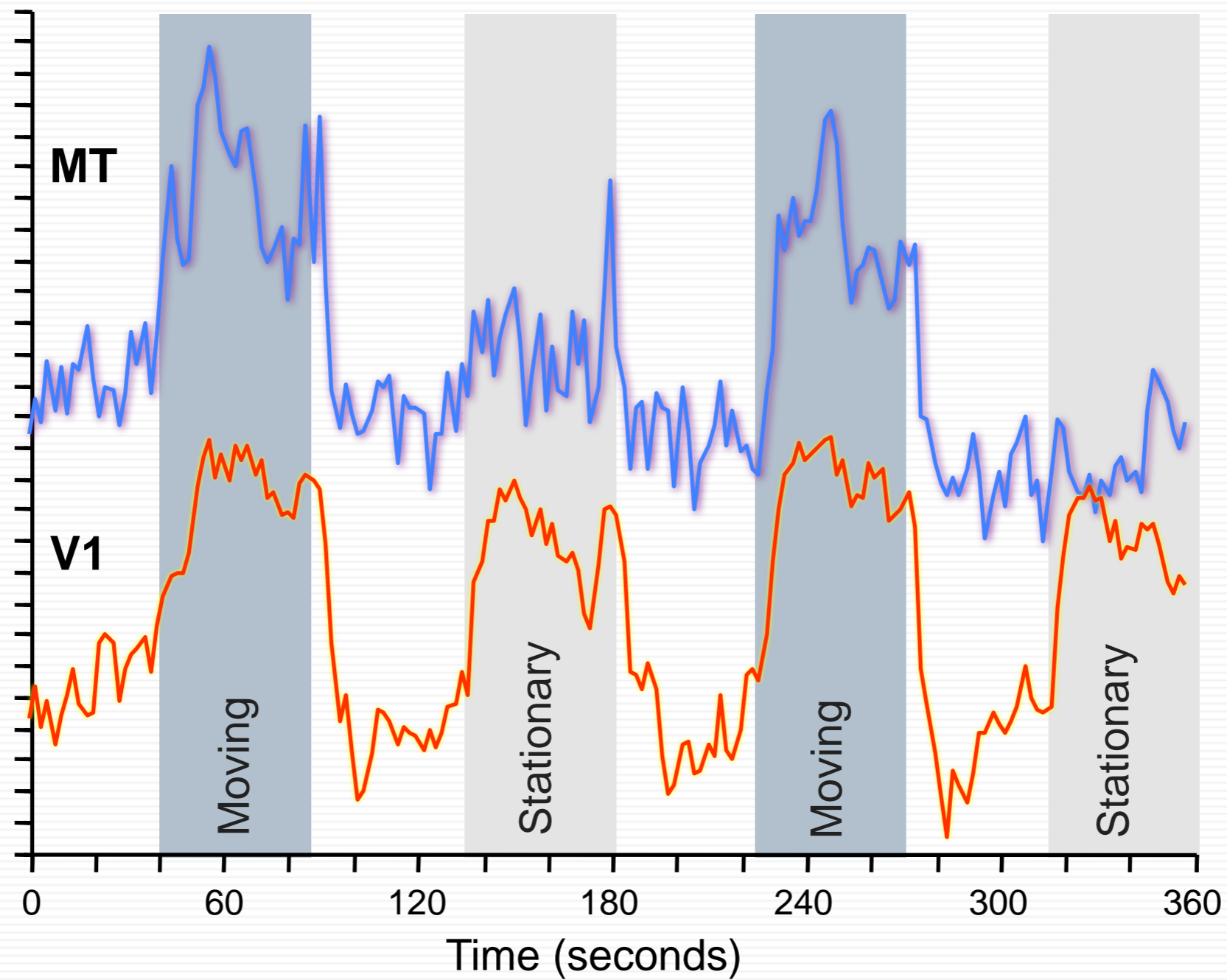
Activation with Moving Visual Stimuli



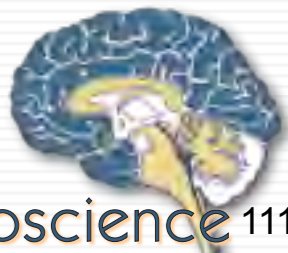
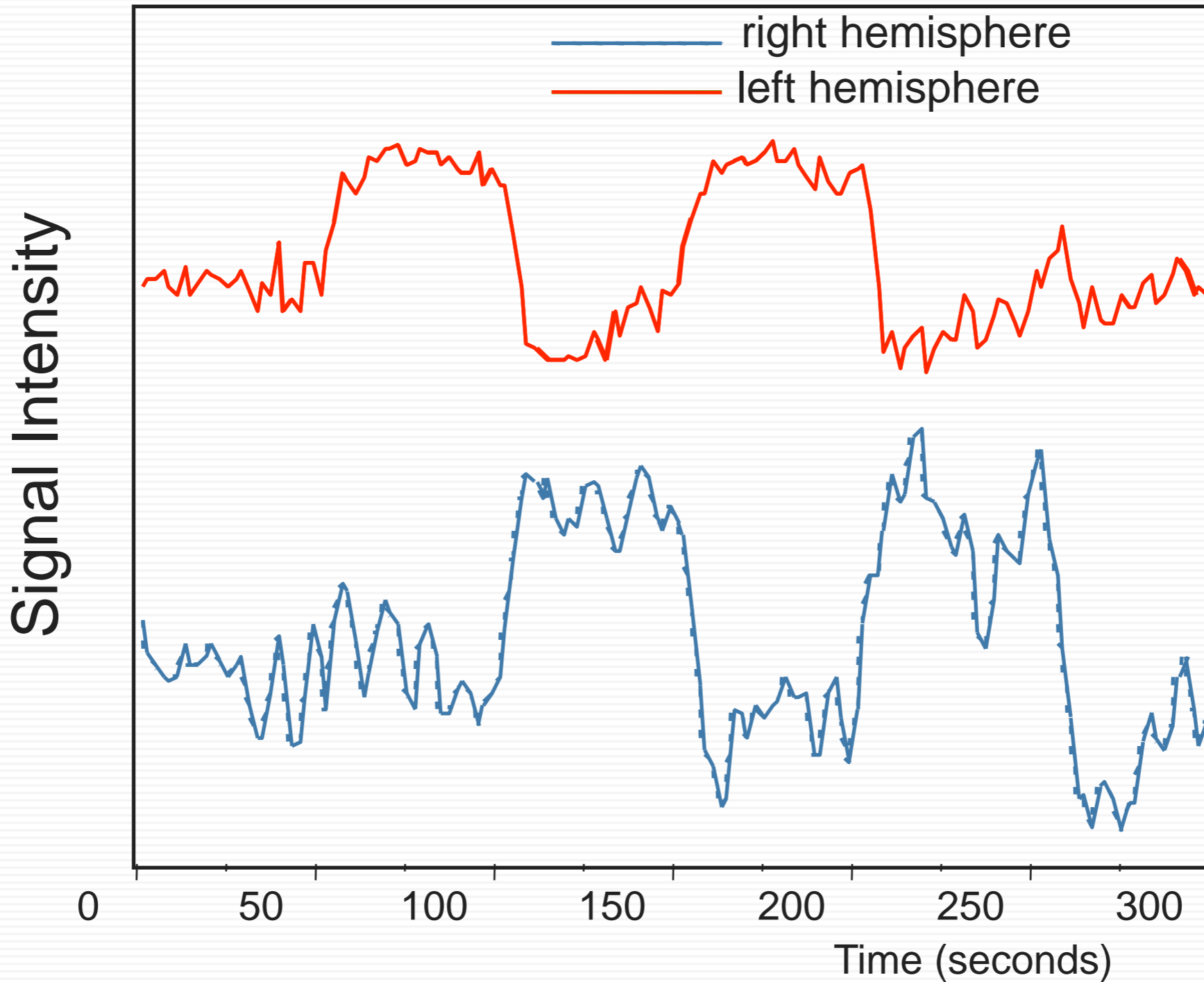
Contrast Response Test



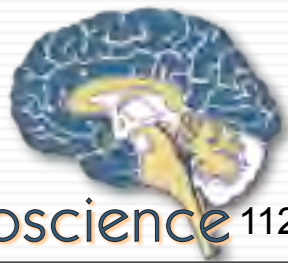
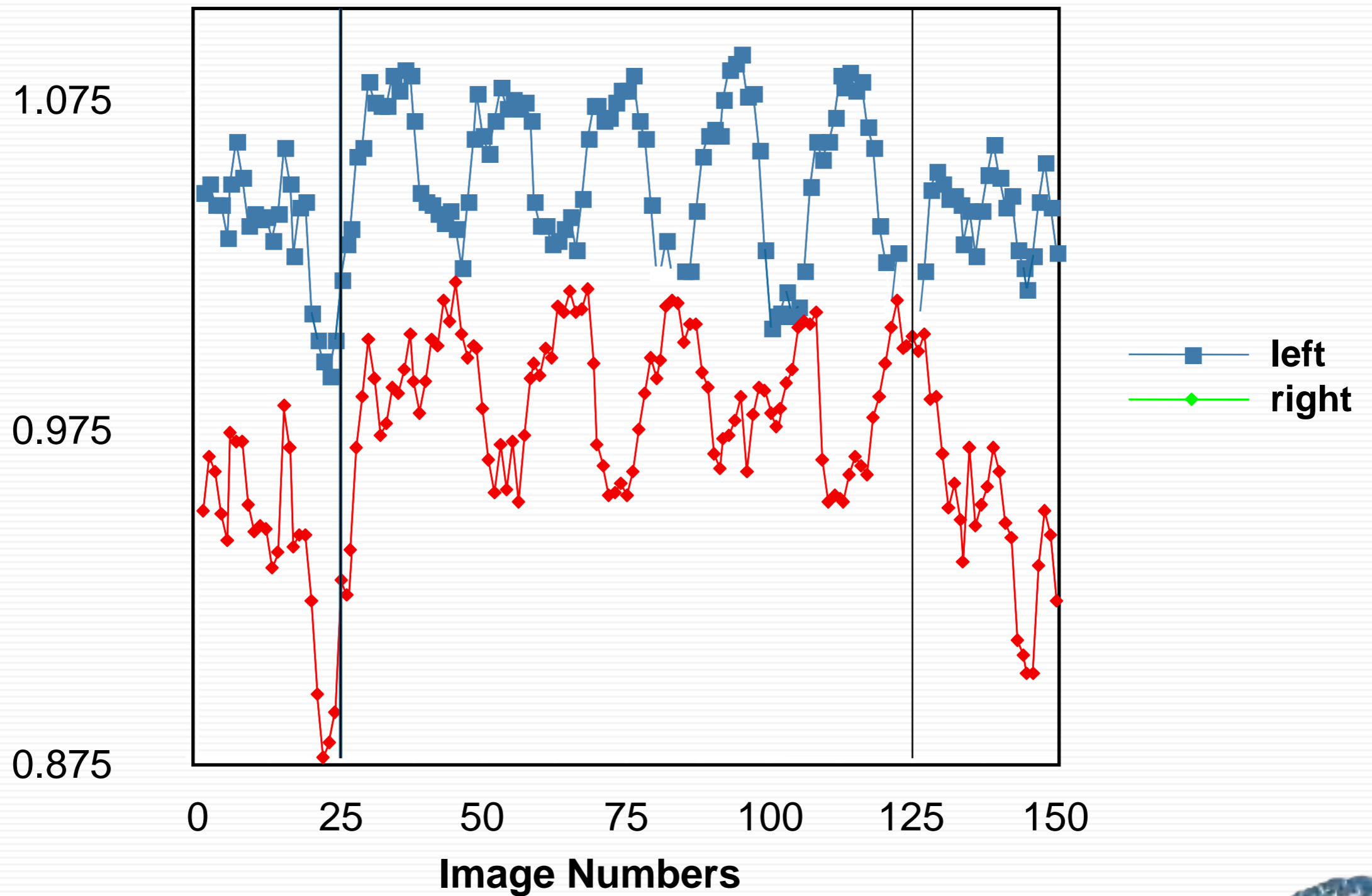
Motion Sensitivity Test



Hemifield Alternation



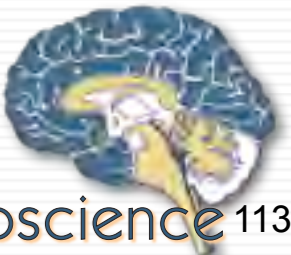
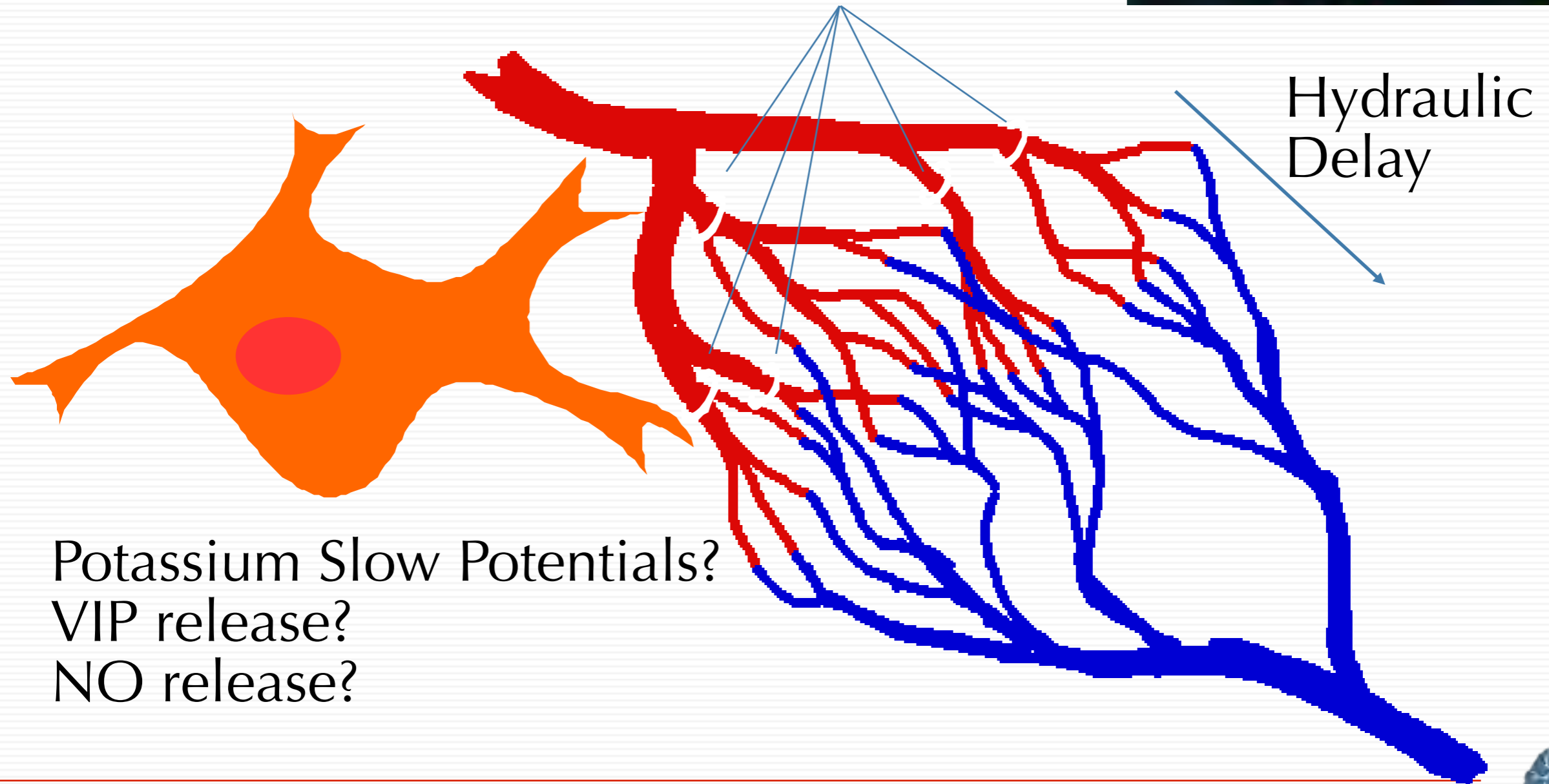
Hemifield Alternation 20 seconds



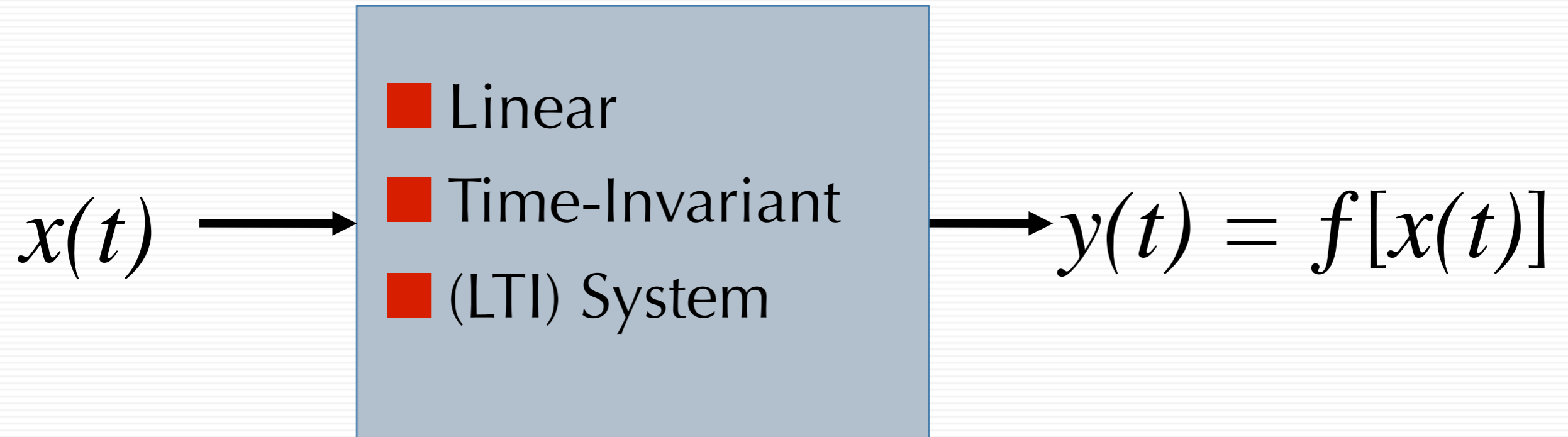
Neurovascular Coupling and *fMRI* latency



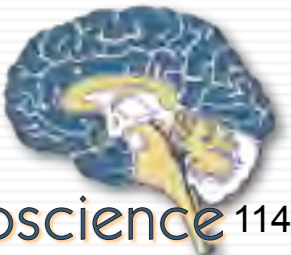
Pre-capillary Sphincters



Linear Systems Approach

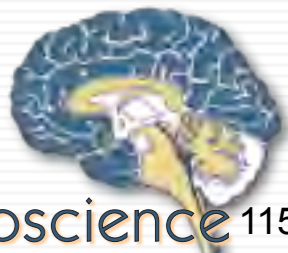
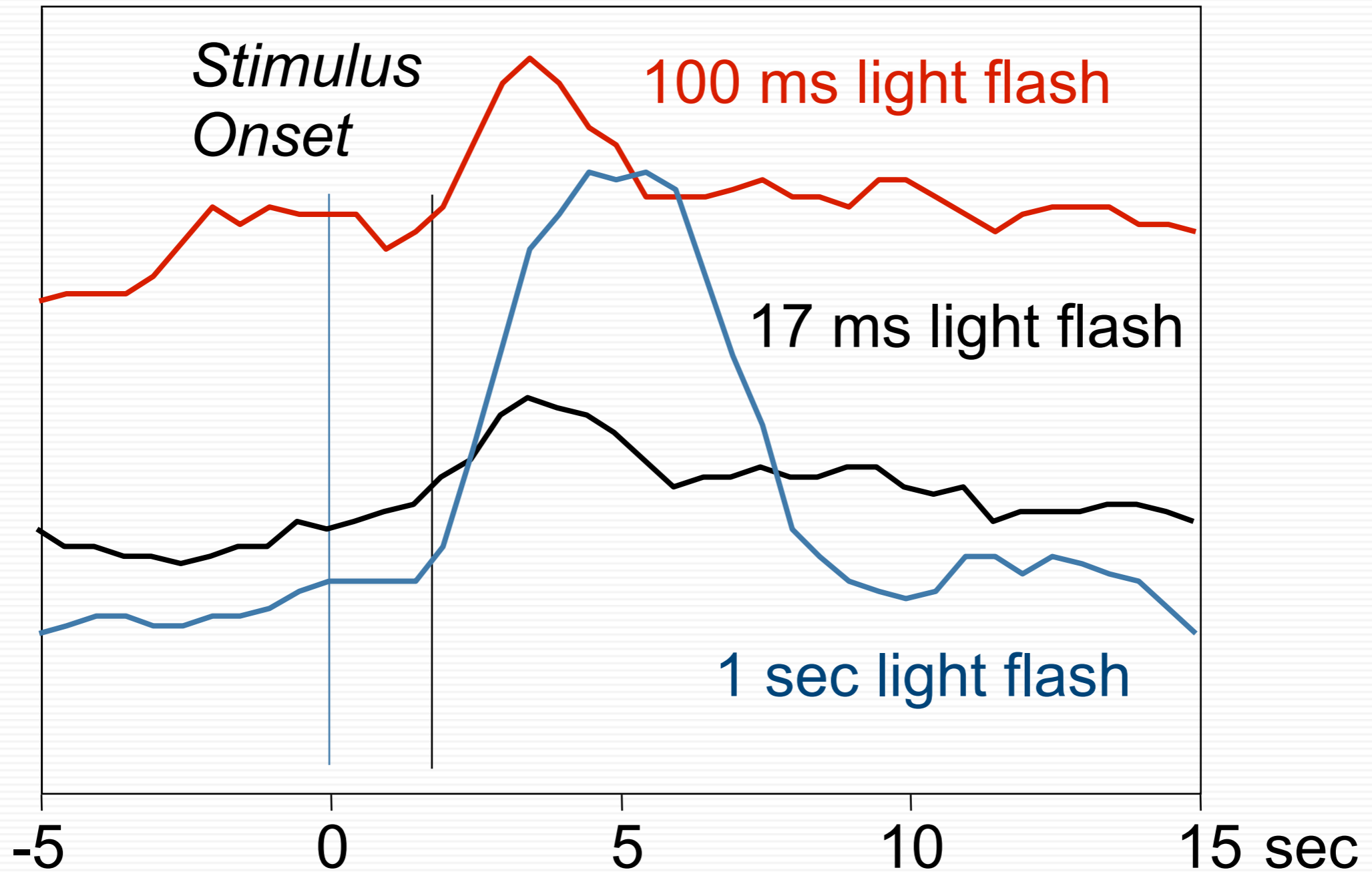


In an LTI system, given two inputs A & B:
 $f(A + B) = f(A) + f(B)$

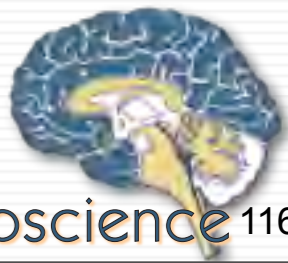
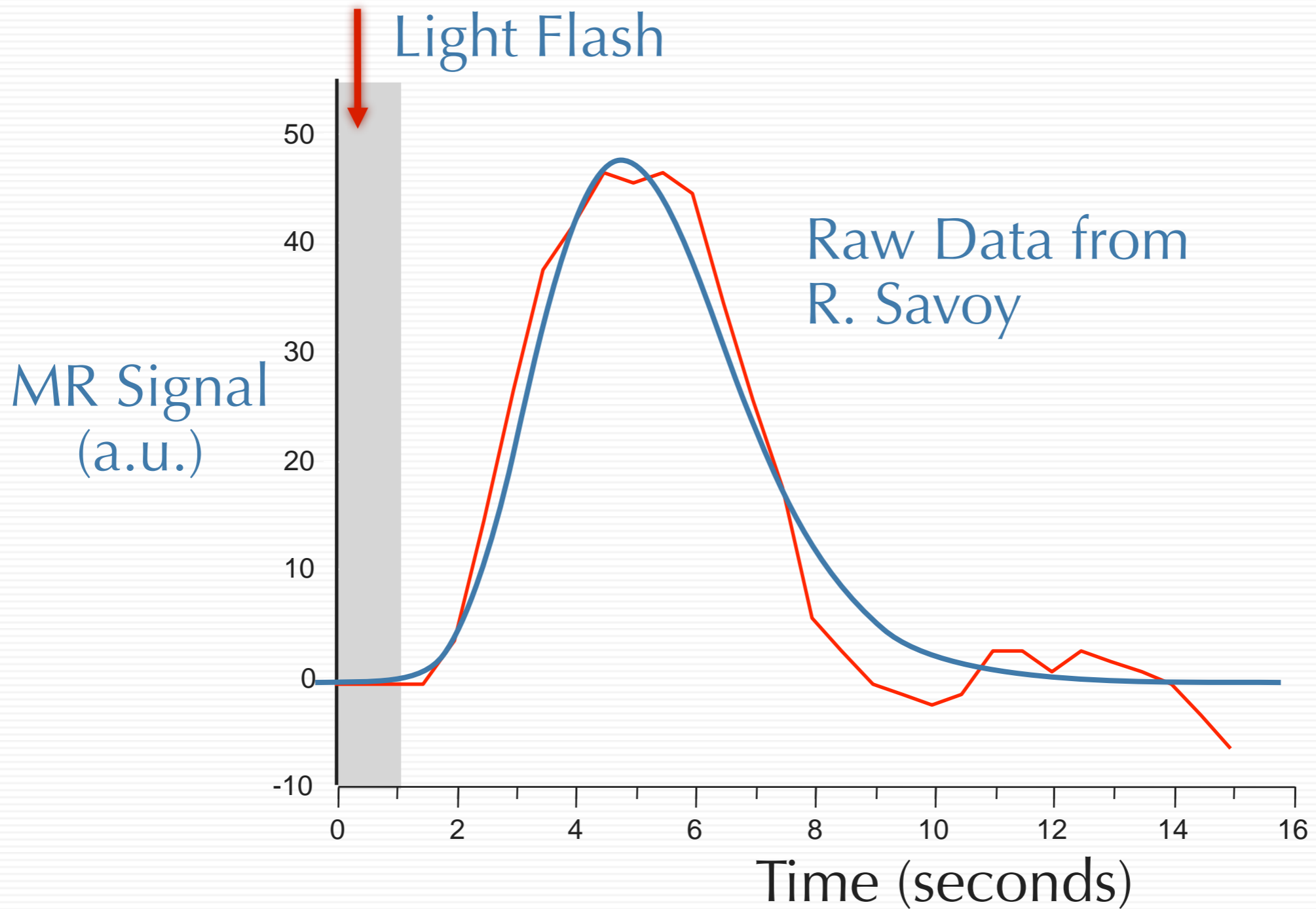


Response Latency vs. Stimulus Duration

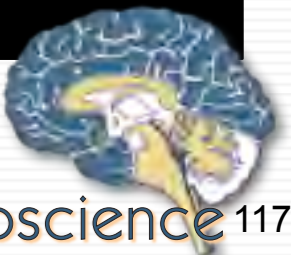
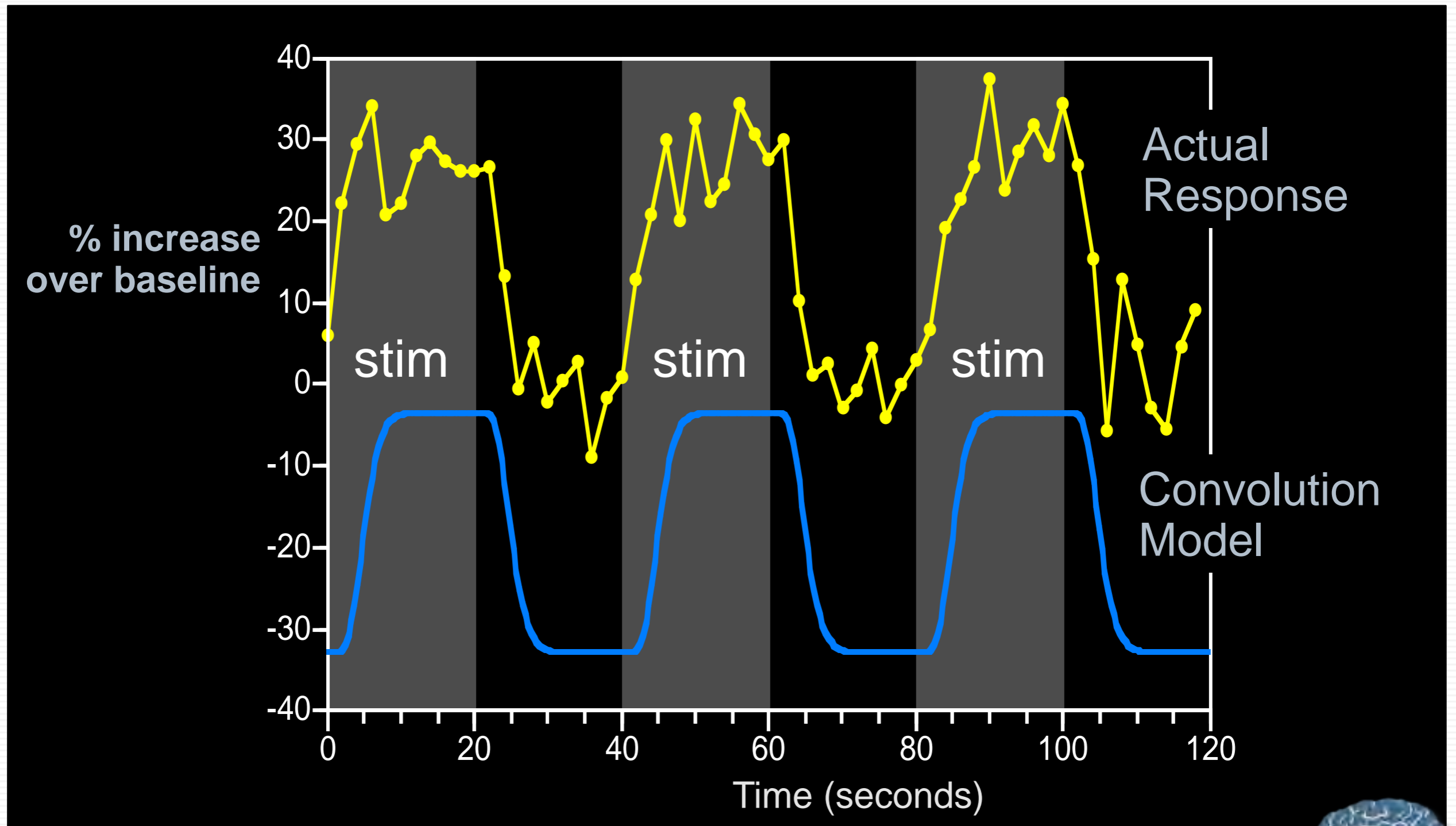
Average of 10 recordings



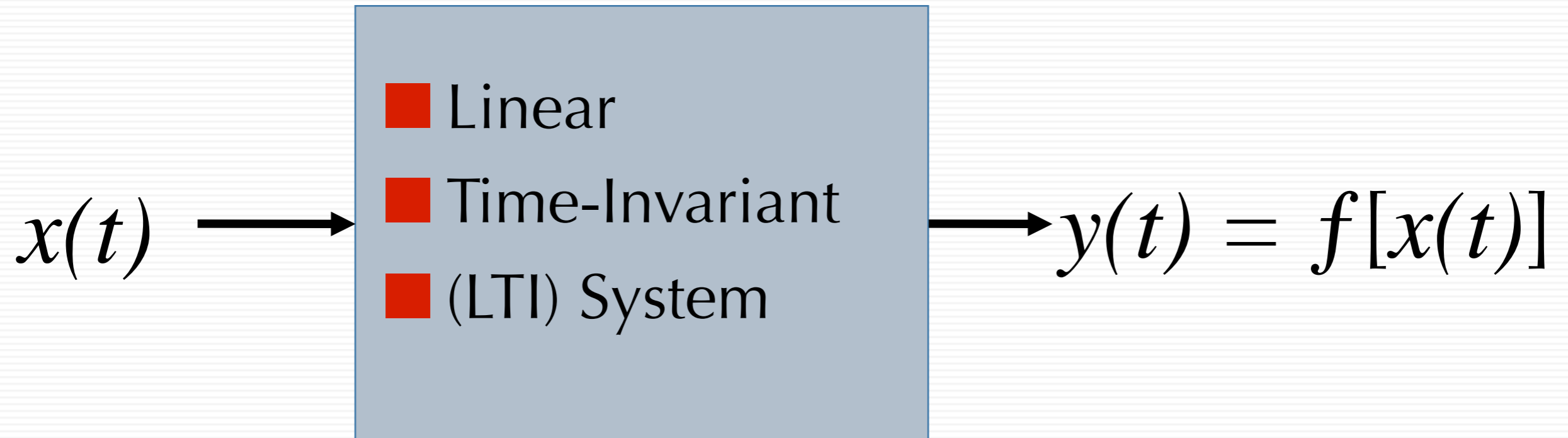
Brain Impulse Response



Convolution of Impulse Responses with Stimuli

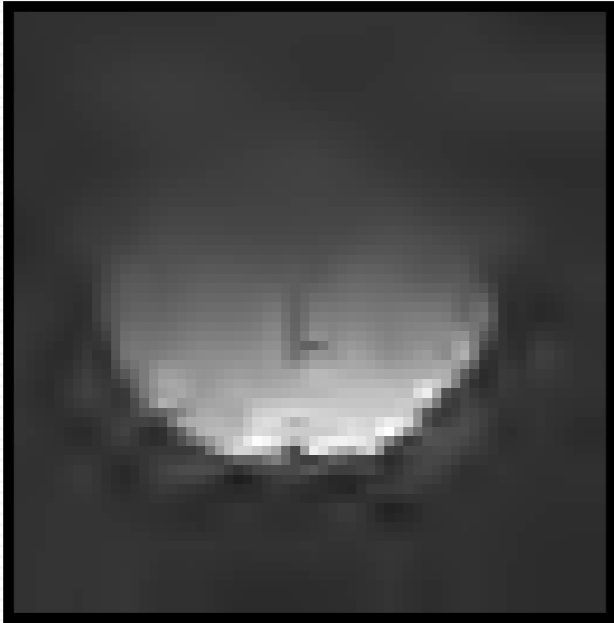


Linear Systems Approach

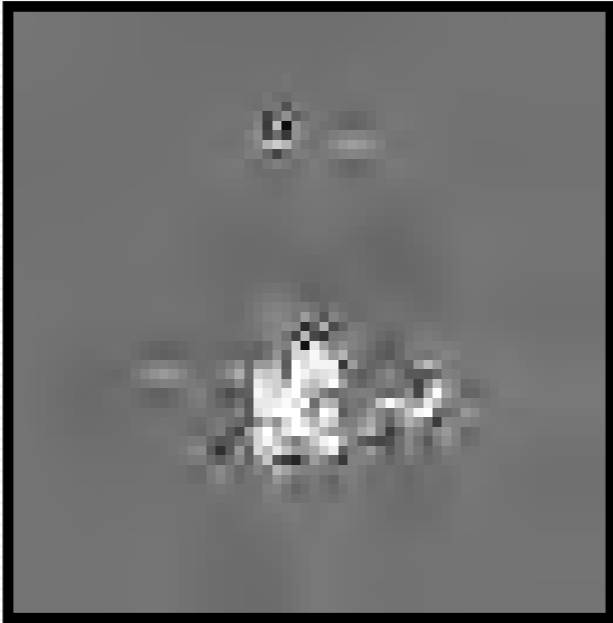


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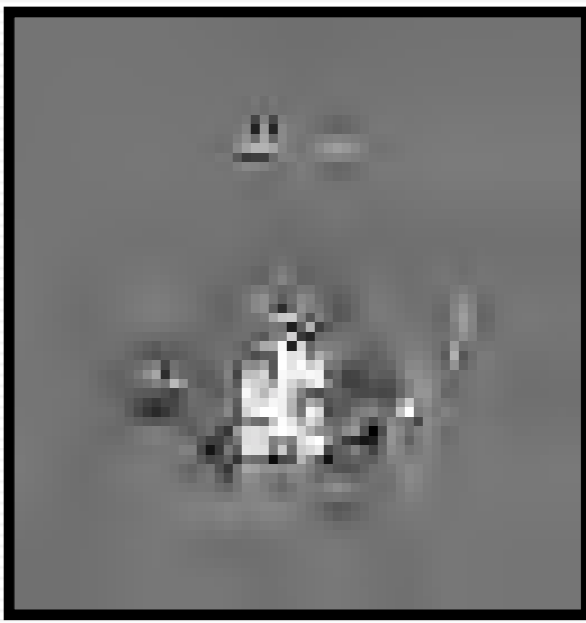
Binocular vs Monocular Activation



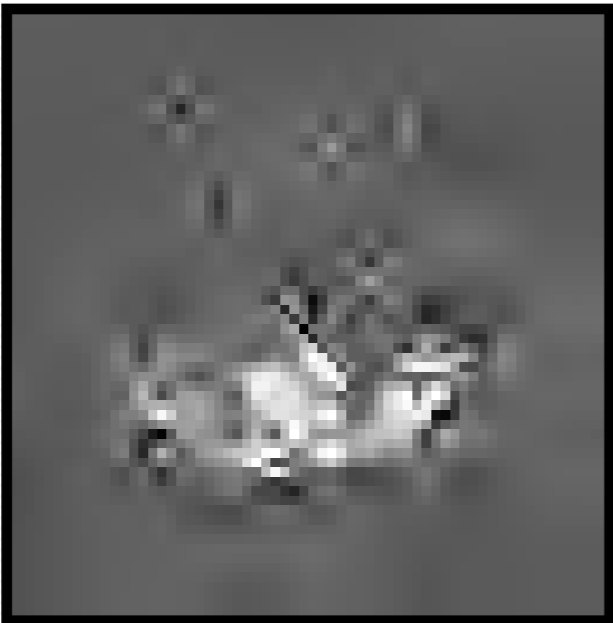
baseline



Binocular



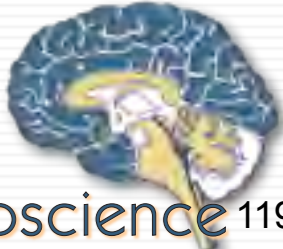
Monocular



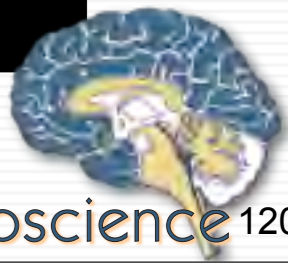
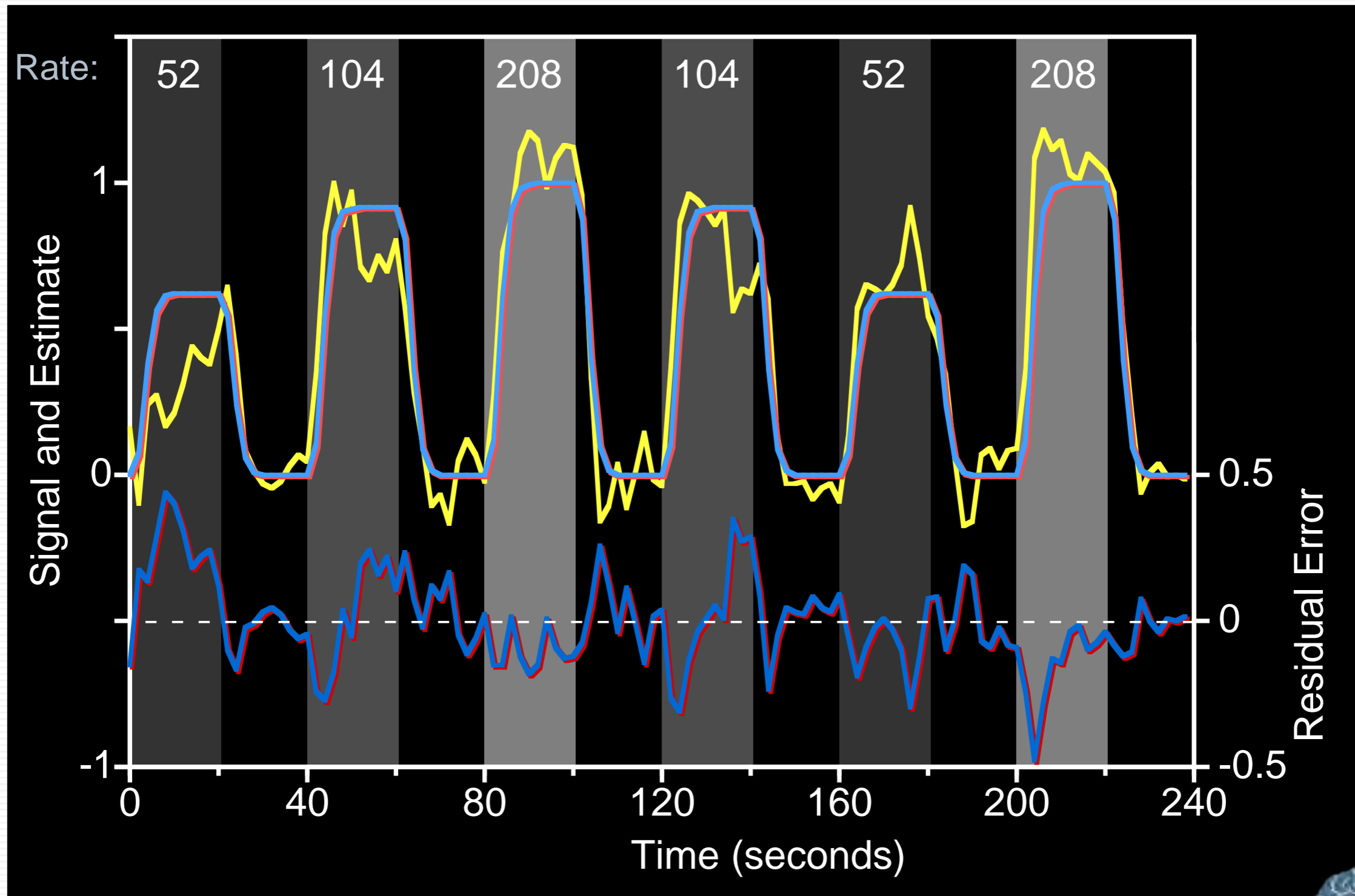
Bino minus Mono



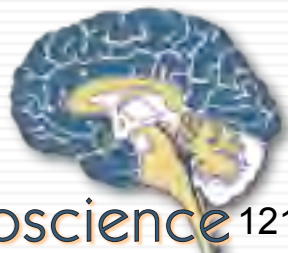
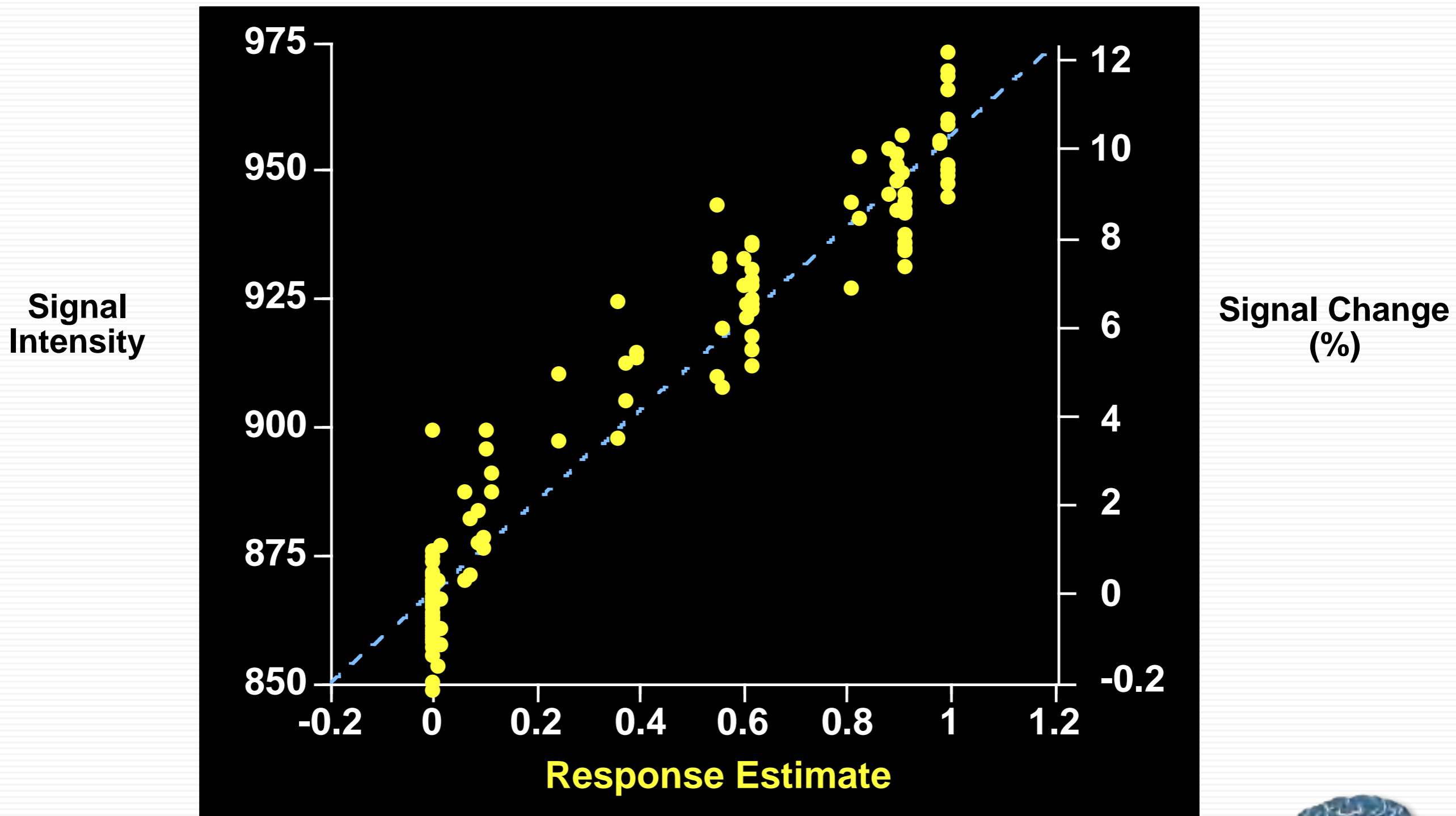
Extrastriate activation



Amplitude-weighted Linear Estimate



Estimated vs. Actual *f*MRI Response



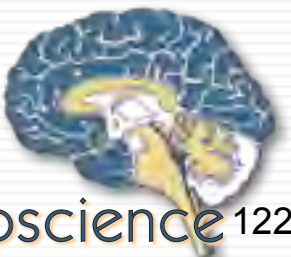
The Plan

- The Magnetic Resonance Phenomenon & Contrast (30)
- Spatial Encoding (26)
- The “Pulse Sequence” Rules Everything (3)

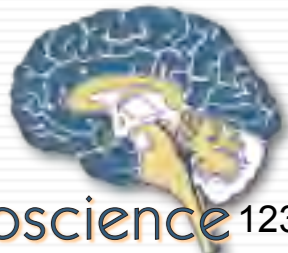
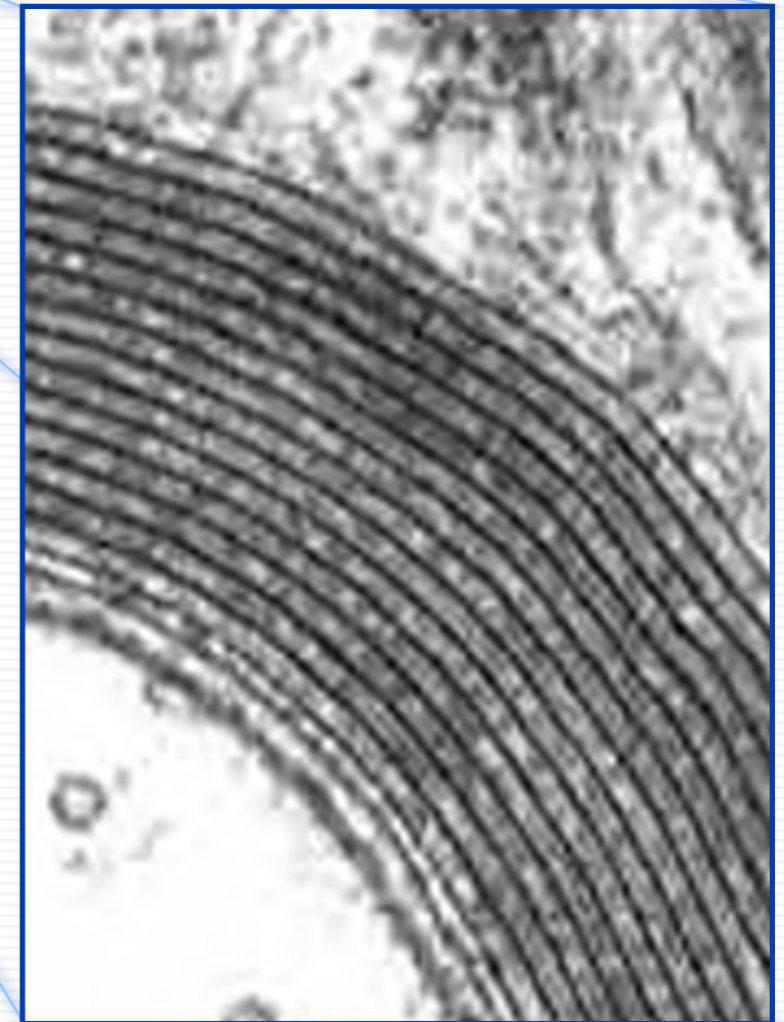
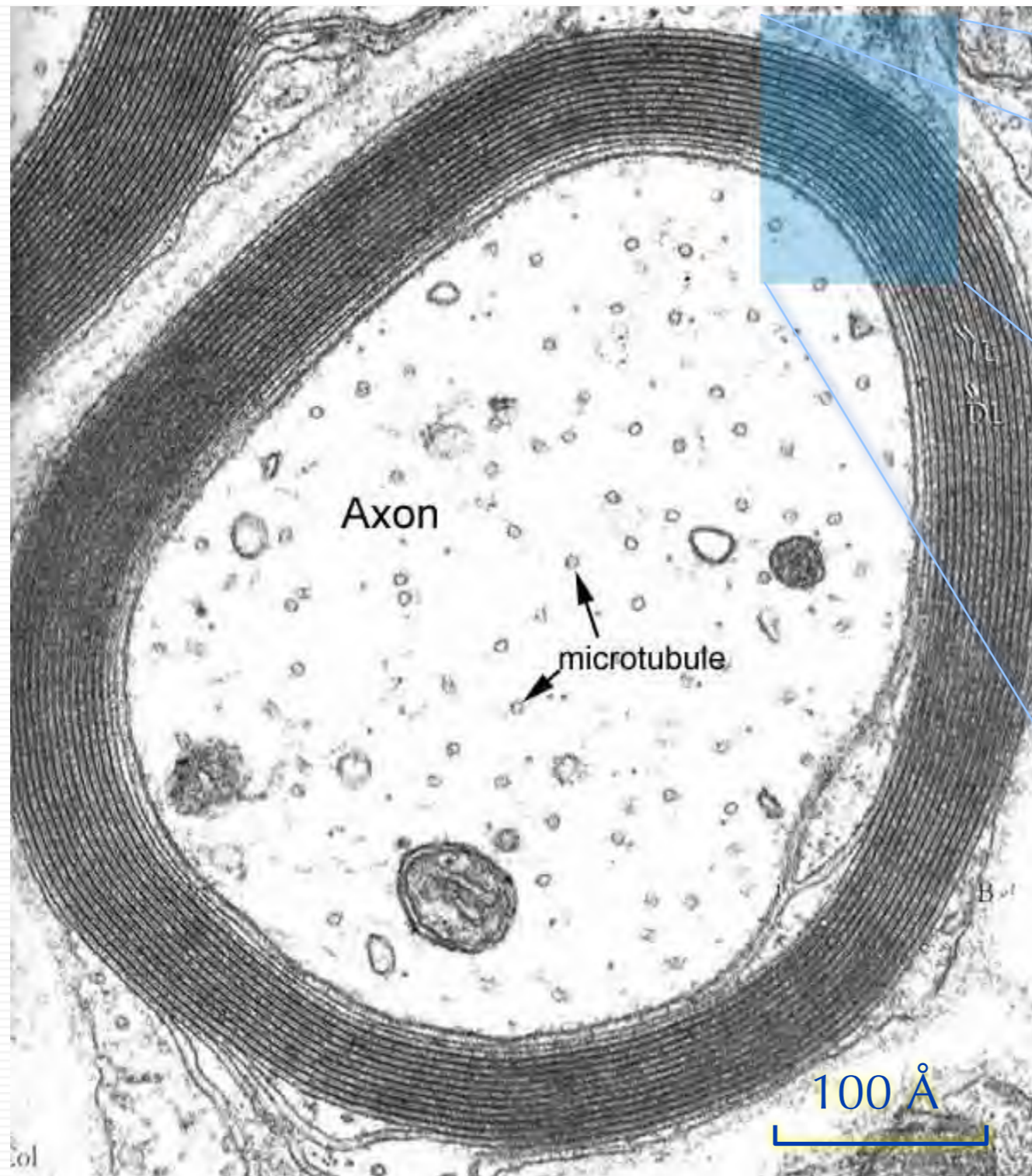
Seventh Inning Stretch

- Fast Imaging (14)
- Functional MRI (18)
- Diffusion and Summary (9)

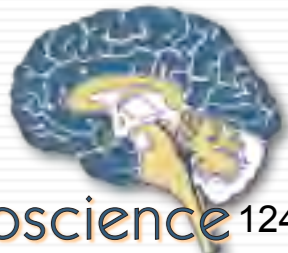
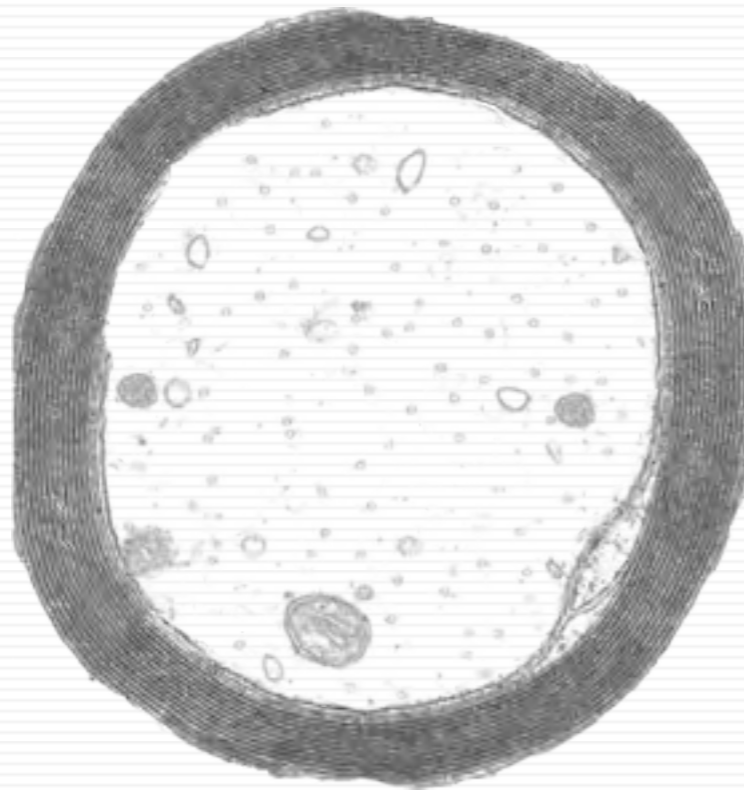
- Image Quality and Artifacts (48)



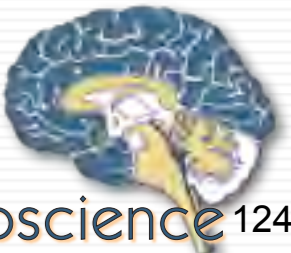
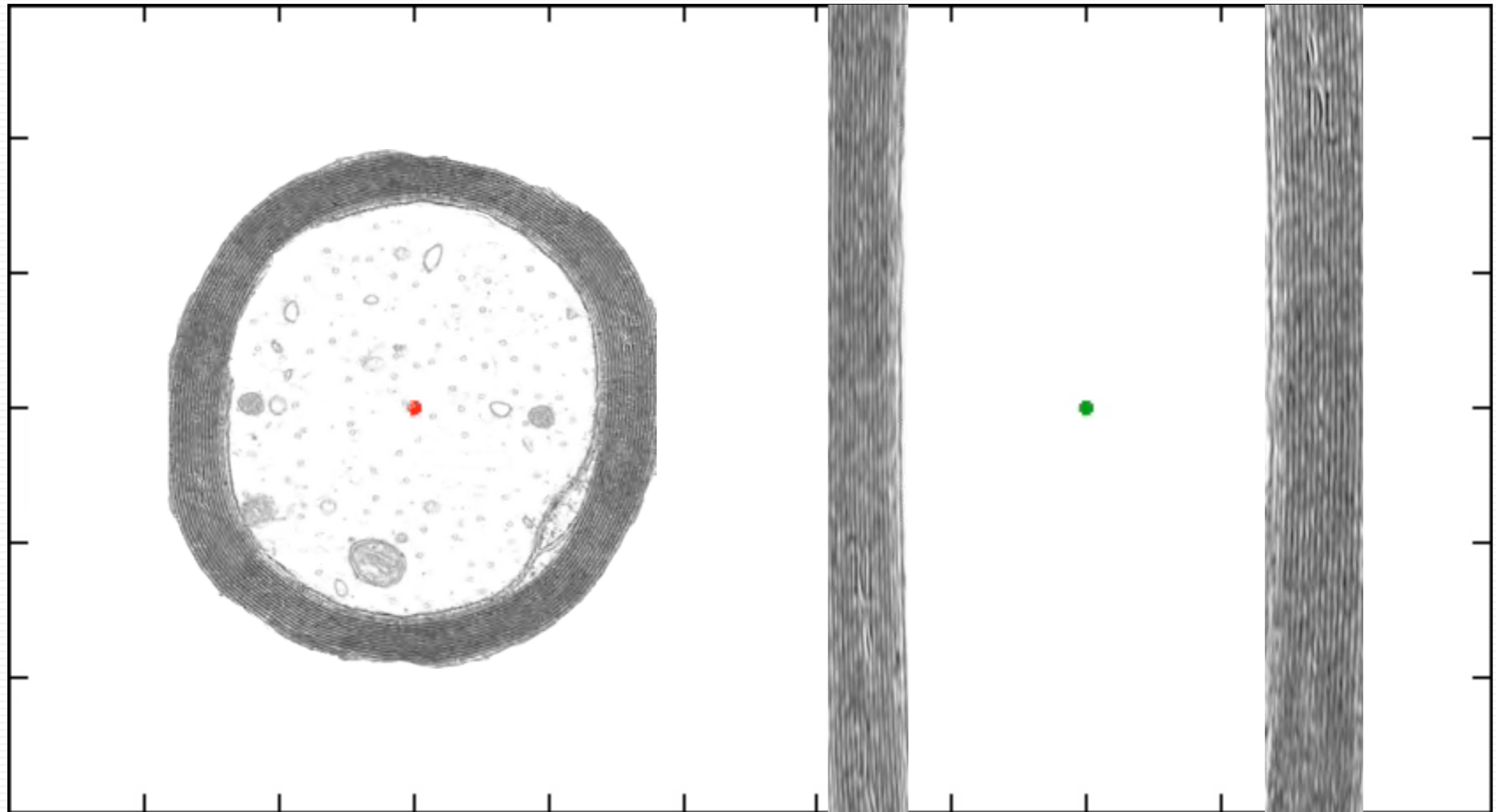
Myelin Sheath



Isotropic vs. Anisotropic Diffusion

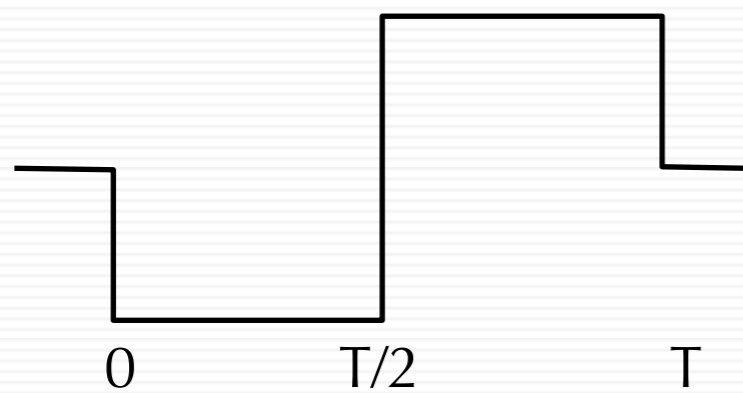


Isotropic vs. Anisotropic Diffusion



Motion Effects on Phase

- Relative Phase is the product $\gamma B t$ (cycles/sec)/Tesla * Tesla * sec
- Motion causes additional phase shifts:

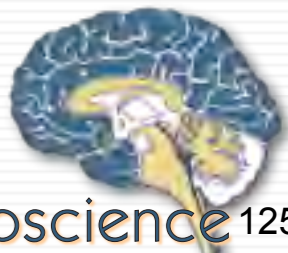
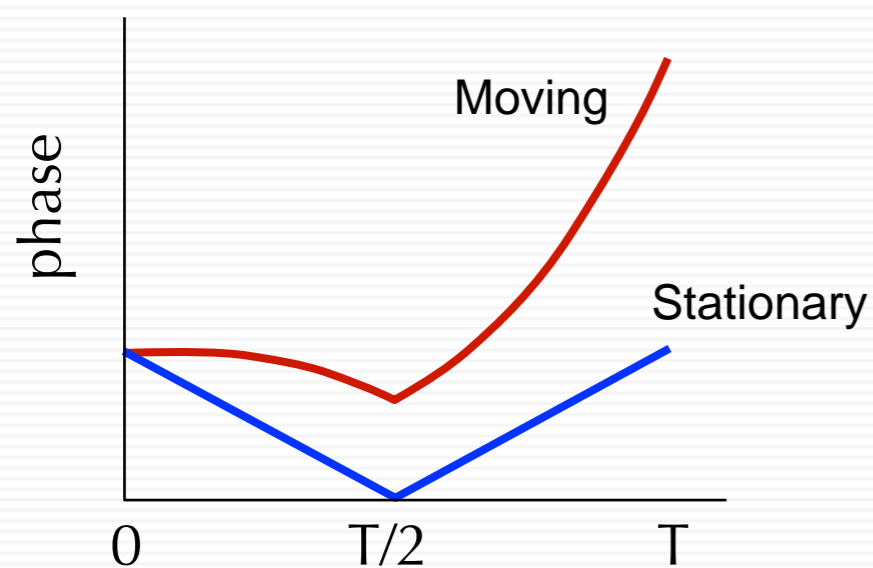


$$x(t) = x_0 + vt + \frac{at^2}{2} + \dots$$

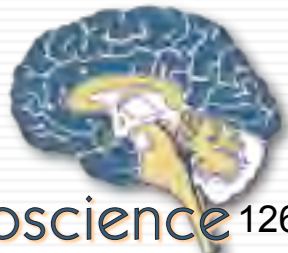
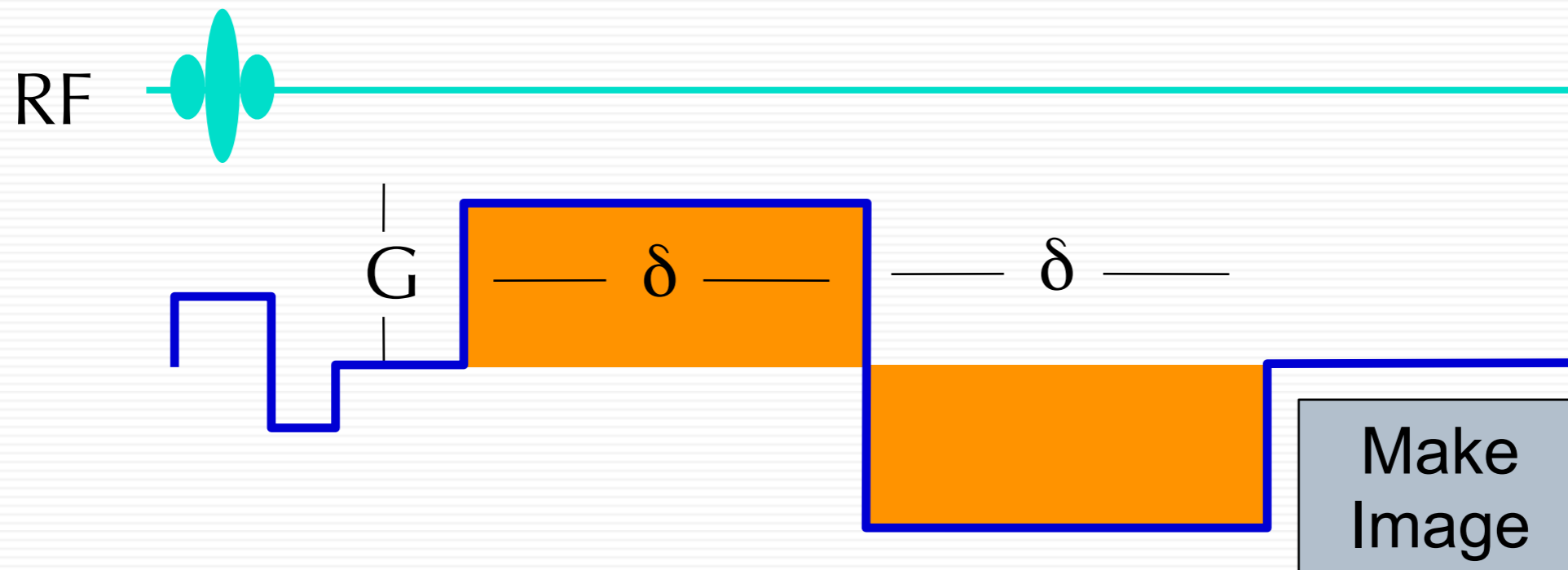
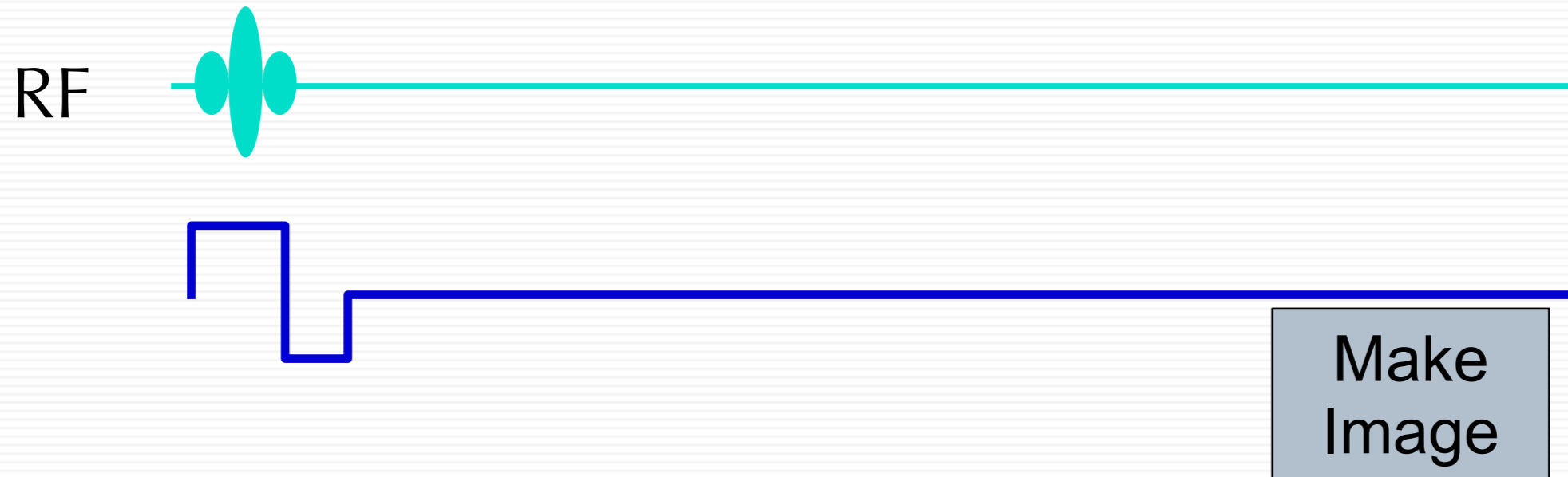
$$\varphi = \gamma \int_0^T G(t)x(t)dt$$

$$= \gamma \int_0^T G(t)[x_0 + vt + \frac{at^2}{2} + \dots]dt$$

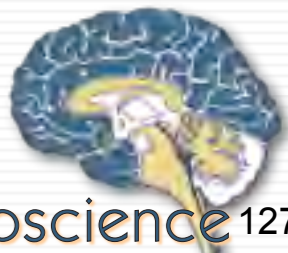
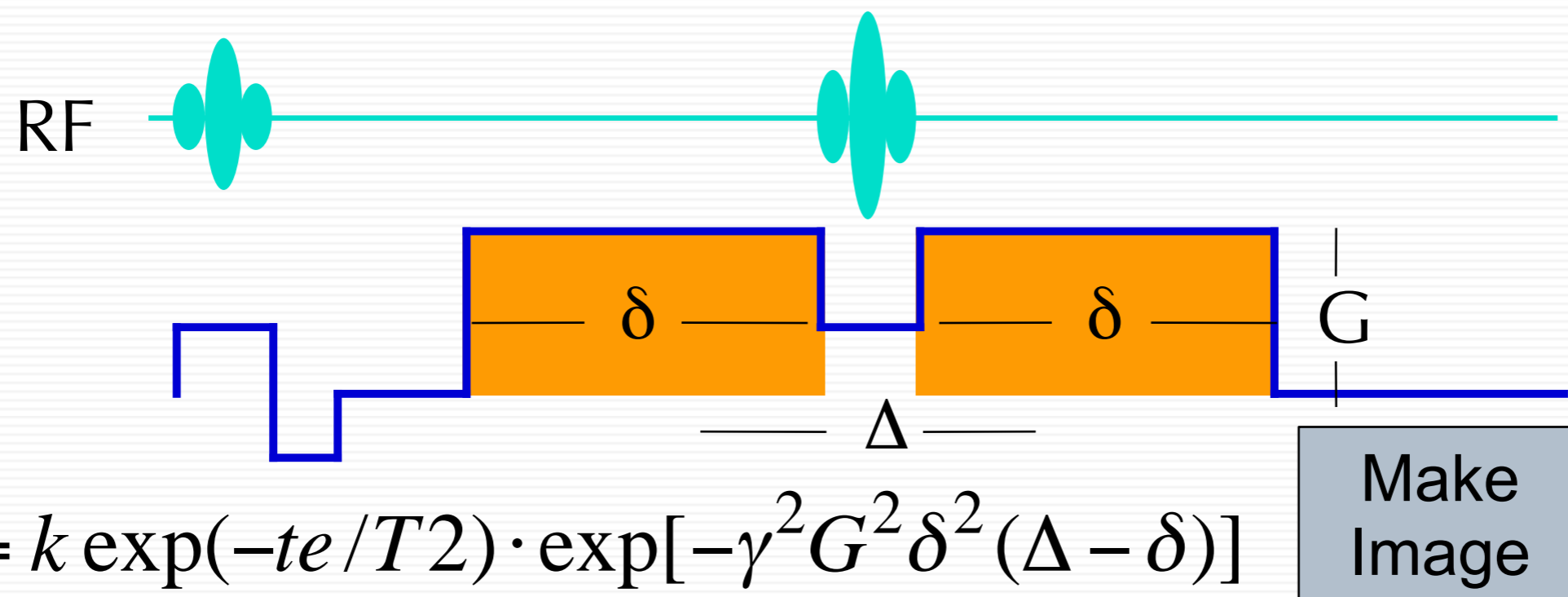
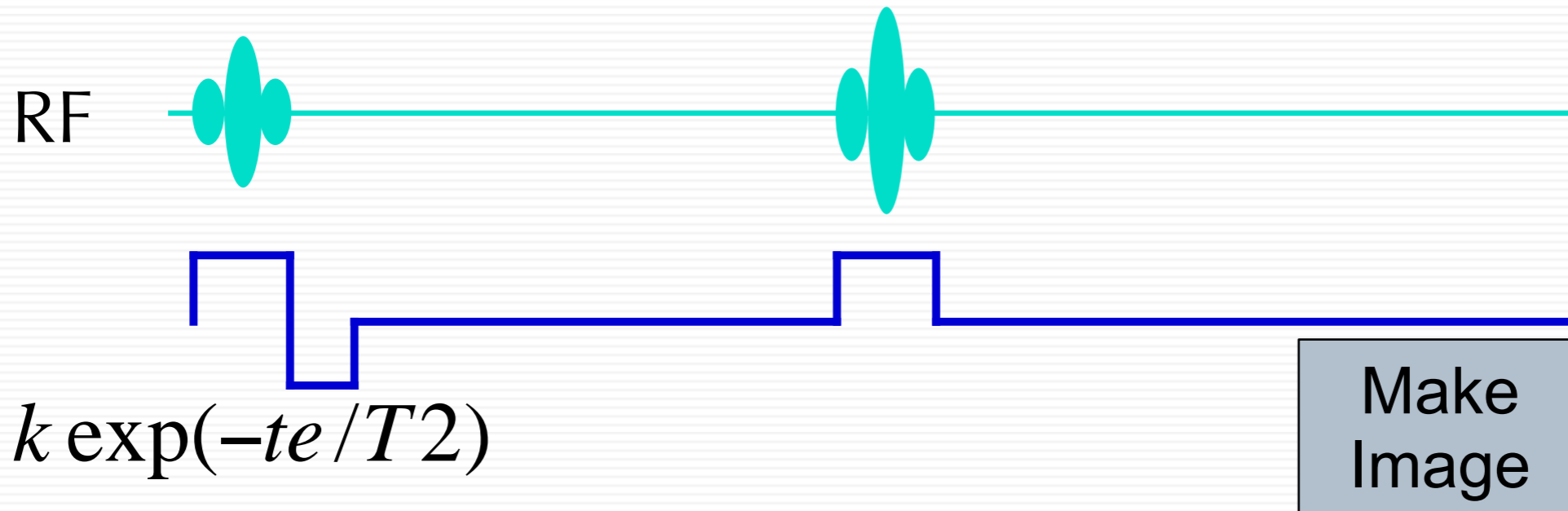
$$= \gamma \left[\frac{vT^2}{4} + \frac{23aT^3}{24} + \dots \right]$$



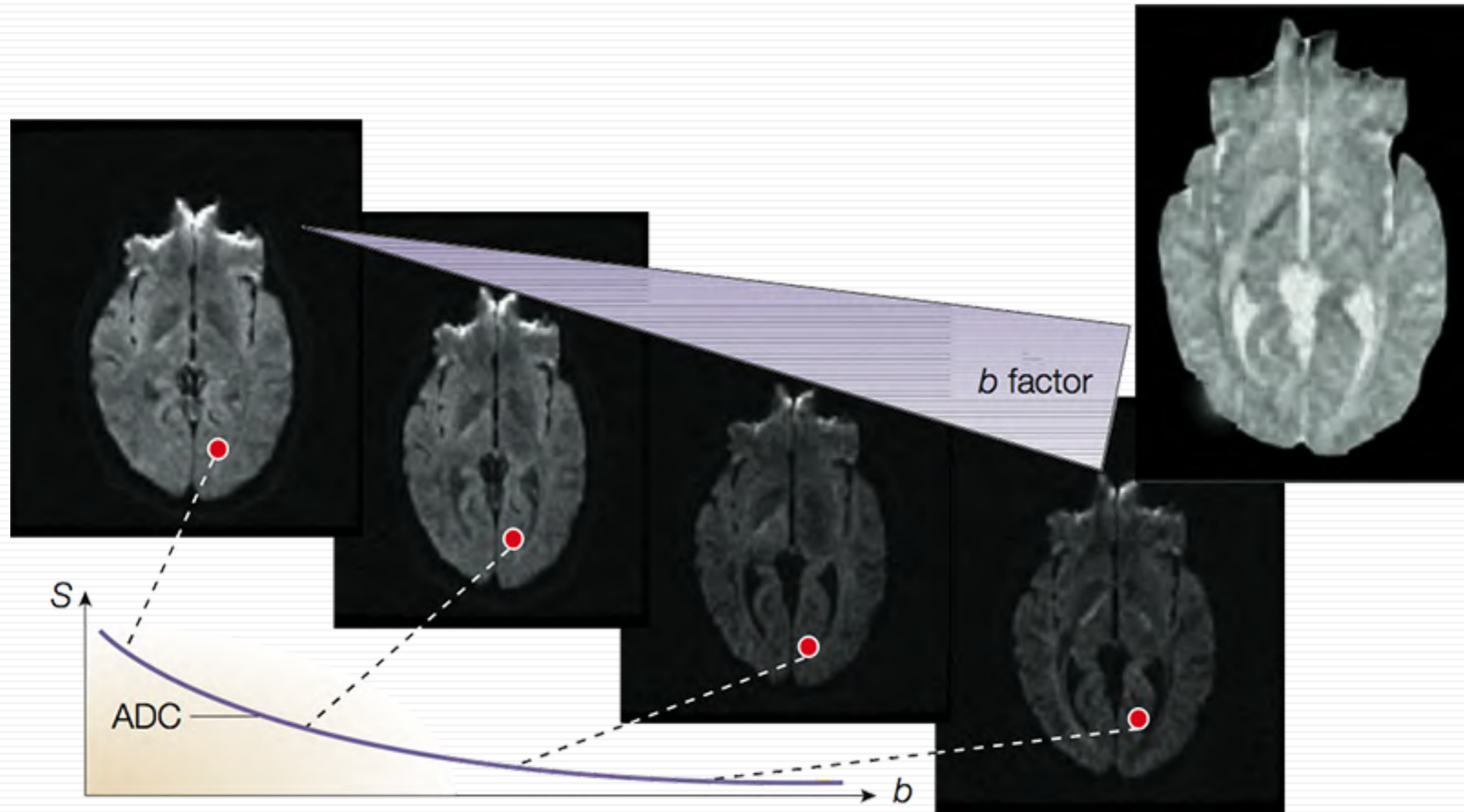
Diffusion Gradients and Signal



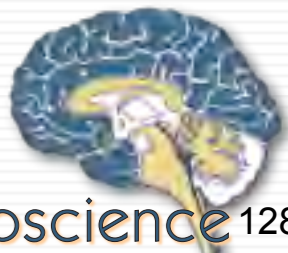
Diffusion Gradients and Signal



Diffusion Attenuates MR Signal

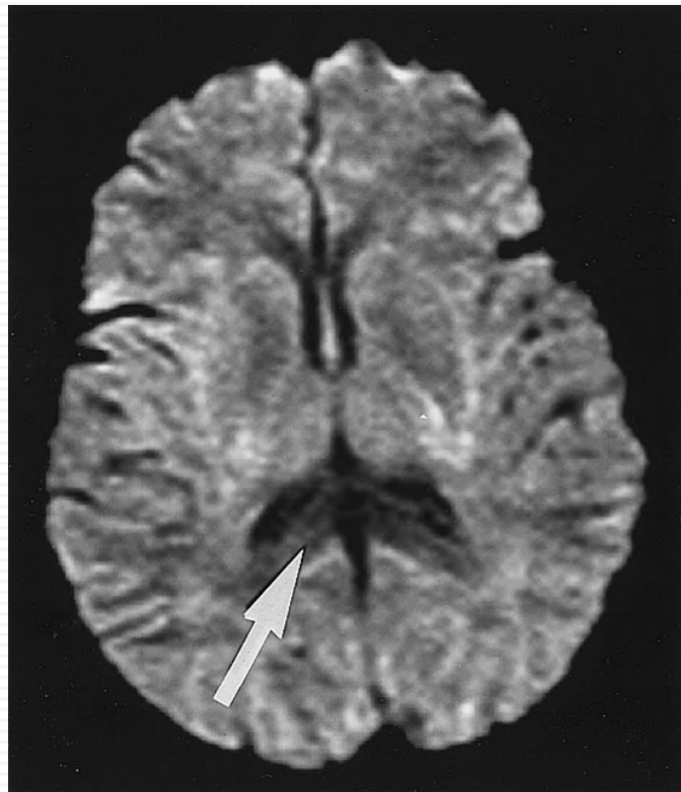


Denis Le Bihan, Nature Reviews in Neuroscience 4:469, 2003

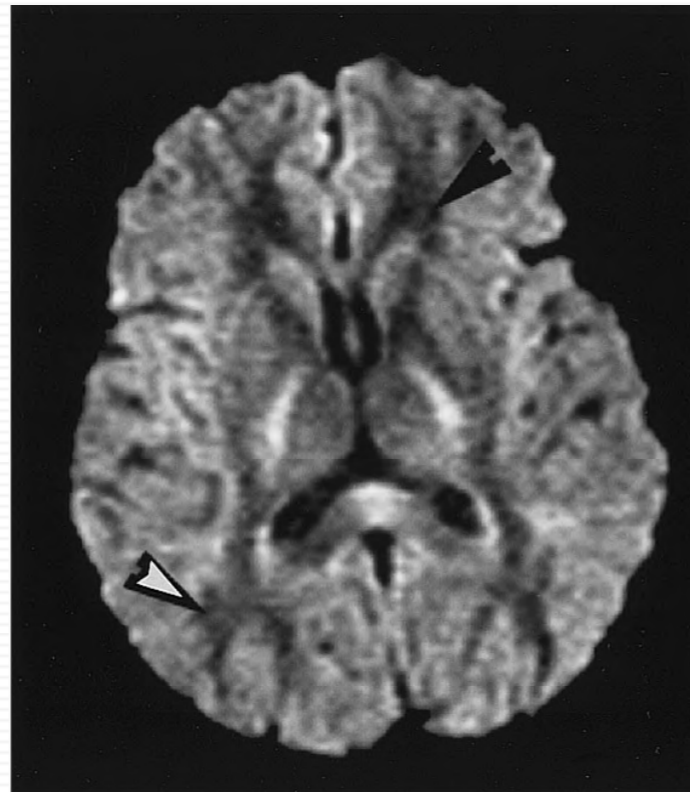


Brain Diffusion is Anisotropic

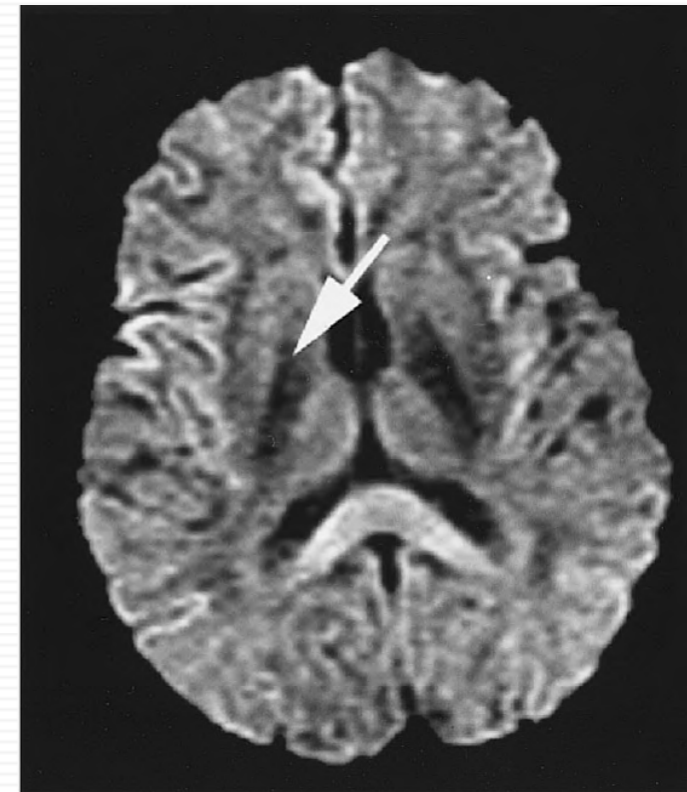
Radiology



Gx

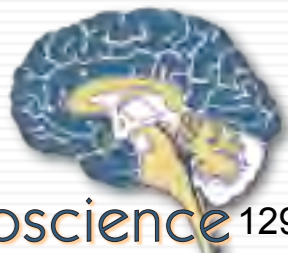


Gy

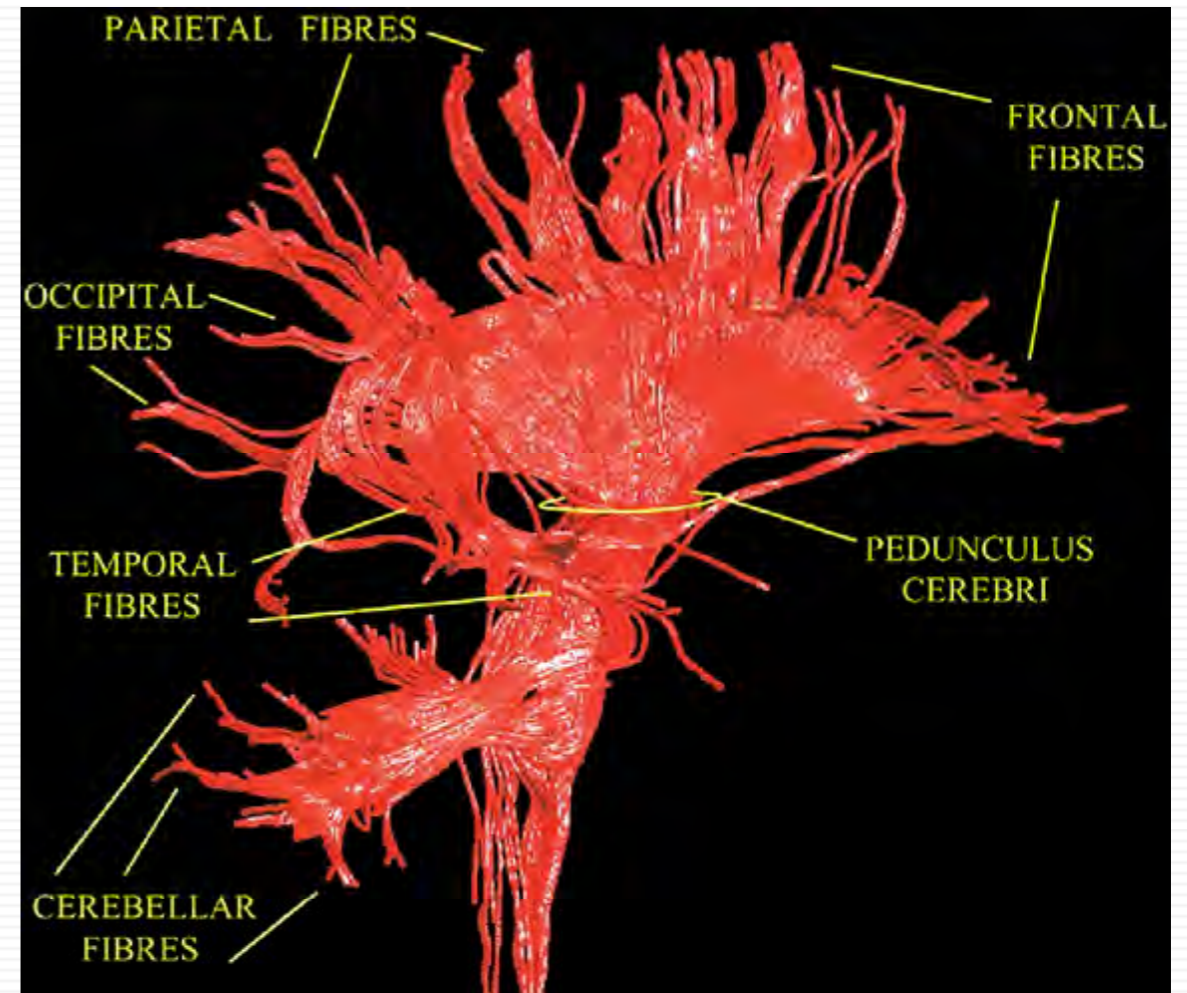
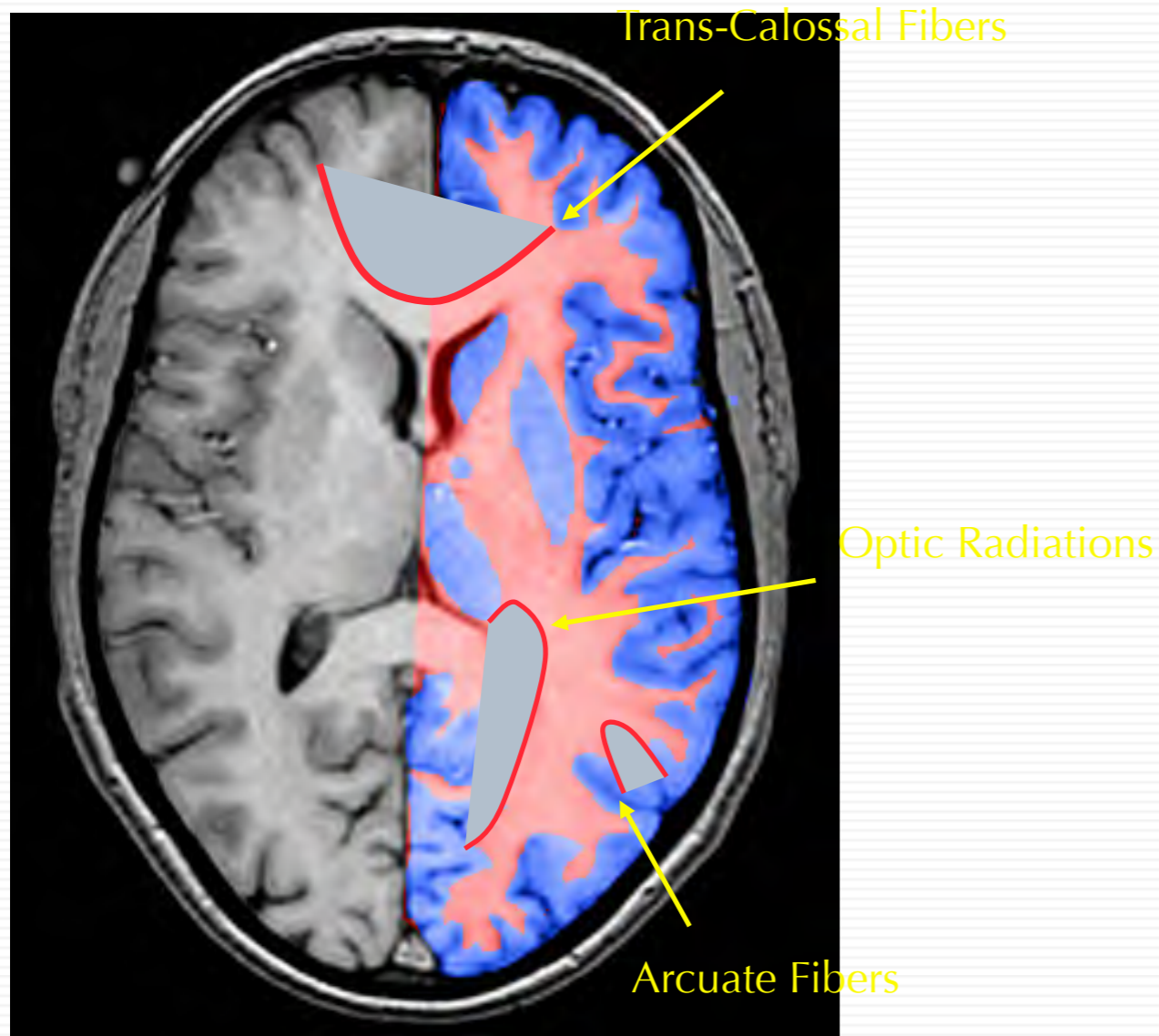


Gz

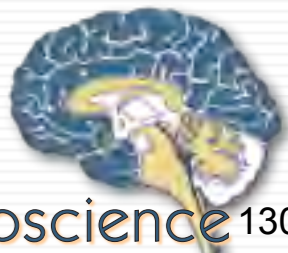
Schaefer, P. W. et al. Radiology 2000;217:331-345



White and Gray Matter

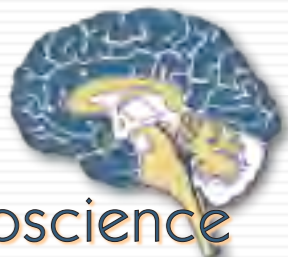


After: Catani, et al., *NeuroImage* 17:77, 2002

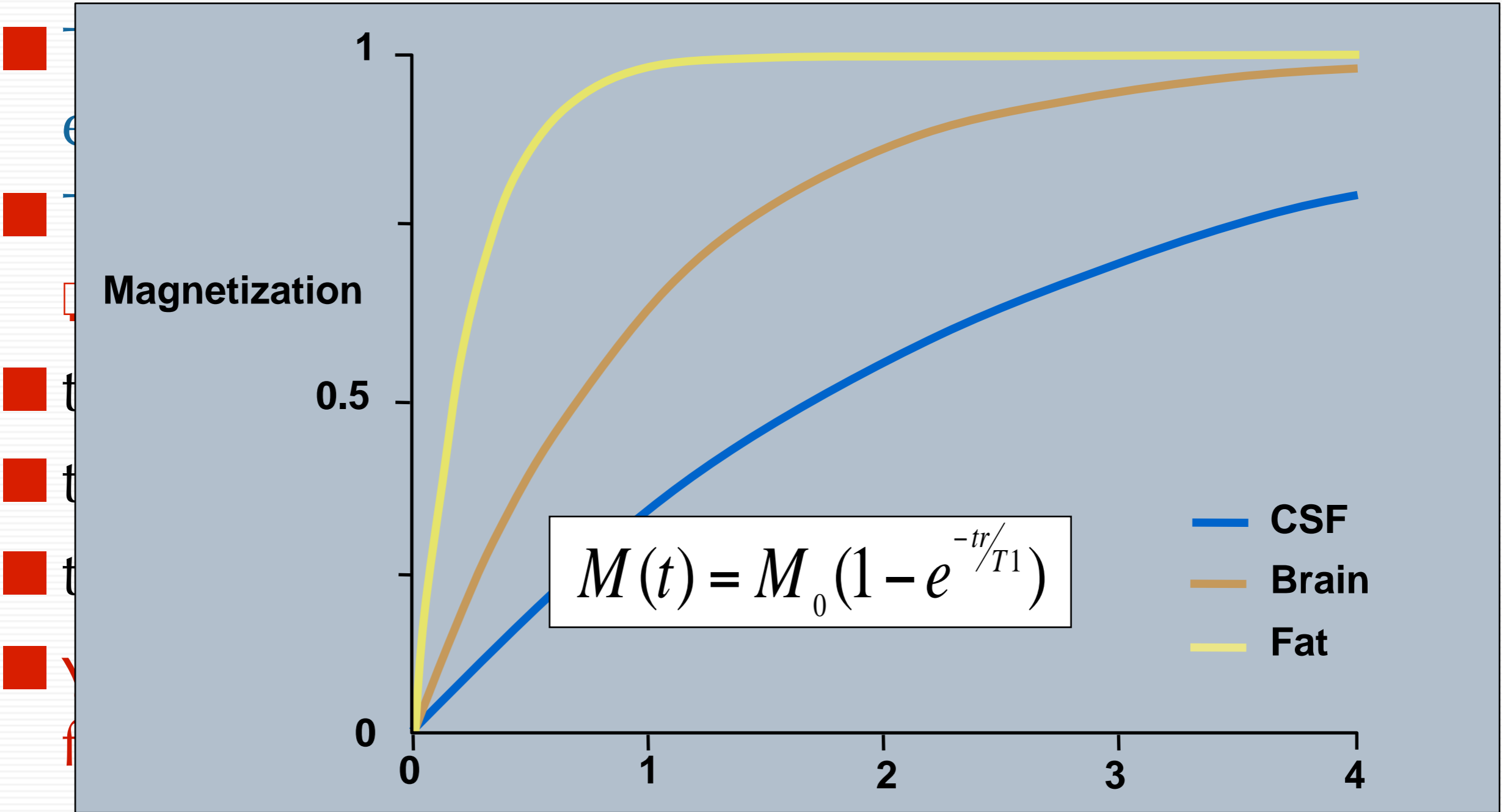


Crib Sheet

- T1 - Longitudinal Relaxation Rate (reaching equilibrium)
- T2 - Transverse Relaxation Rate (dephasing)
 - T2* - observed T2 decay, made up of T2, T2', T2D, etc...
- tr - Repetition time between excitation pulses
- te - Time after excitation before forming images
- ti - Time between inversion and excitation
- γ - Gyromagnetic ratio - proportionality of field and frequency
- B0 - Static Magnetic Field
- B1 - Rotating Magnetic Field



Crib Sheet



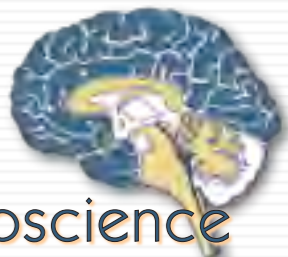
■ B0 - Static Magnetic Field

■ B1 - Rotating Magnetic Field



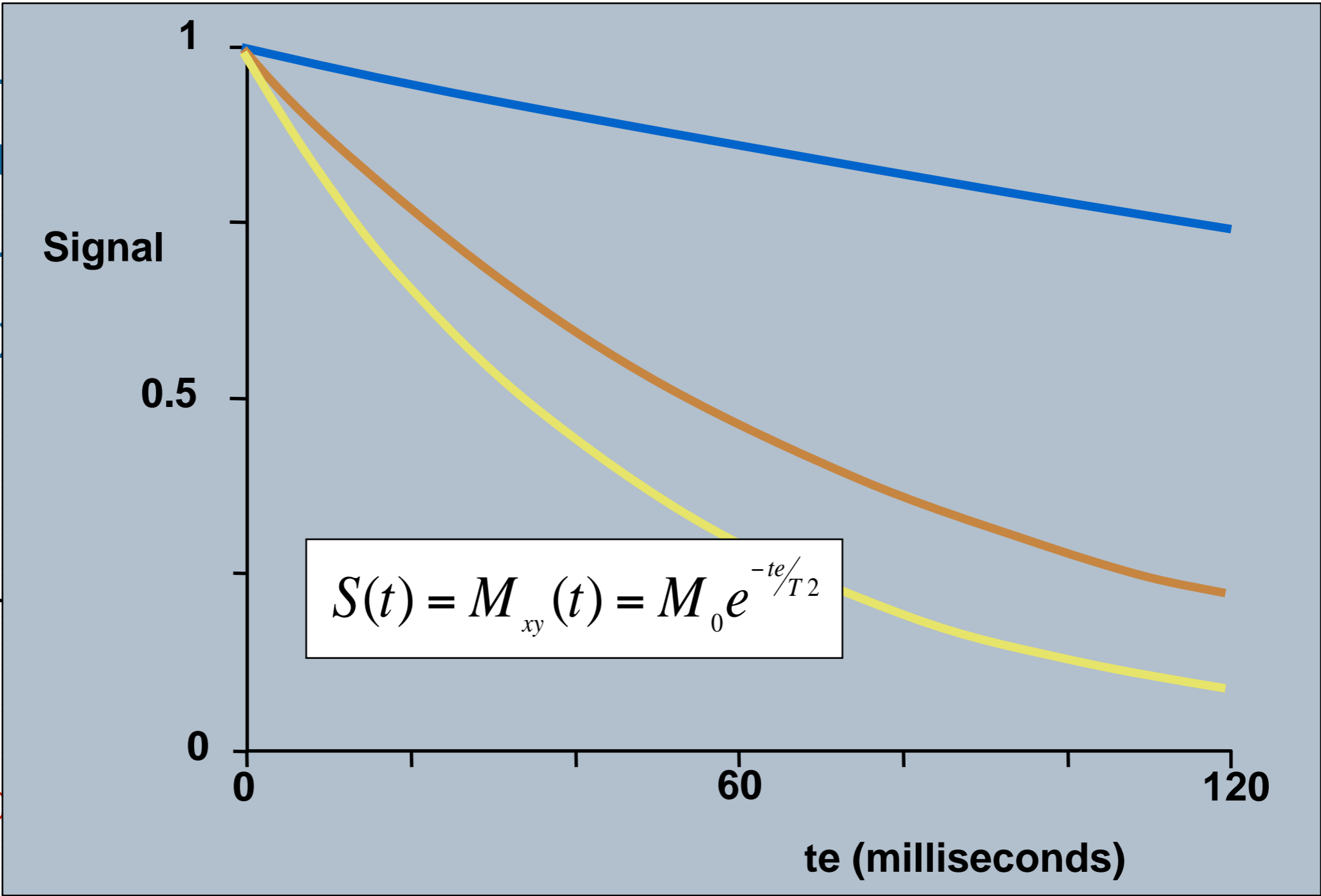
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Crib Sheet

- T1 -
- equ
- T2 -
- T2*
- tr -
- te -
- ti -
- γ -
- freq



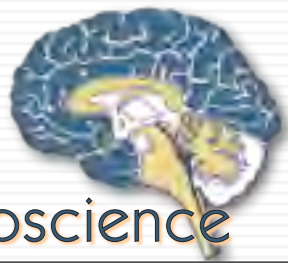
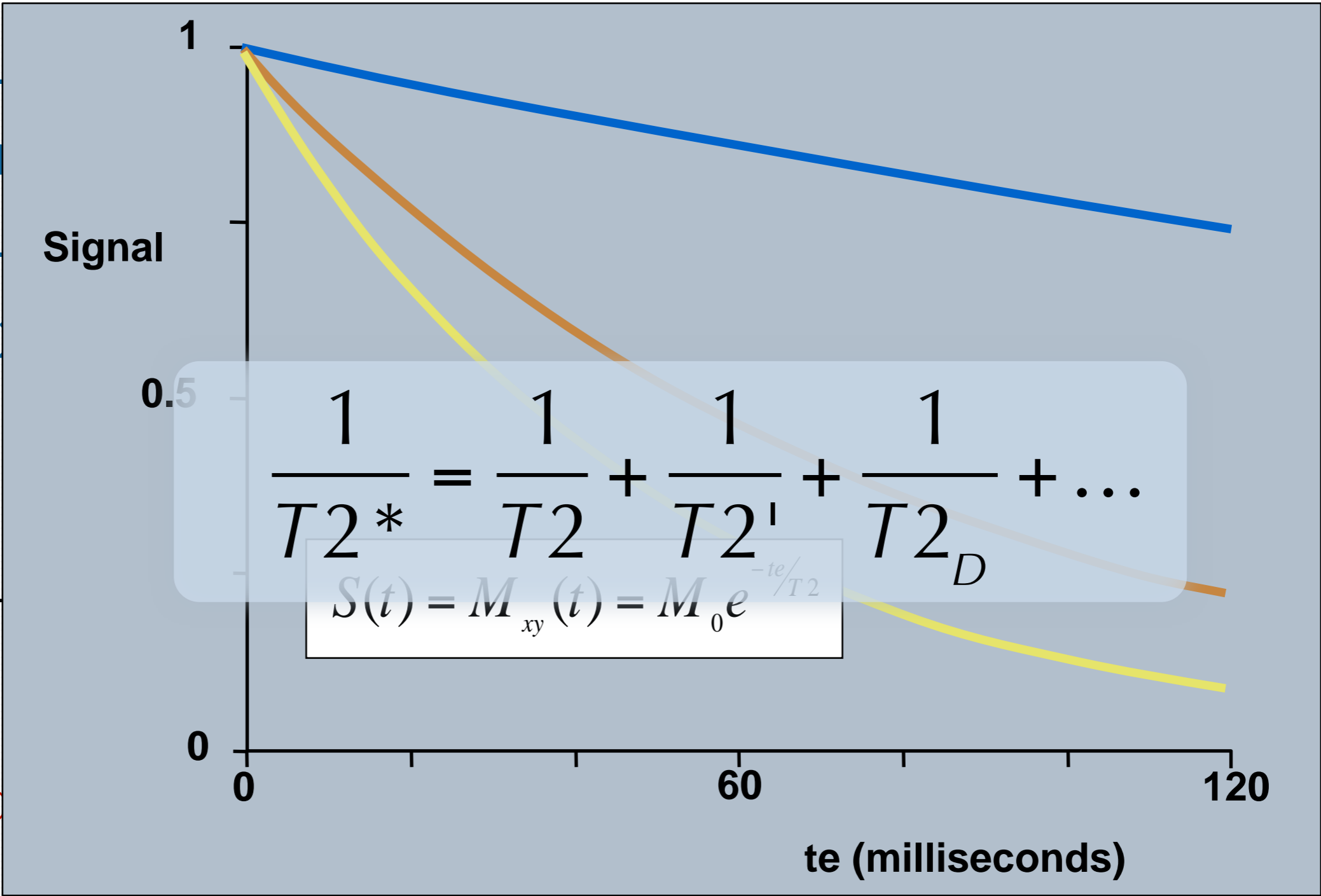
■ B0 - static magnetic field

■ B1 - Rotating Magnetic Field



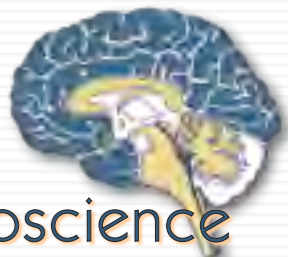
Crib Sheet

- T1 - longitudinal relaxation time
- T2 - transverse relaxation time
- T2* - effective transverse relaxation time
- tr - repetition time
- te - echo time
- ti - inversion time
- γ - gyromagnetic ratio
- freq - frequency
- B0 - static magnetic field
- B1 - Rotating Magnetic Field



Crib Sheet

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Crib Sheet

■ T1 - L
equili

■ T2 - T

□ T2*

■ tr - Re

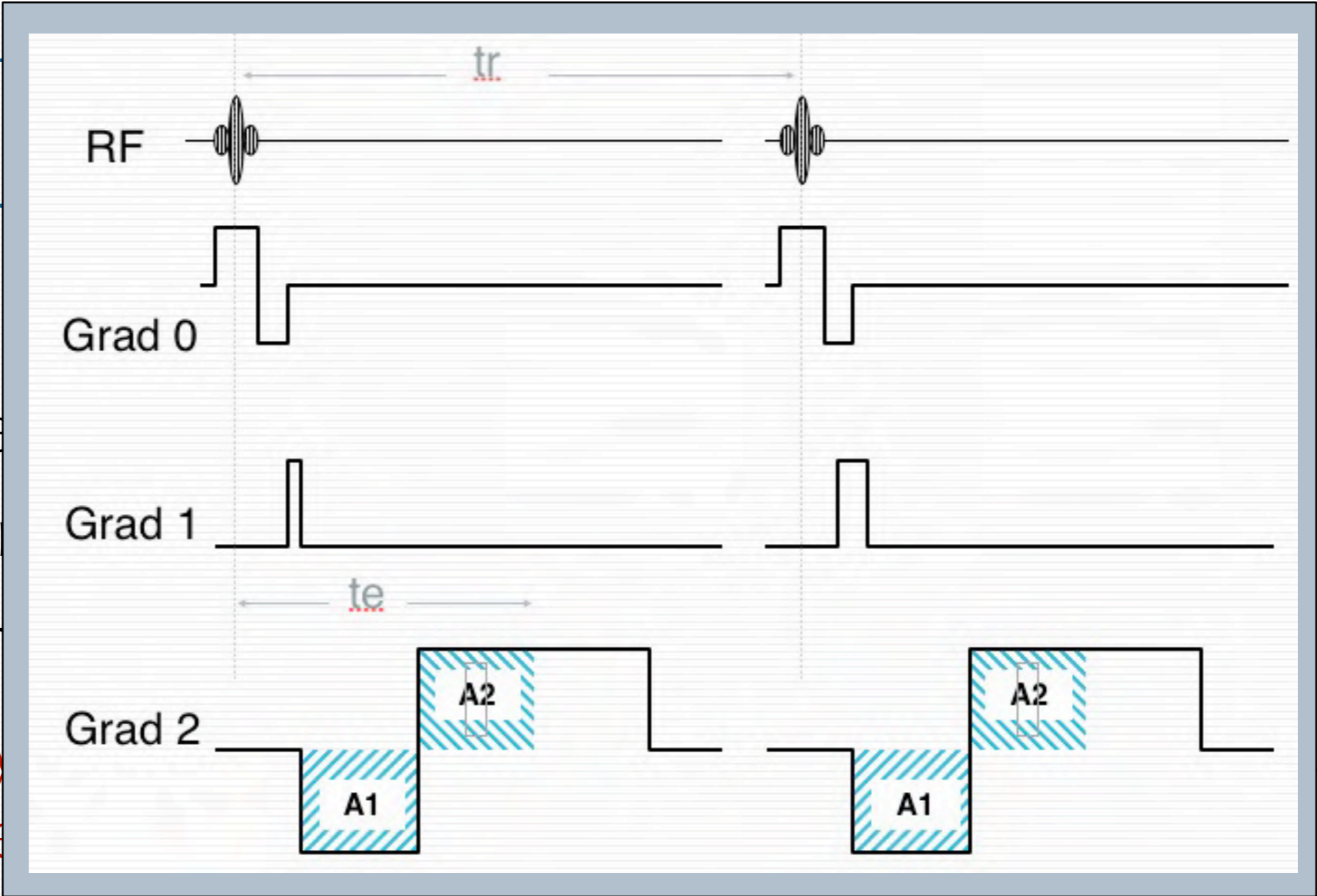
■ te - Ti

■ ti - Tir

■ γ - Gy
freque

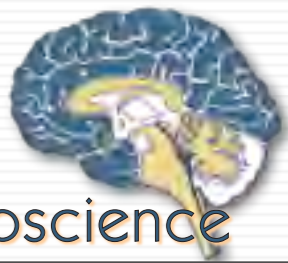
■ B0 - Static Magnetic Field

■ B1 - Rotating Magnetic Field



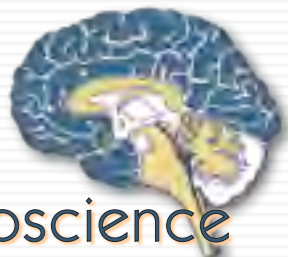
tc...

nd



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Crib Sheet

■ T1

equ

■ T2

□ T

■ tr -

■ te -

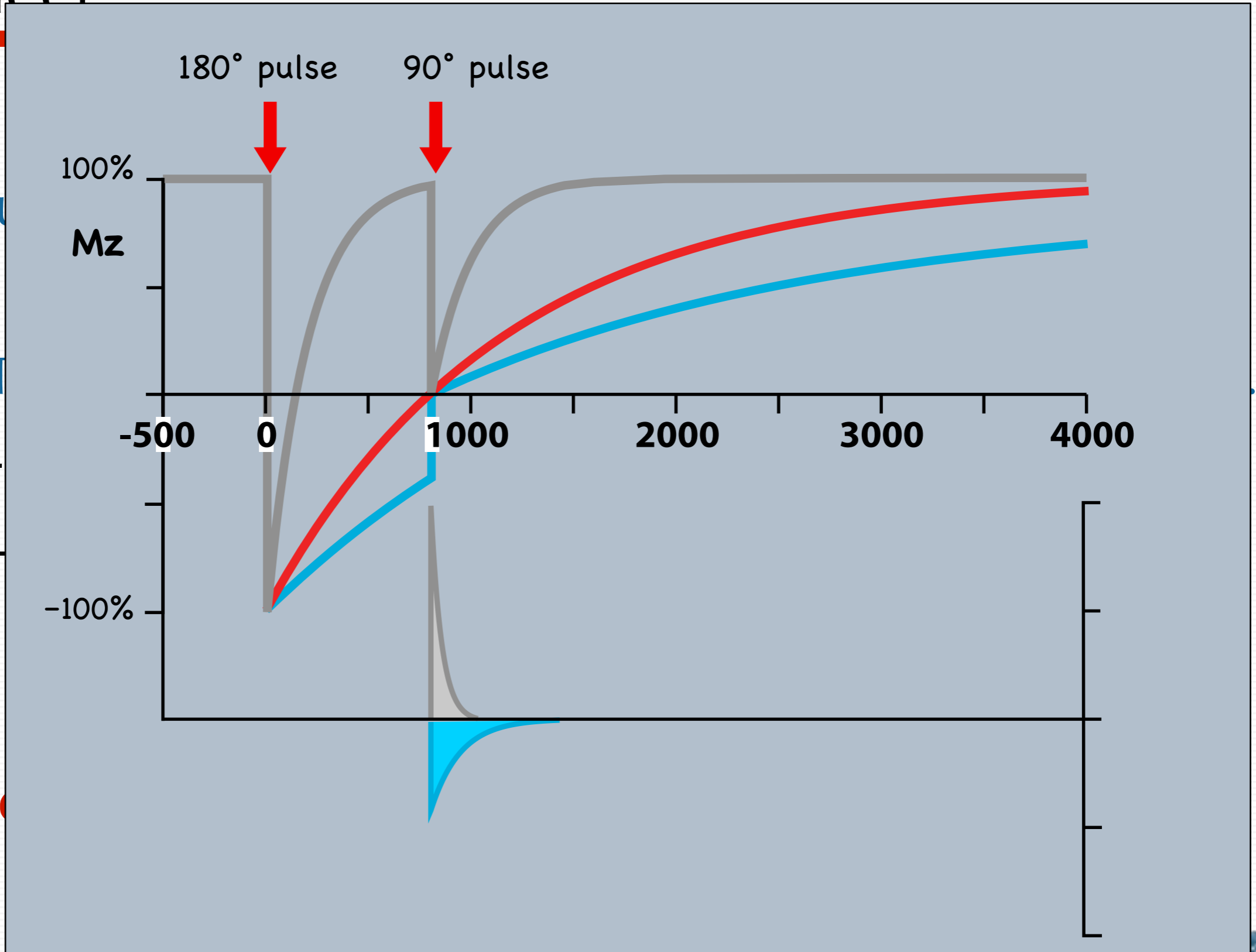
■ ti -

■ γ -

freq

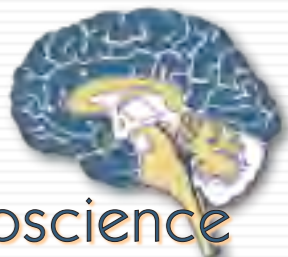
■ B0

■ B1 - Rotating Magnetic Field



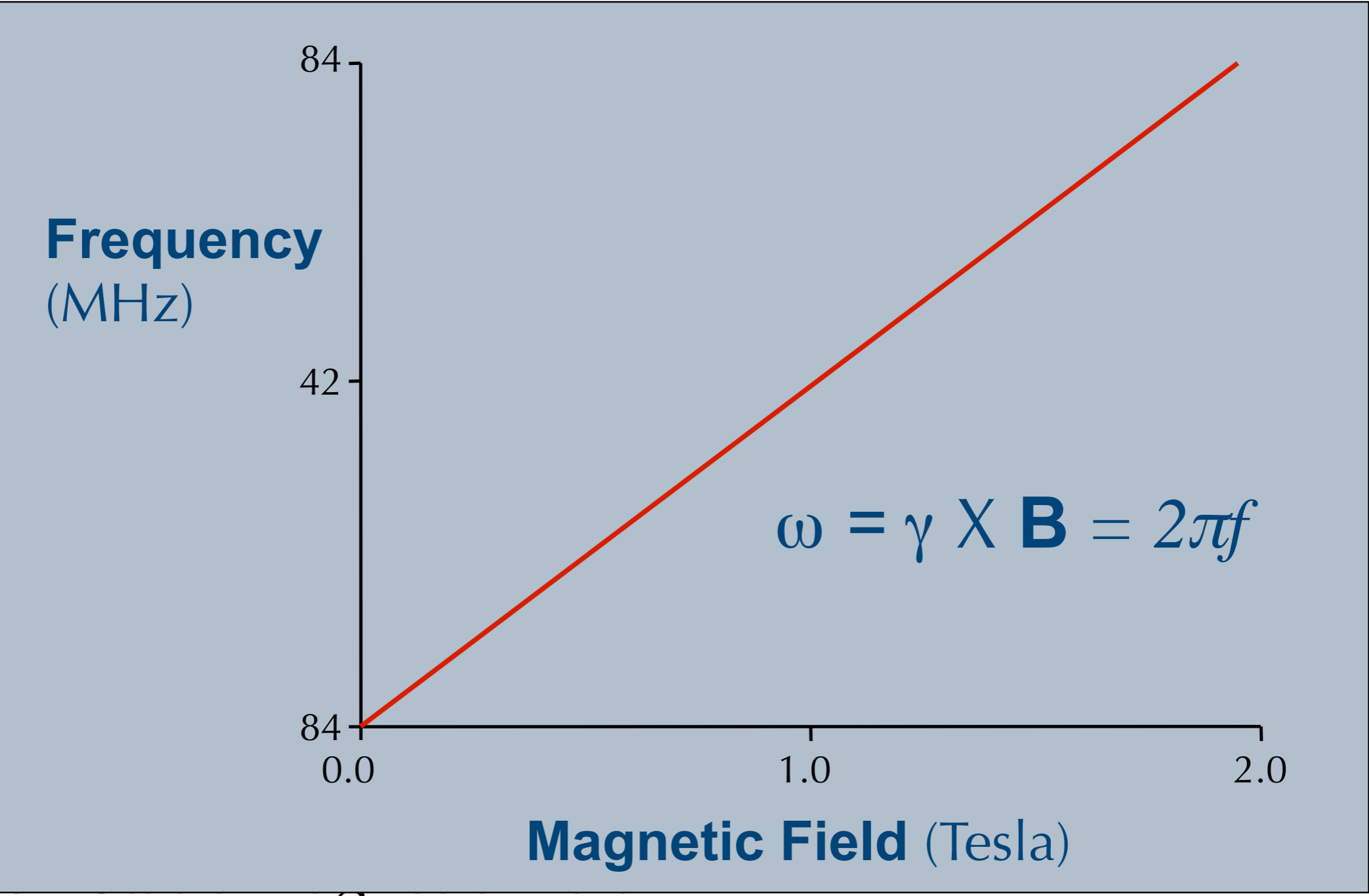
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Crib Sheet

- T
- e
- T
-
- tr
- te
- ti
- γ
- fr
- B

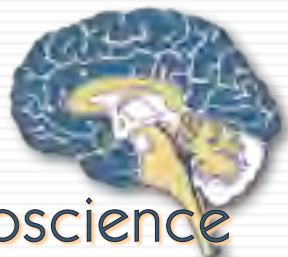


■ B1 - Rotating Magnetic Field



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- B0 - Static Magnetic Field
- B1 - Rotating Magnetic Field



Crib Sheet

- T1 - Longitudinal Relaxation Rate (reaching

equilib

- T2 - Tra

- T2* -

- tr - Rep

- te - Tim

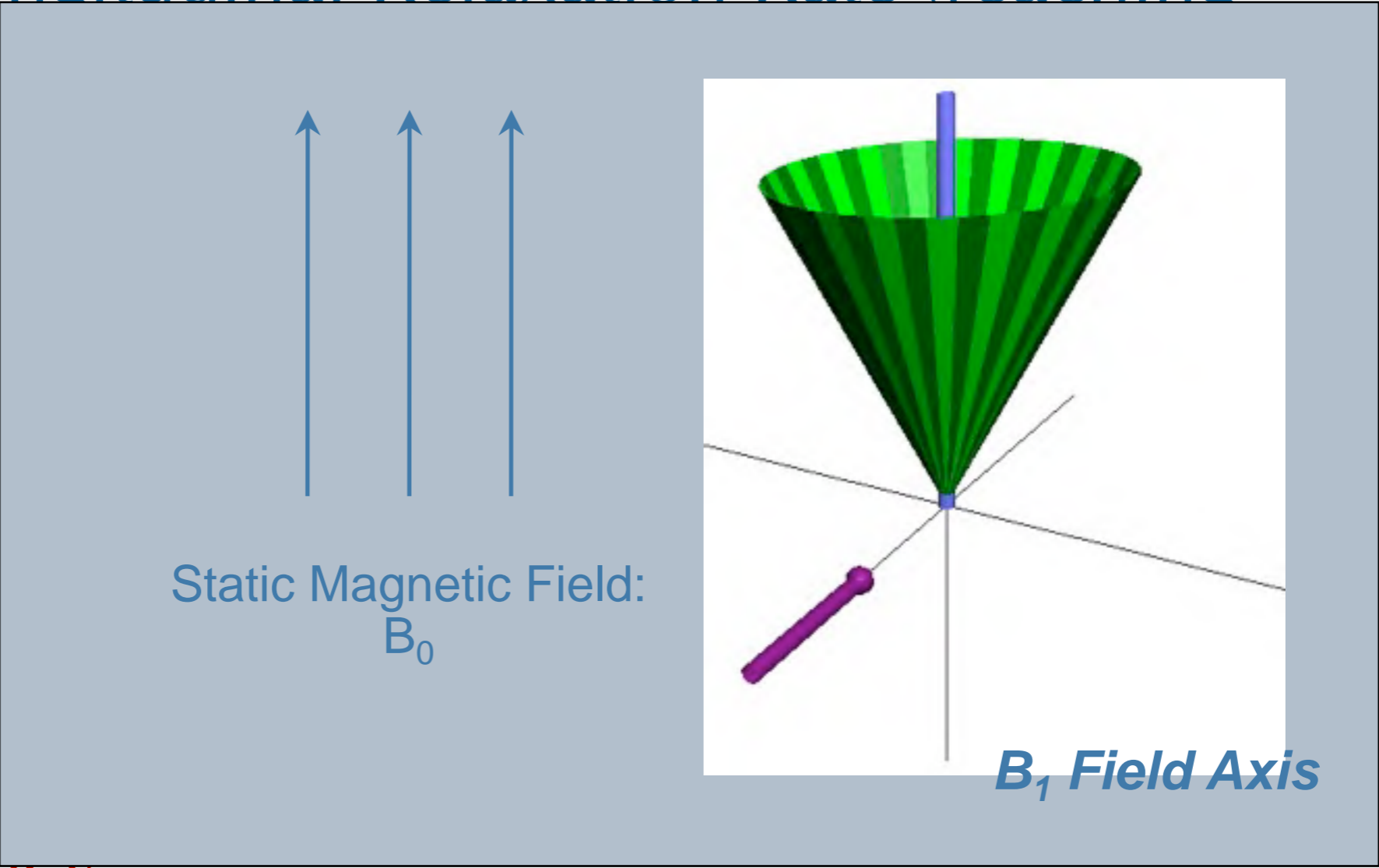
- ti - Tim

- γ - Gyr

frequency

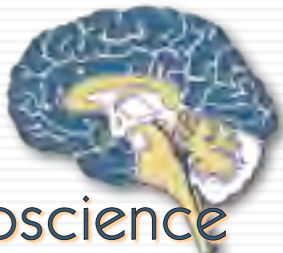
- B0 - Static Magnetic Field

- B1 - Rotating Magnetic Field



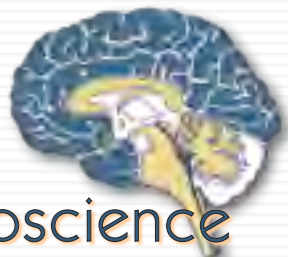
etc...

and



Crib Sheet

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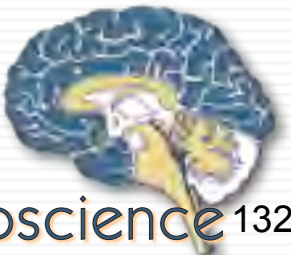
The Plan

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- Functional MRI (18)
- Diffusion and Summary (9)

- Image Quality and Artifacts (48)



An “Equation” in Resolution

Because MR is an emission modality the temporal resolution, spatial resolution and contrast are inter-dependent:

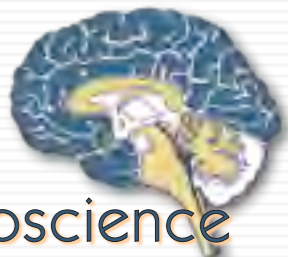
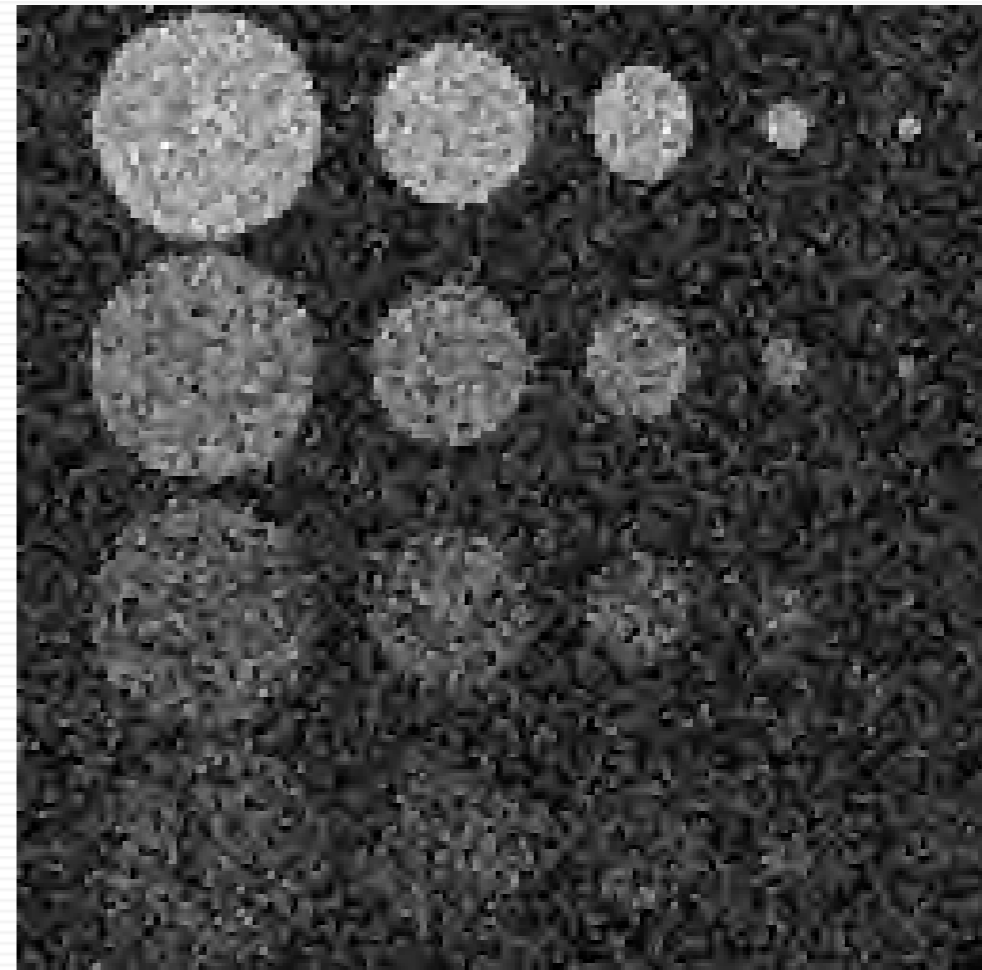
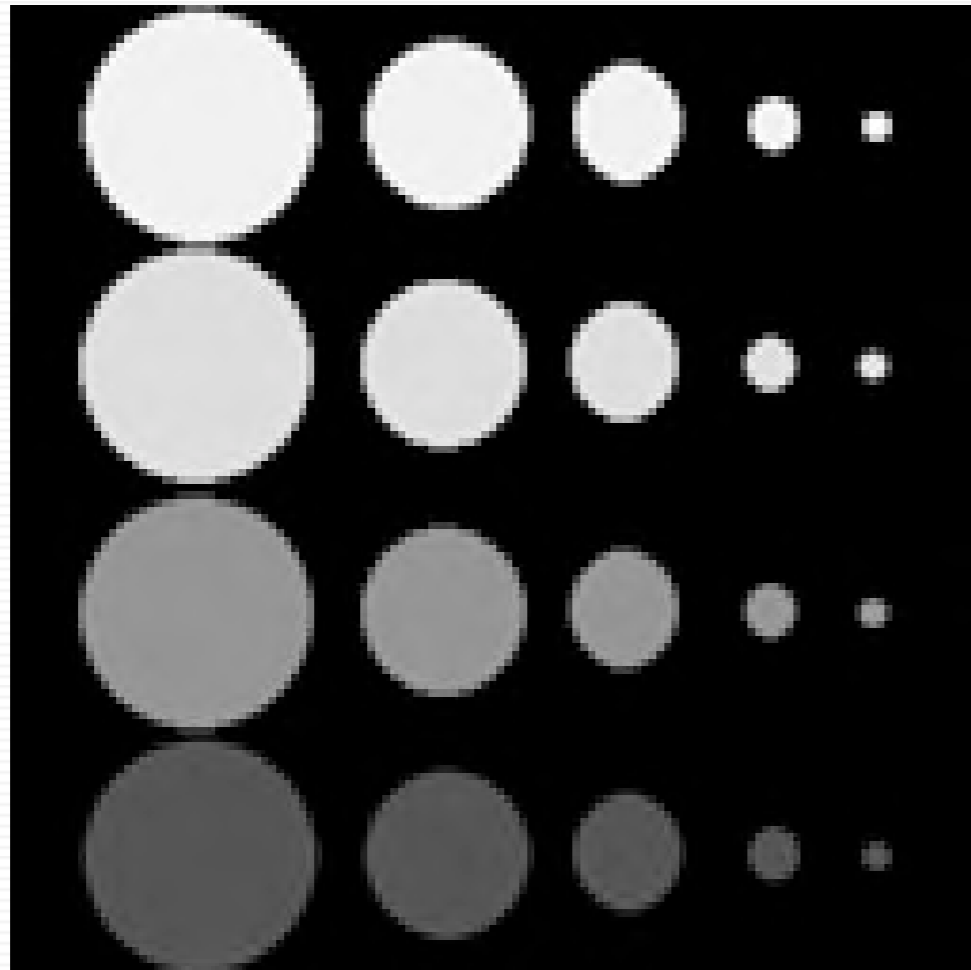
$$\text{Signal} = kB_0(\text{voxel size})\sqrt{\text{imaging time}}$$

–contrast

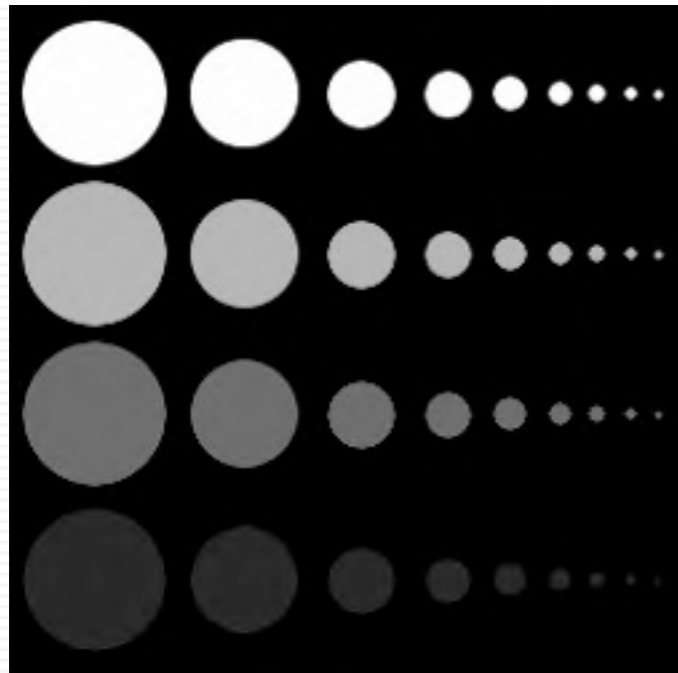
where B_0 is the field strength.



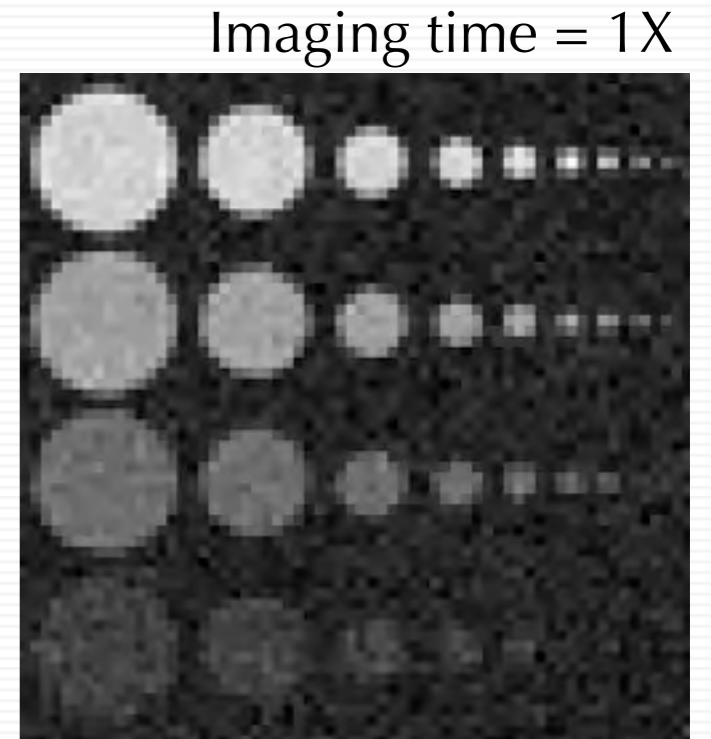
Contrast to Noise Ratio



CNR vs. Resolution

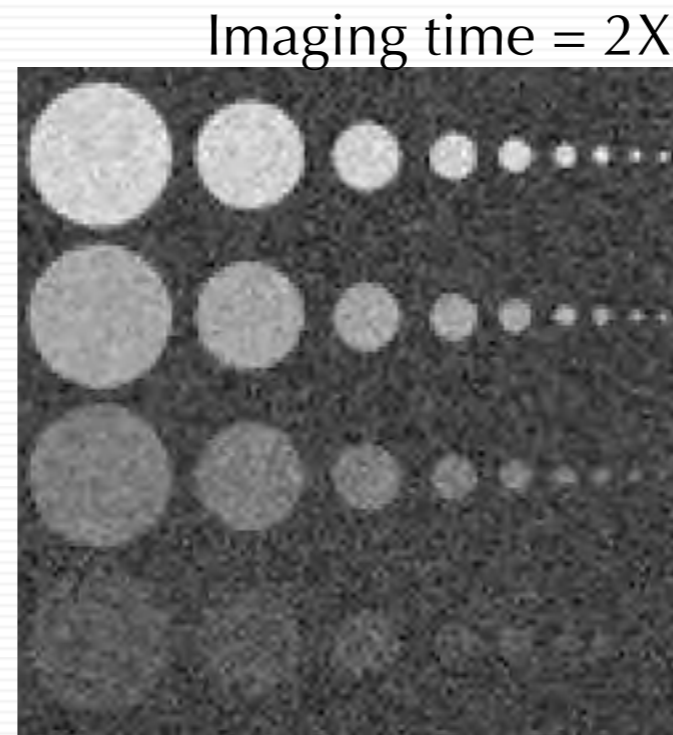


Noise free



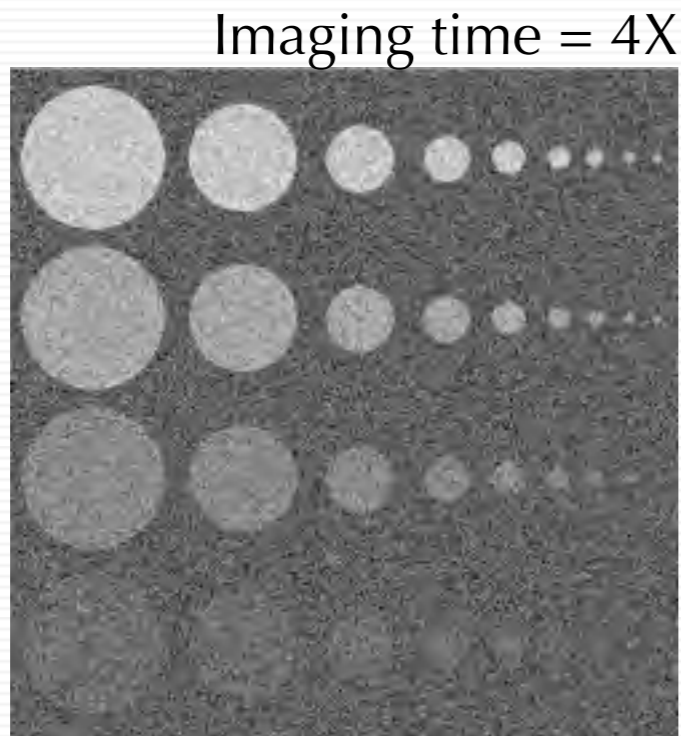
Imaging time = 1X

64 X 64



Imaging time = 2X

128 X 128



Imaging time = 4X

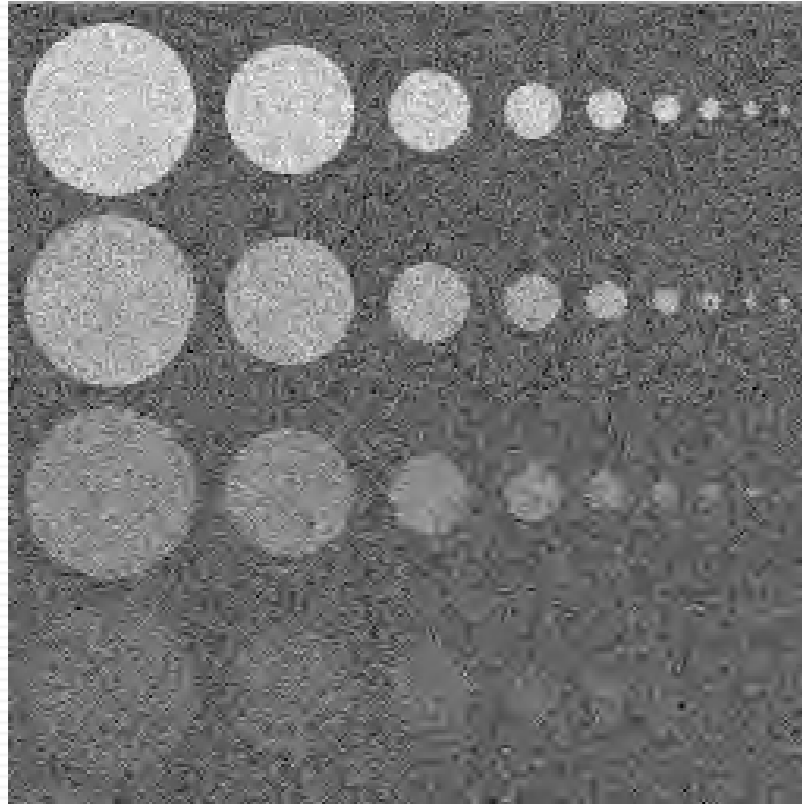
256 X 256

Minimum Imaging Time



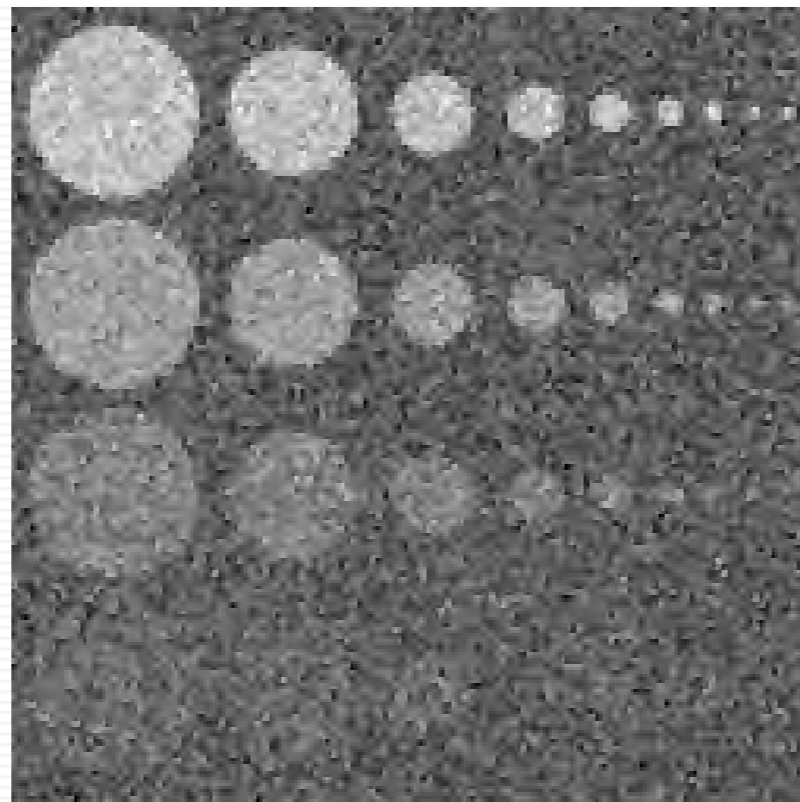
CNR vs. Resolution

256 X 256

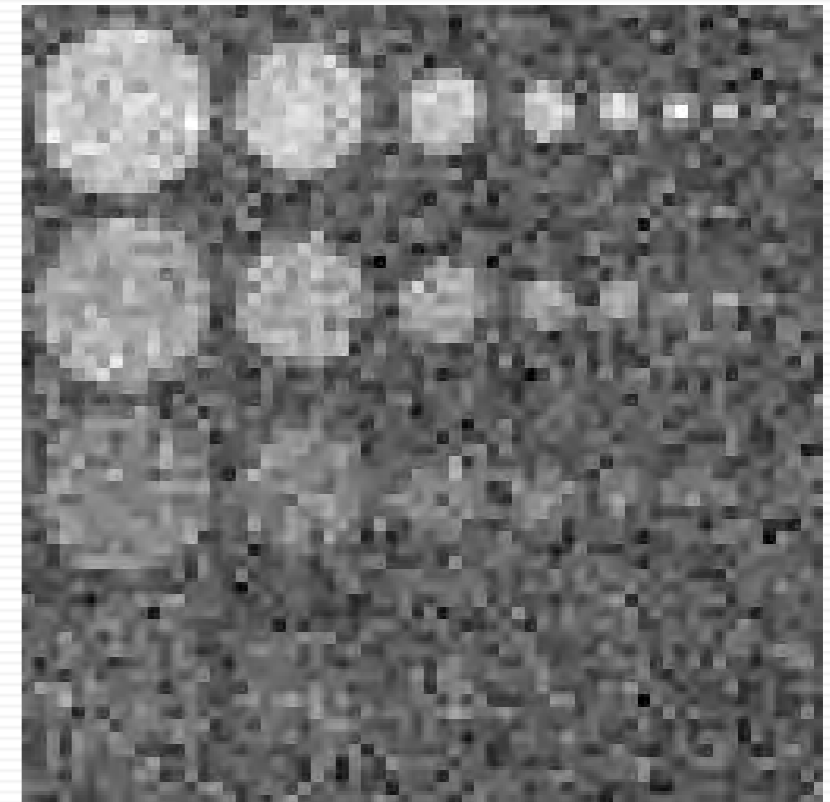


Signal/Noise Ratio Held Constant

128 X 128



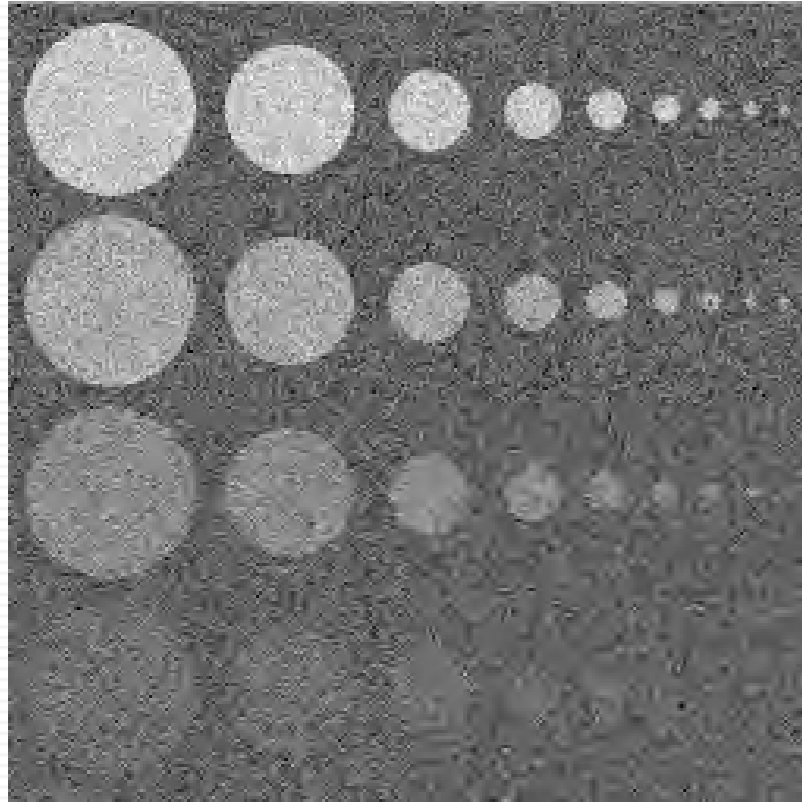
64 X 64



CNR vs. Resolution

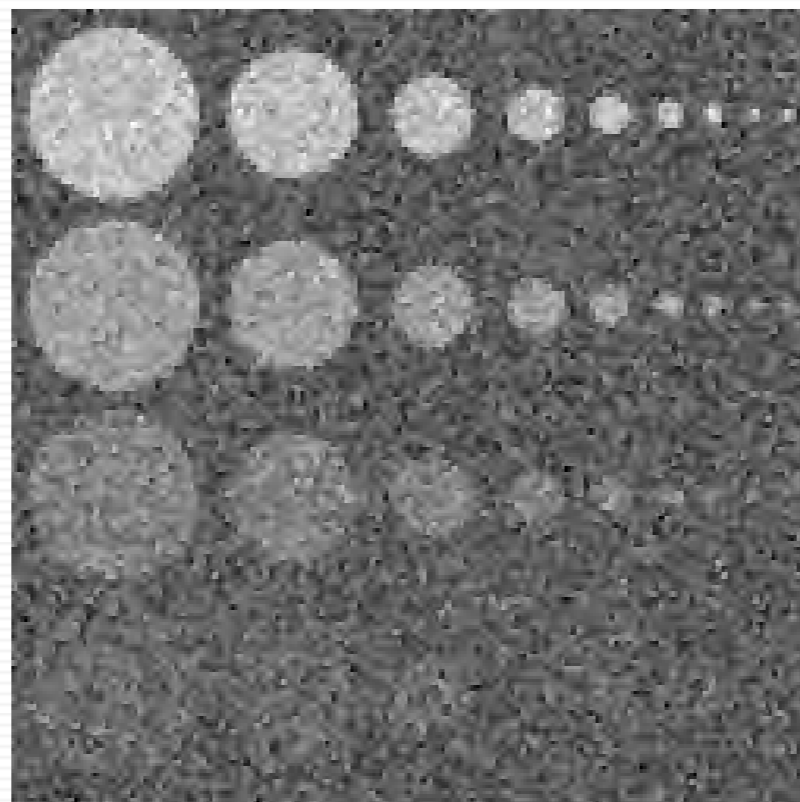
Signal/Noise Ratio Held Constant

256 X 256



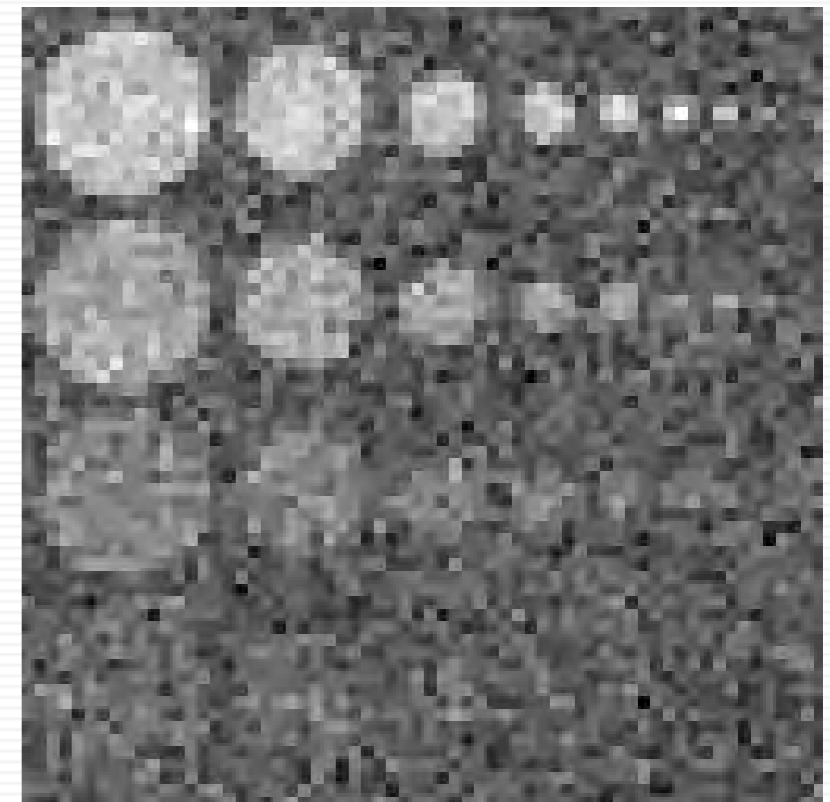
Imaging time = 16X

128 X 128



Imaging time = 4X

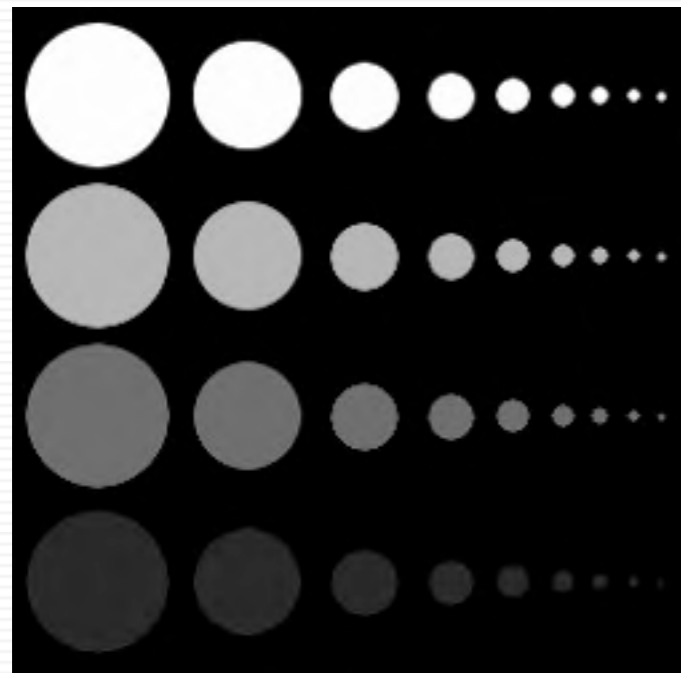
64 X 64



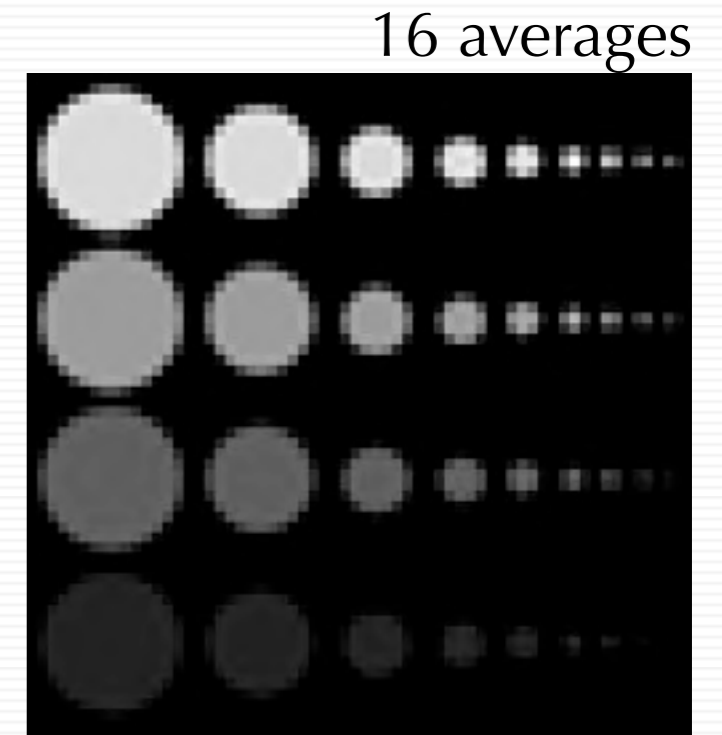
Imaging time = 1X



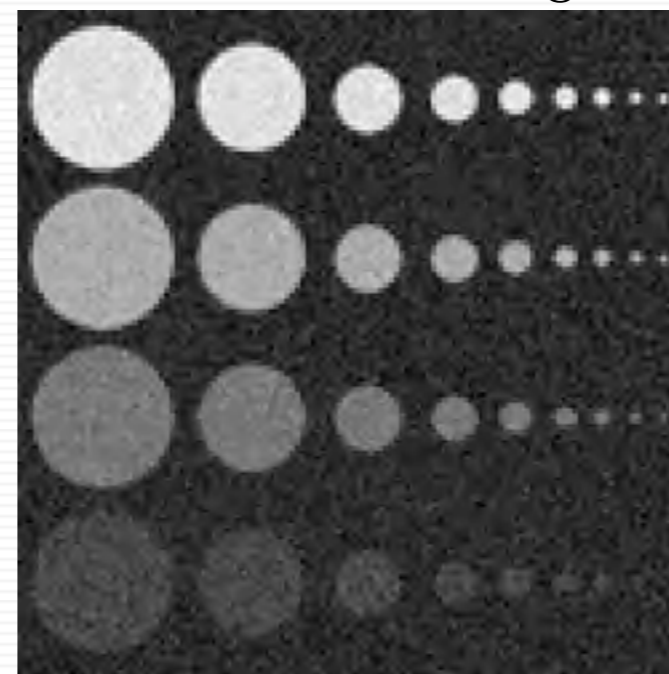
CNR vs. Resolution



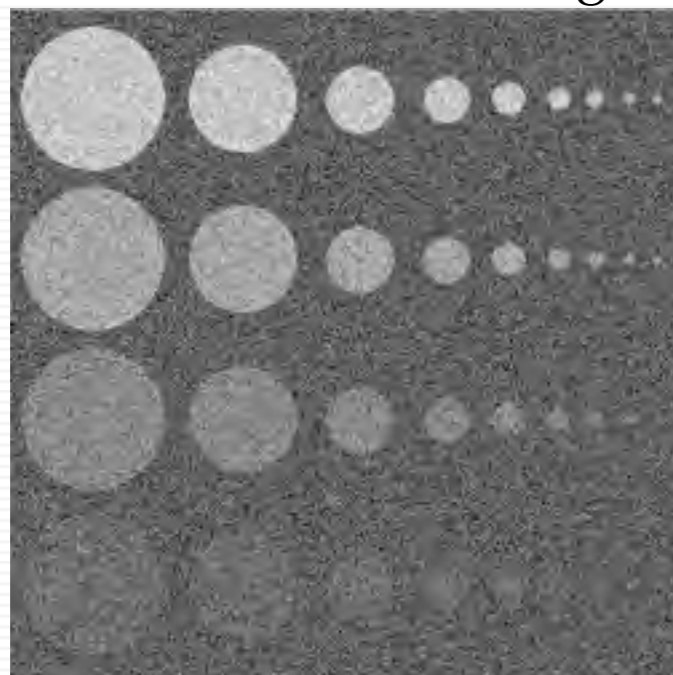
Noise free



16 averages



4 averages



1 average

64 X 64

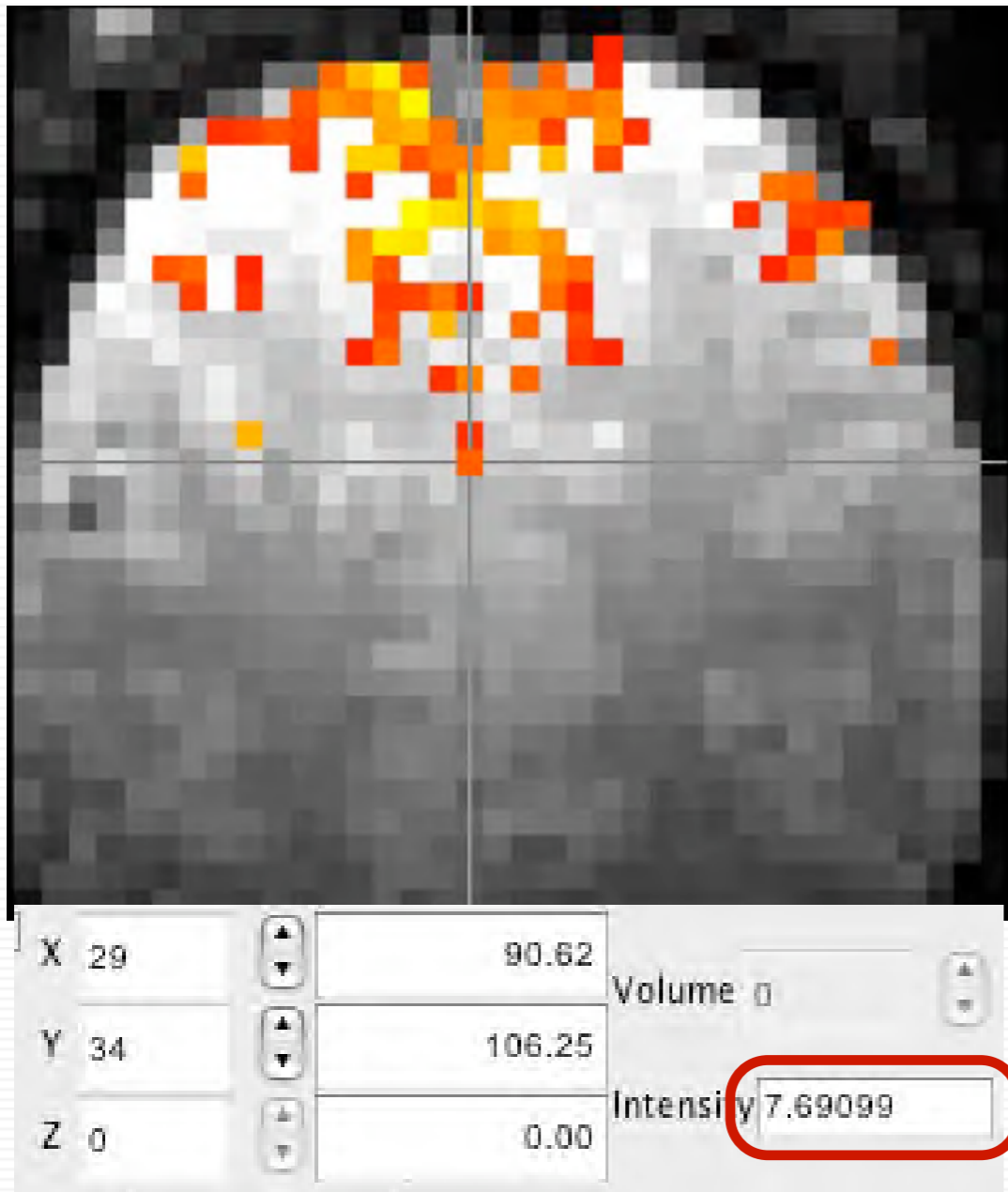
128 X 128

256 X 256

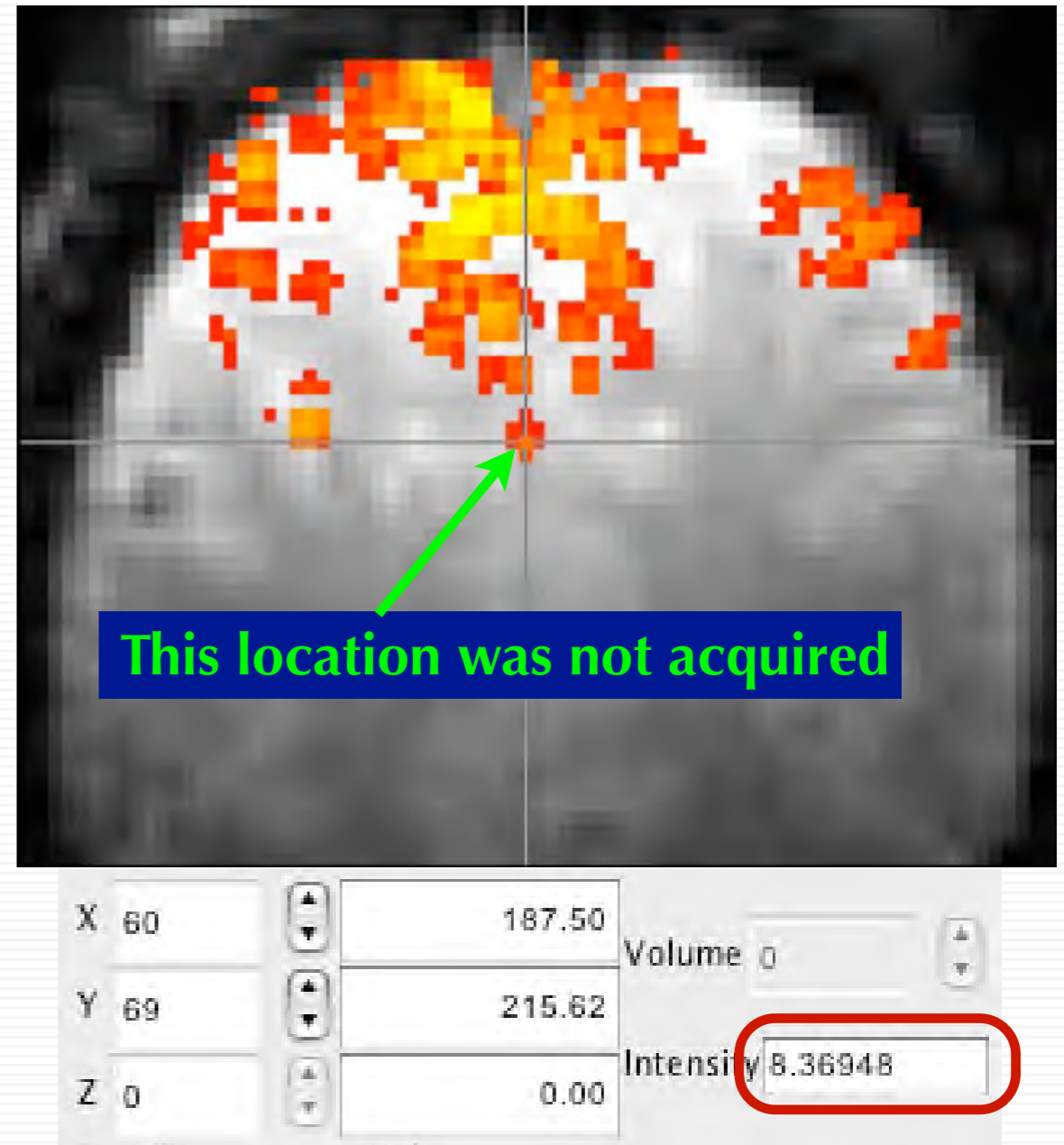
Imaging Time Held Constant



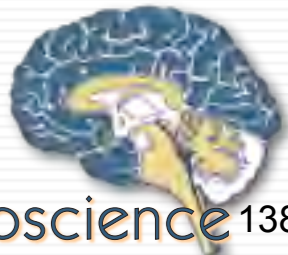
Interpolation



Native Resolution

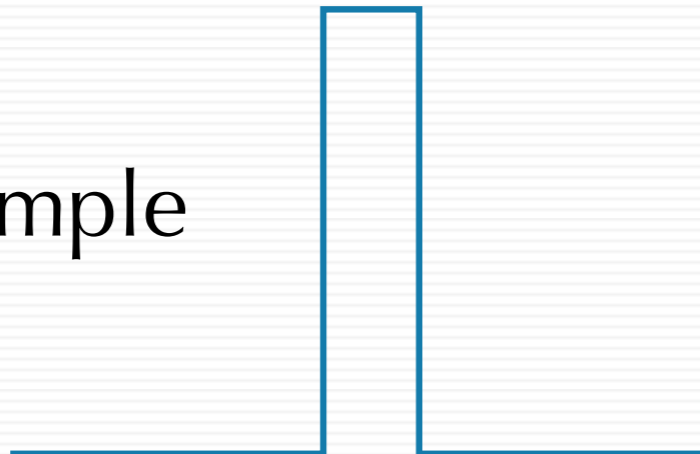


Bilinear Interpolation

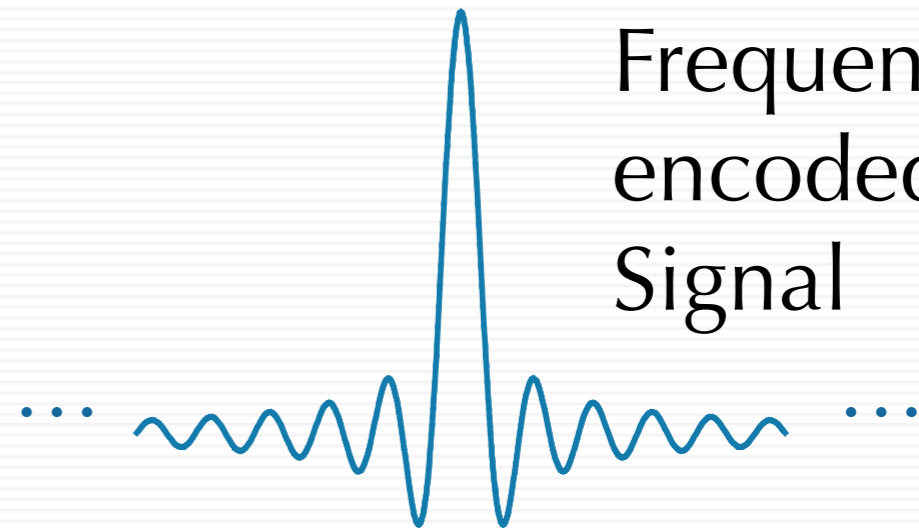


Truncation in Fourier Domain

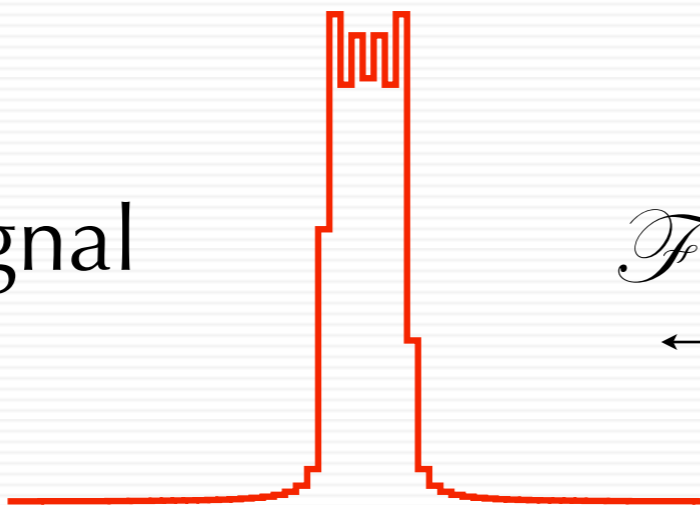
Original Sample



Frequency-
encoded
Signal



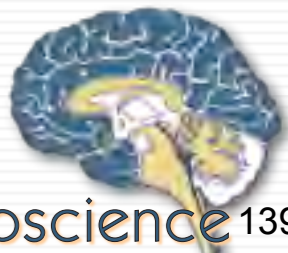
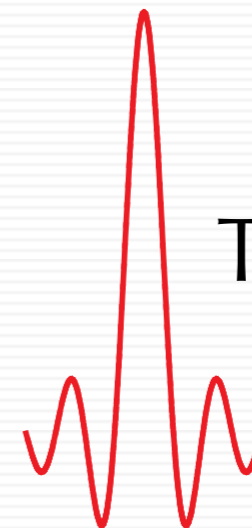
Apparent Signal



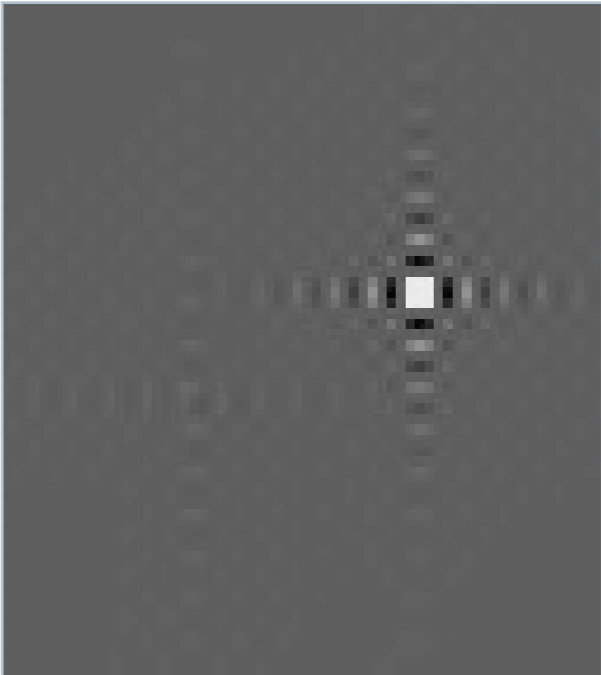
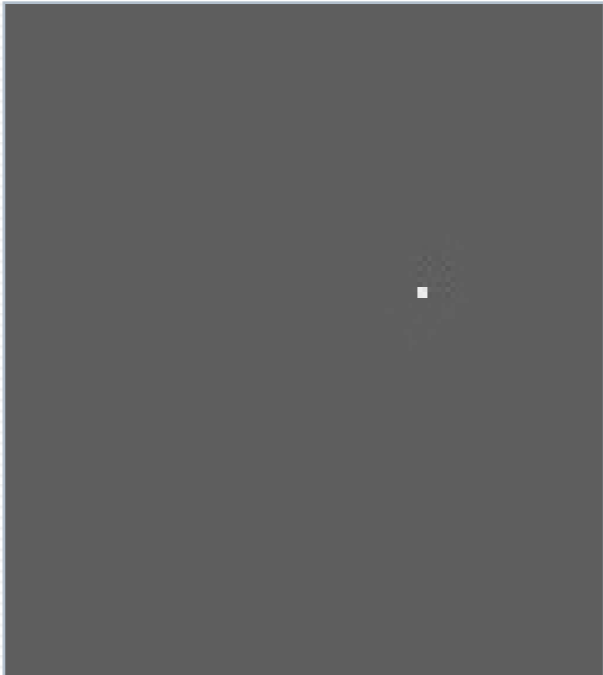
$$\mathcal{F}^{-1}(s)$$



Truncated Series

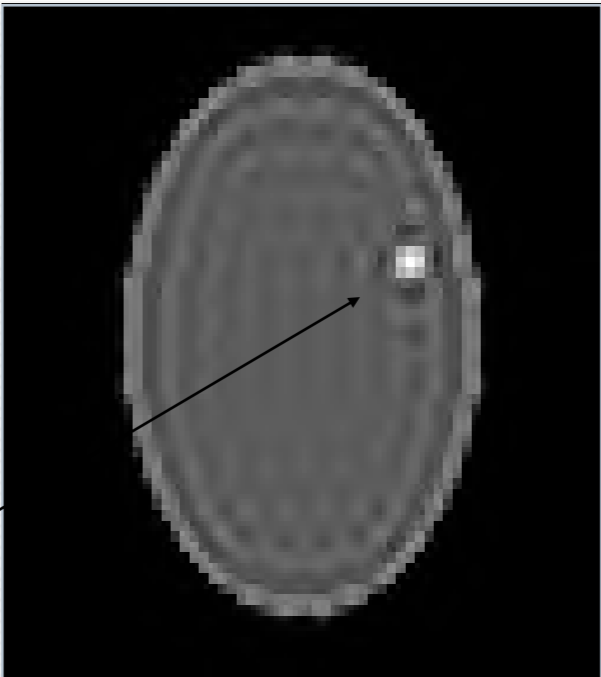
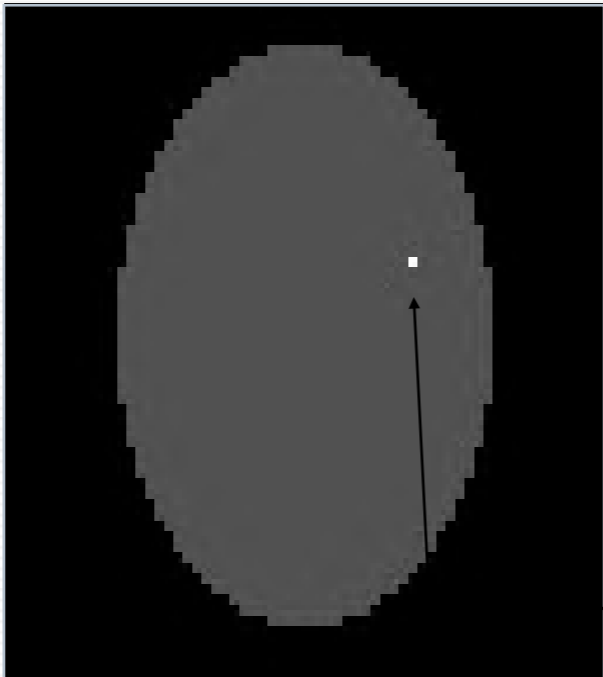


What is the actual resolution of MRI?

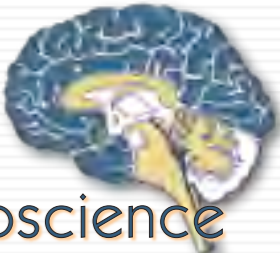


Original Data

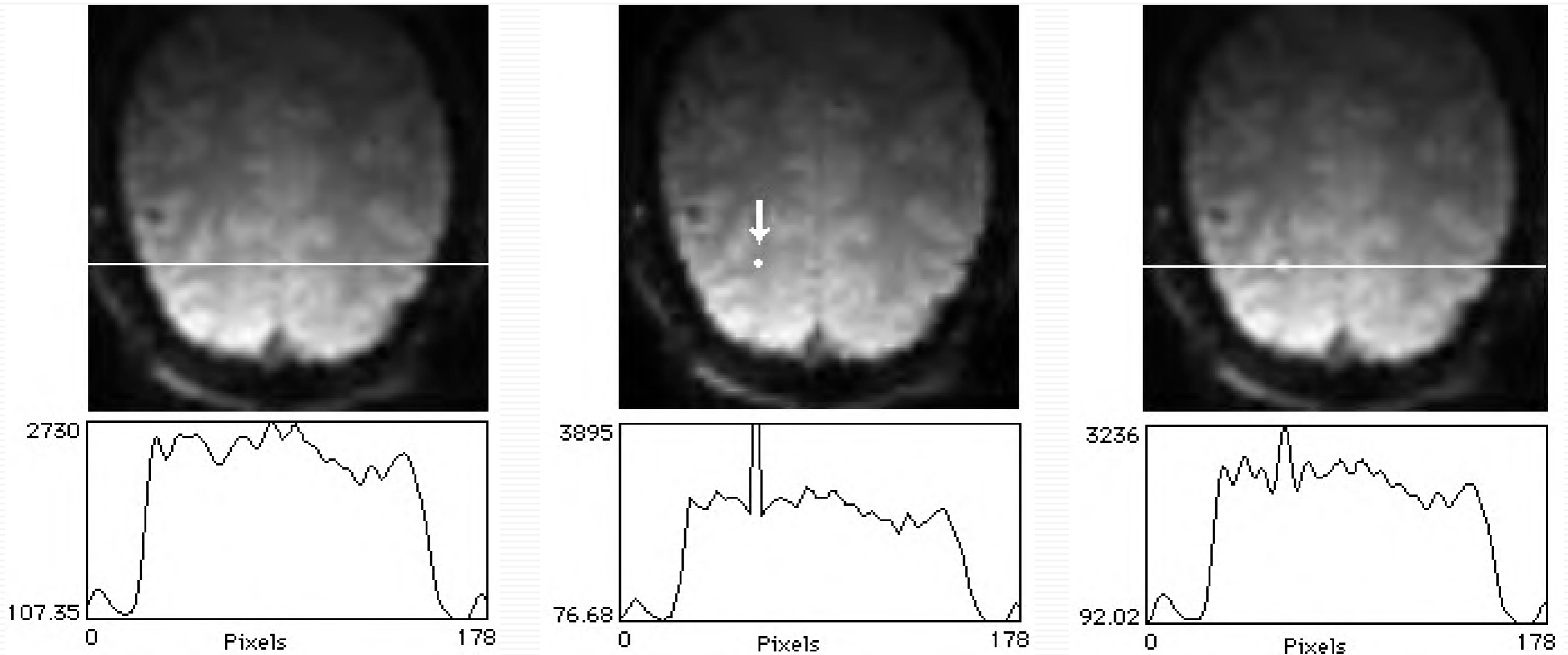
MR Image



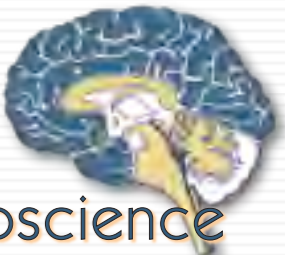
Single pixel "activation"



The Actual Resolution of *f*MRI



<http://ccn.ucla.edu/BMCweb/SharedCode/MRArtifacts/MRArtifacts.html>



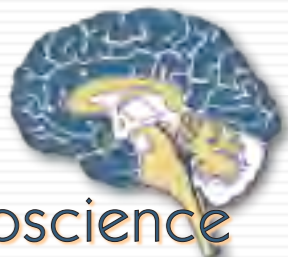
Bandwidth and Readout

- Position is encoded by FREQUENCY
- Bandwidth refers to the Frequency Difference from the center of the image to its edge:

$$\text{Frequency per pixel} = \frac{2 * \text{Bandwidth}}{\text{number of pixels}} = \frac{1}{\text{readout duration}}$$

- Bandwidth decreases with readout duration:

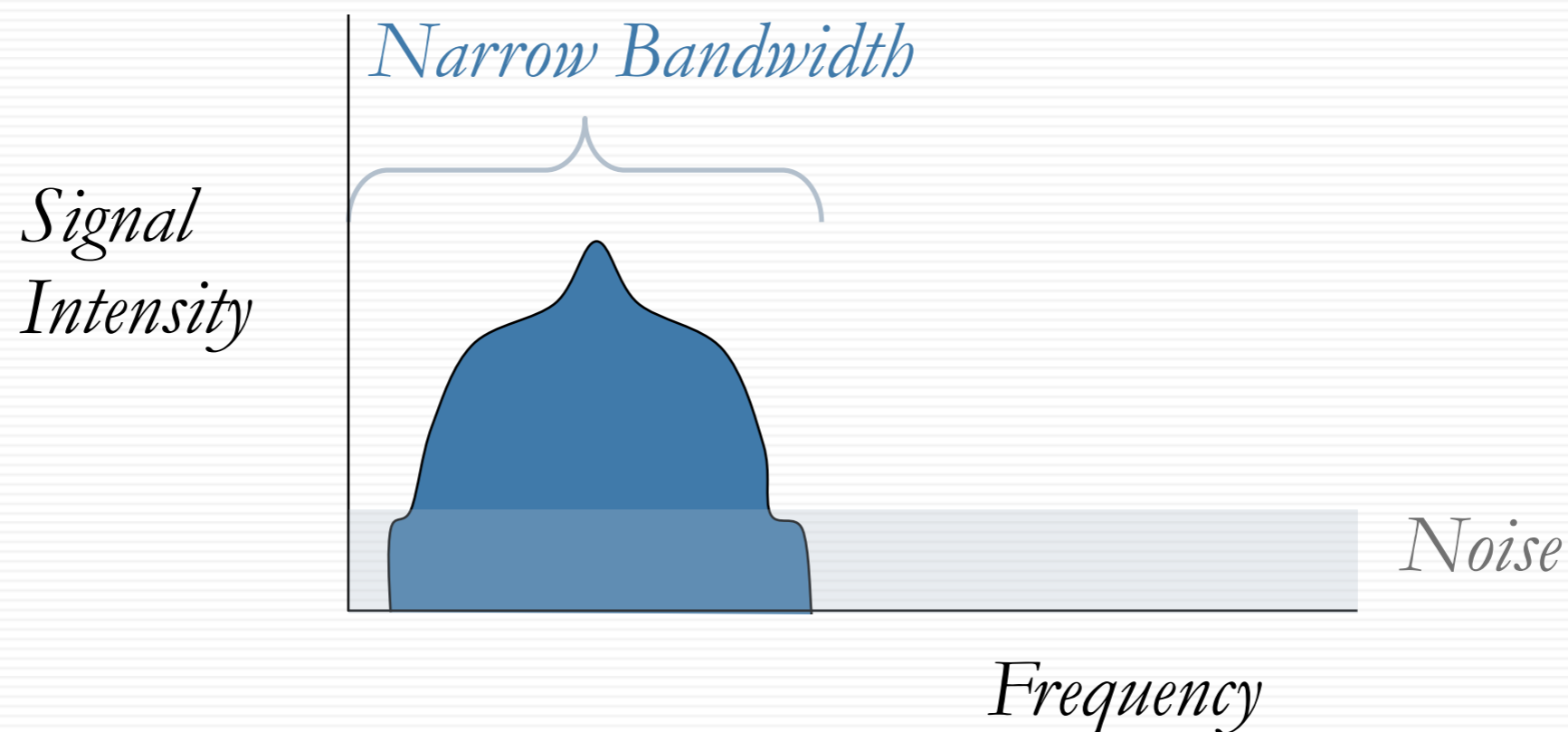
$$\text{Bandwidth} = \frac{\text{number of pixels}}{2 * \text{readout duration}}$$



Bandwidth and SNR

Decreasing the Bandwidth Improves SNR:

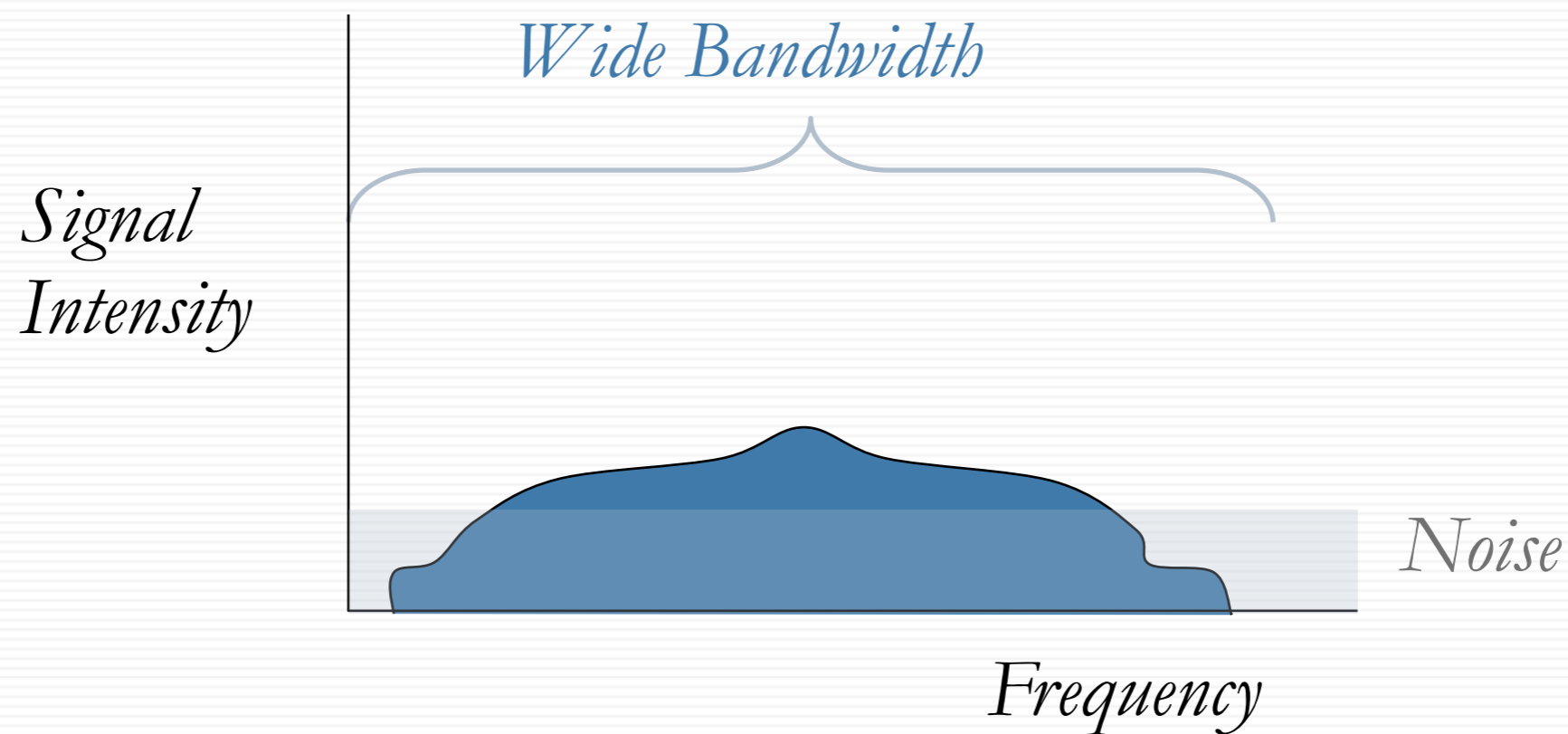
Imaging Time is **INCREASED** and high frequency noise is excluded



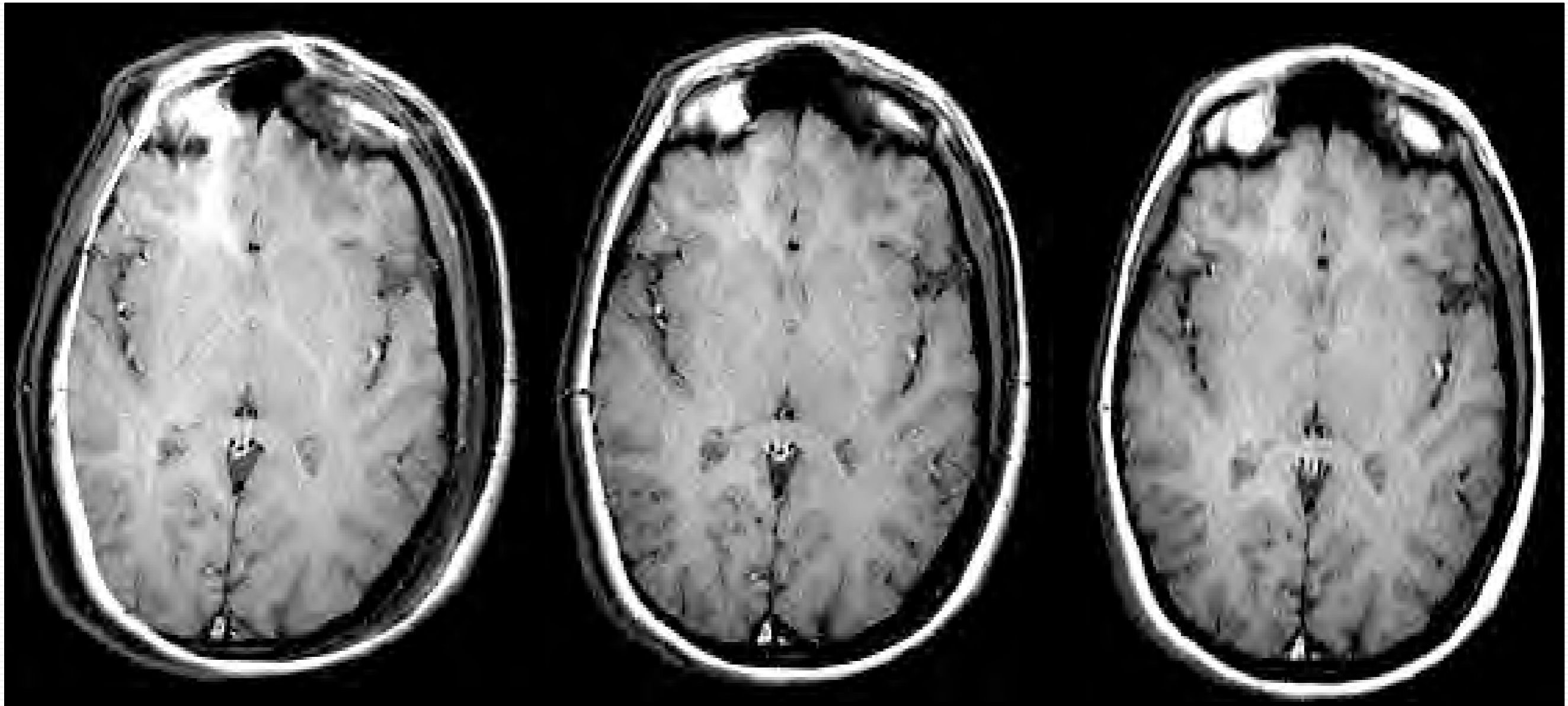
Bandwidth and SNR

Decreasing the Bandwidth Improves SNR:

Imaging Time is **INCREASED** and high frequency noise is excluded



Bandwidth



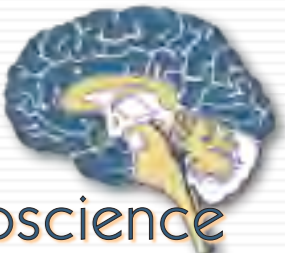
BW=4kHz

BW=8kHz

BW=16kHz

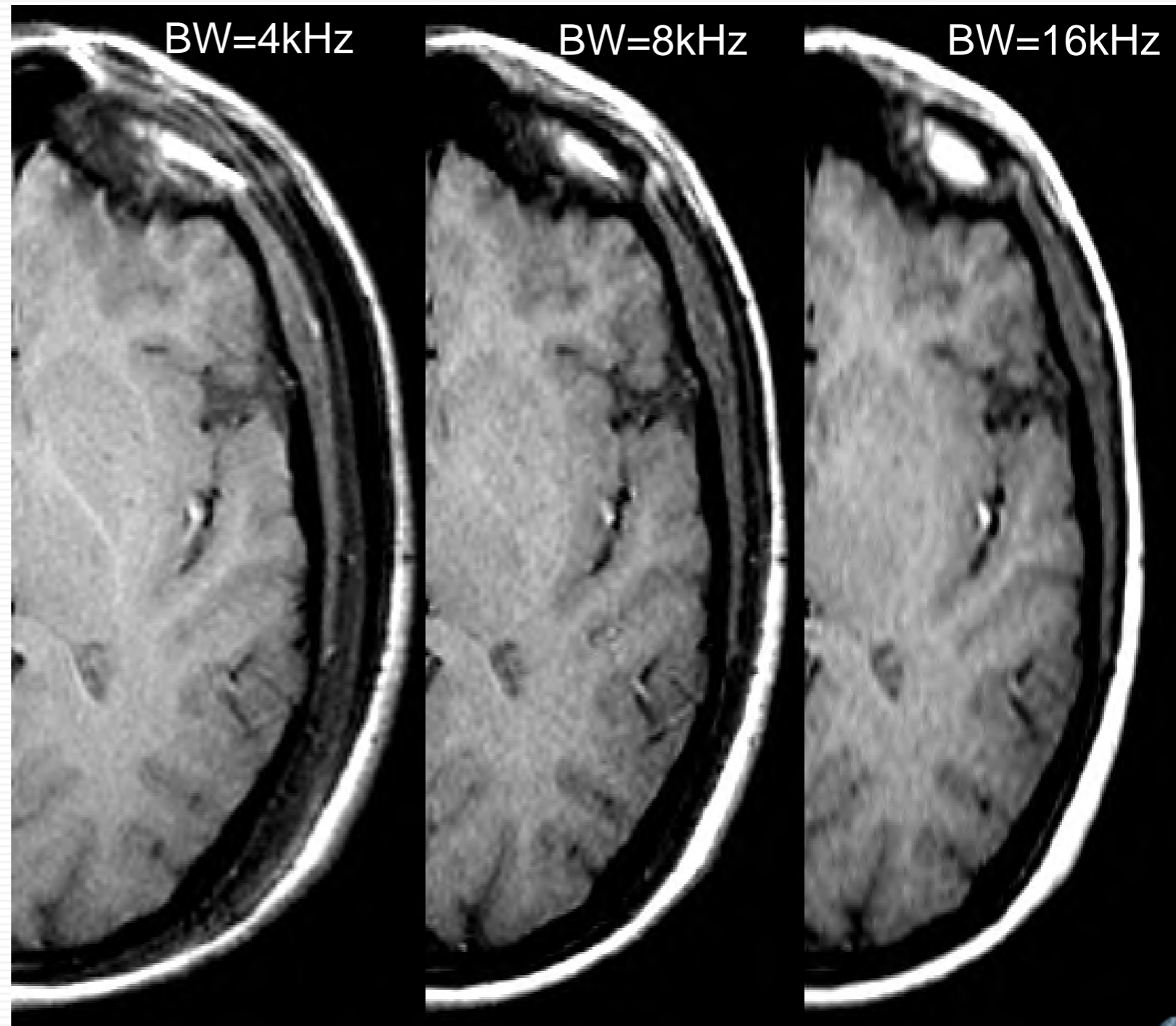
TE=11-14
TR=500

NEX=1 **Thick=3mm**
Matrix=256x256

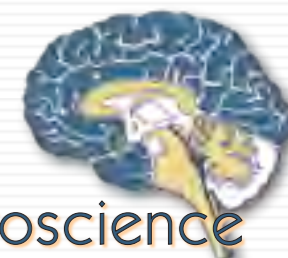
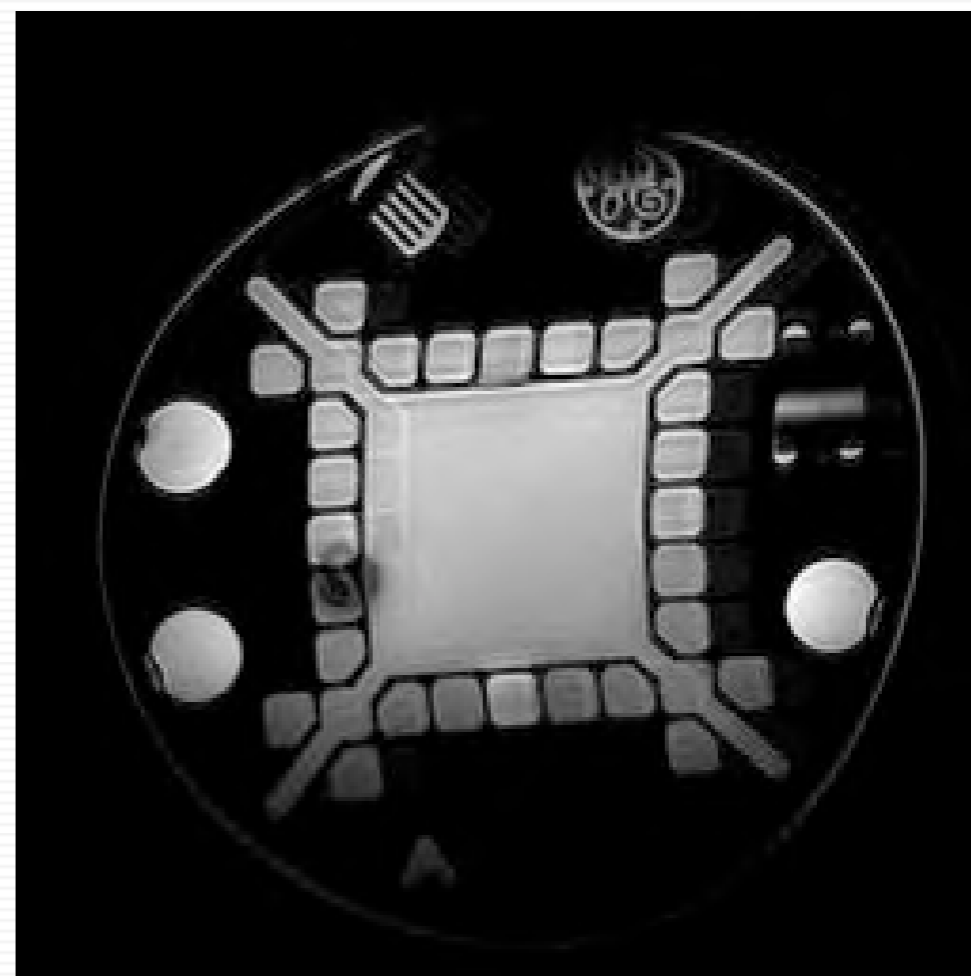
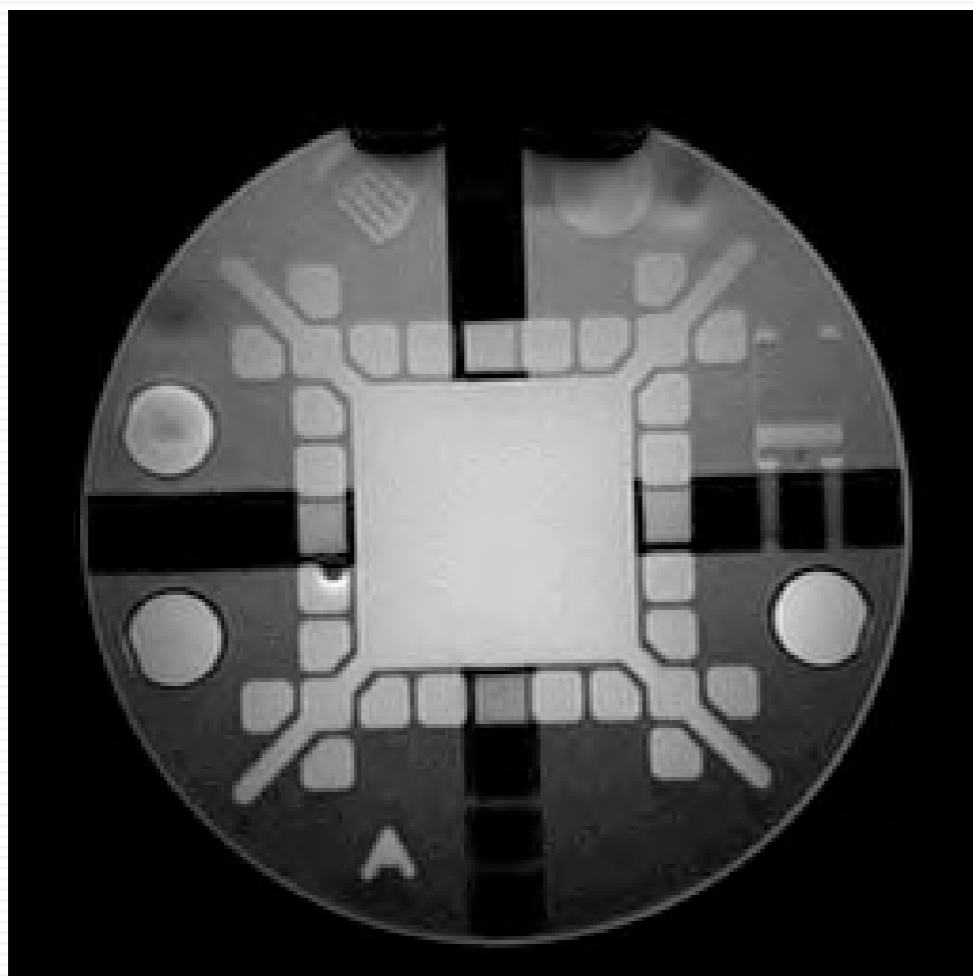


Bandwidth

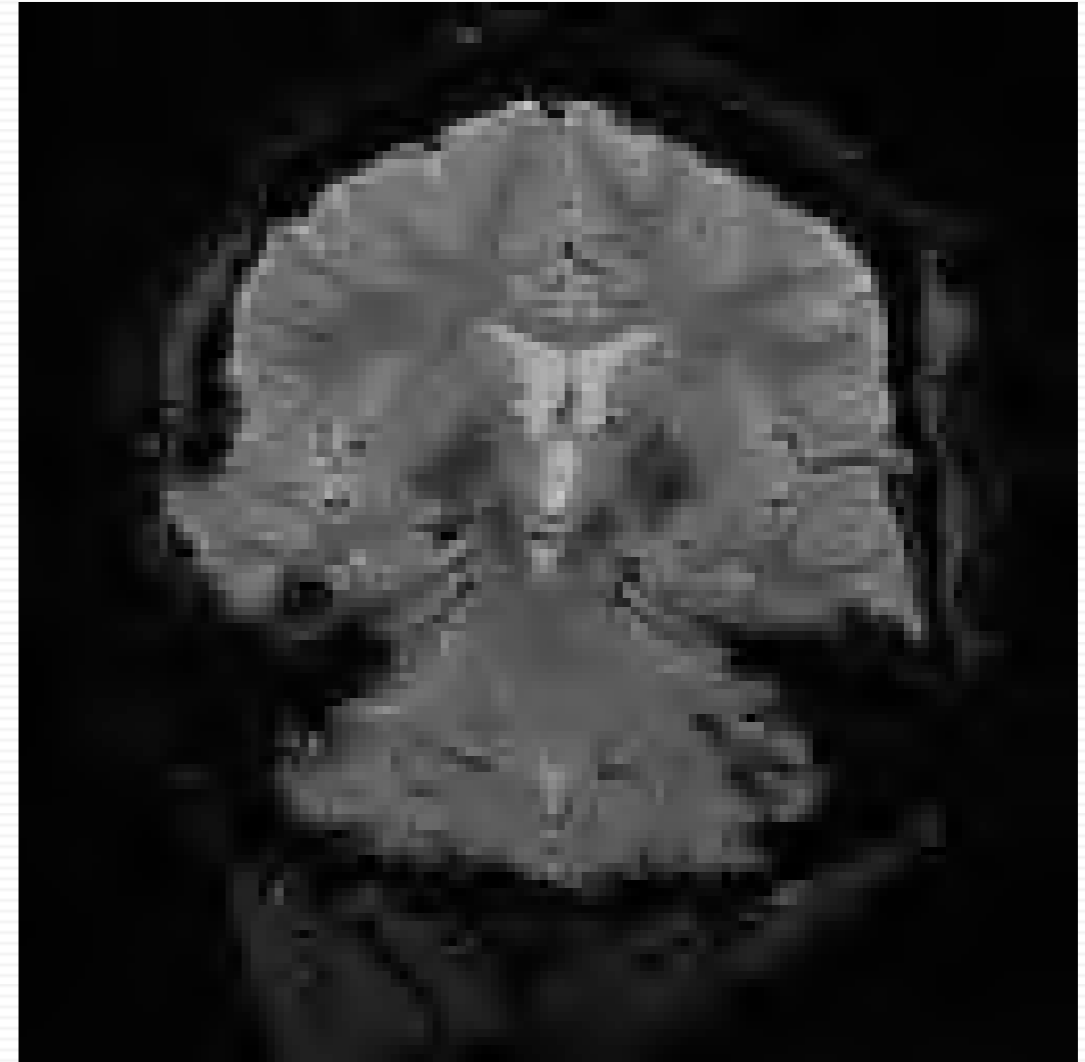
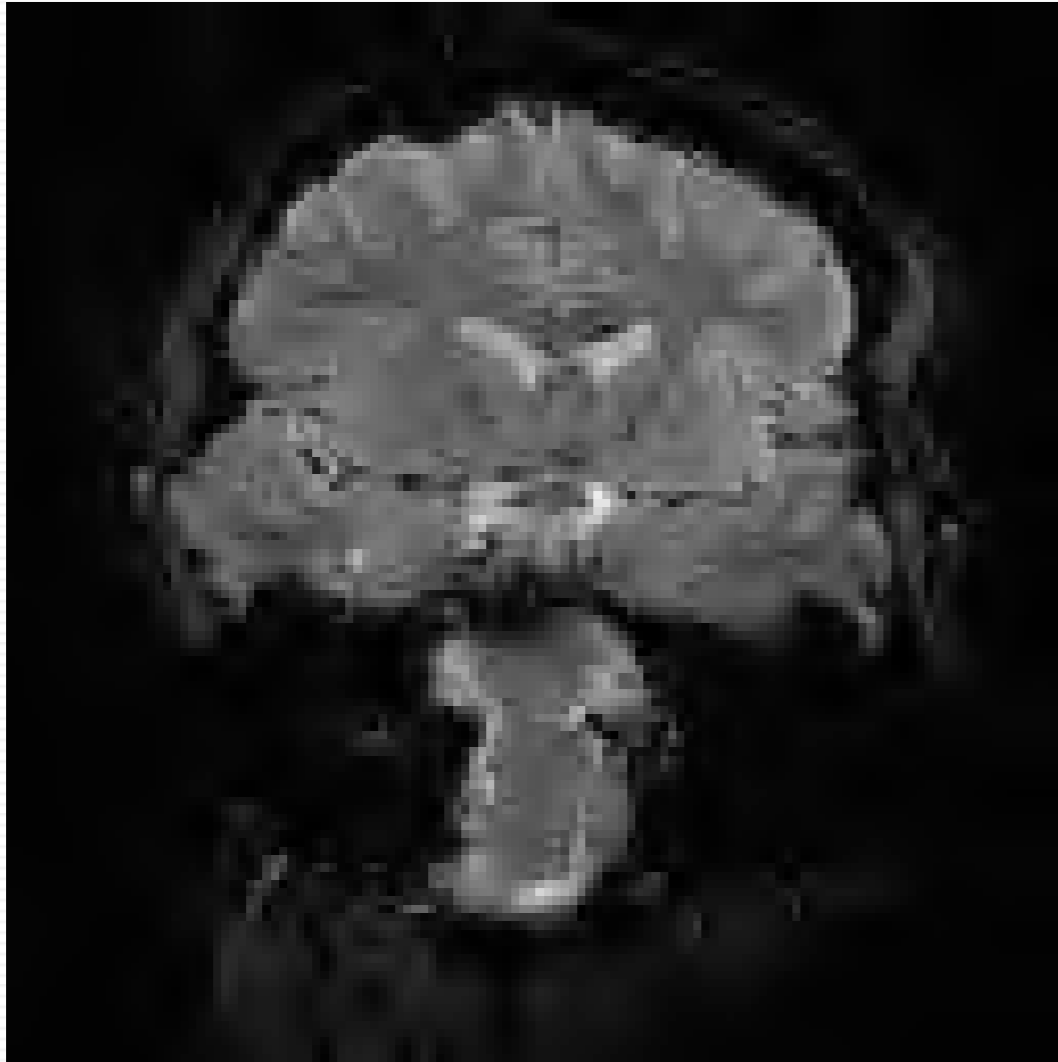
TE=11-14
NEX=1
Thick=3mm
TR=500
Matrix=256x256



Shape and Bandwidth



Distortions are More Severe at High Magnetic Field Strength



Variation in sample magnetization of is proportional to field strength.



High Field images lose more signal from field

inhomogeneity

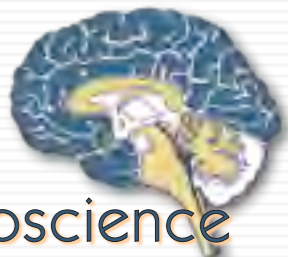
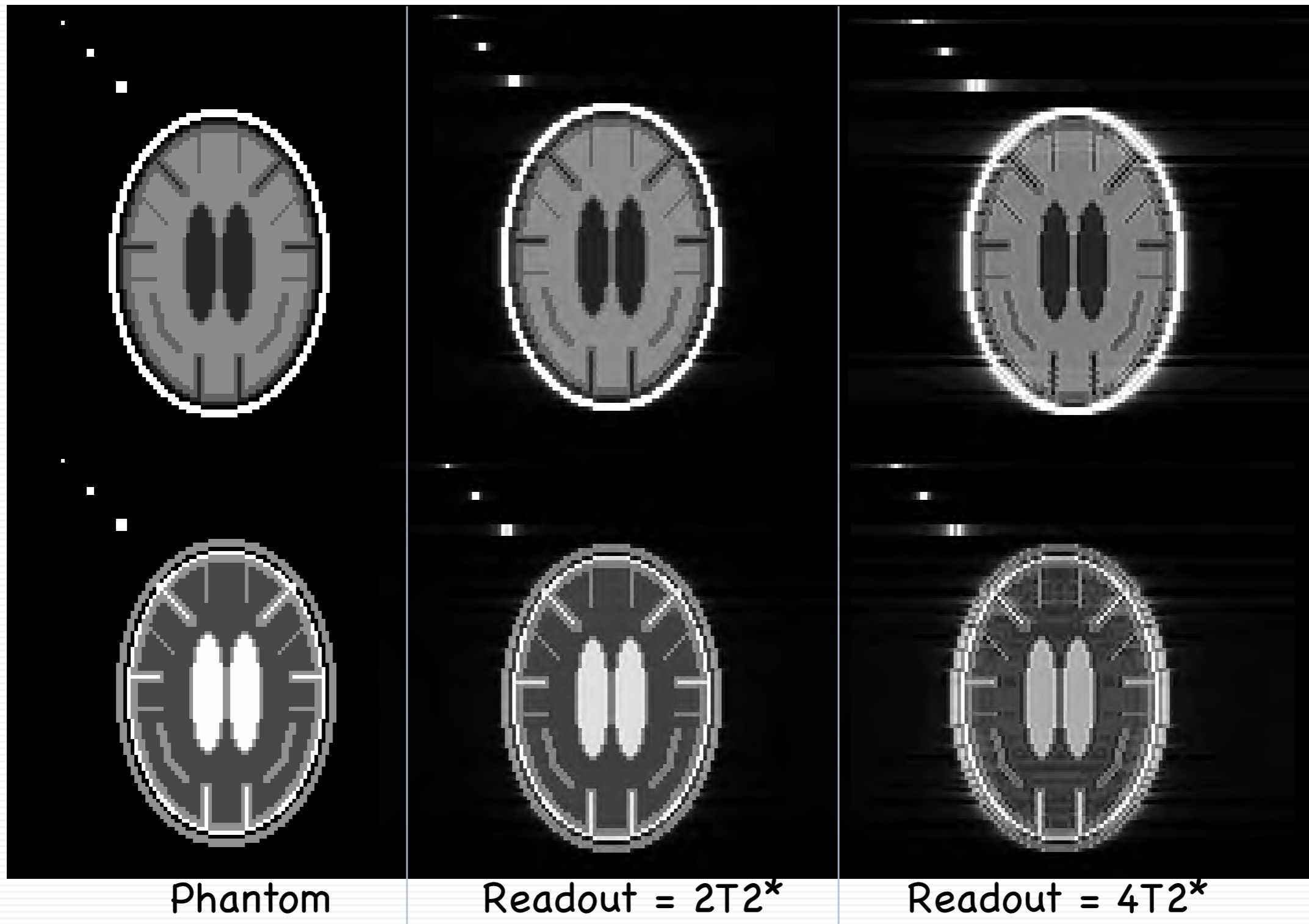
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www.brainmapping.org

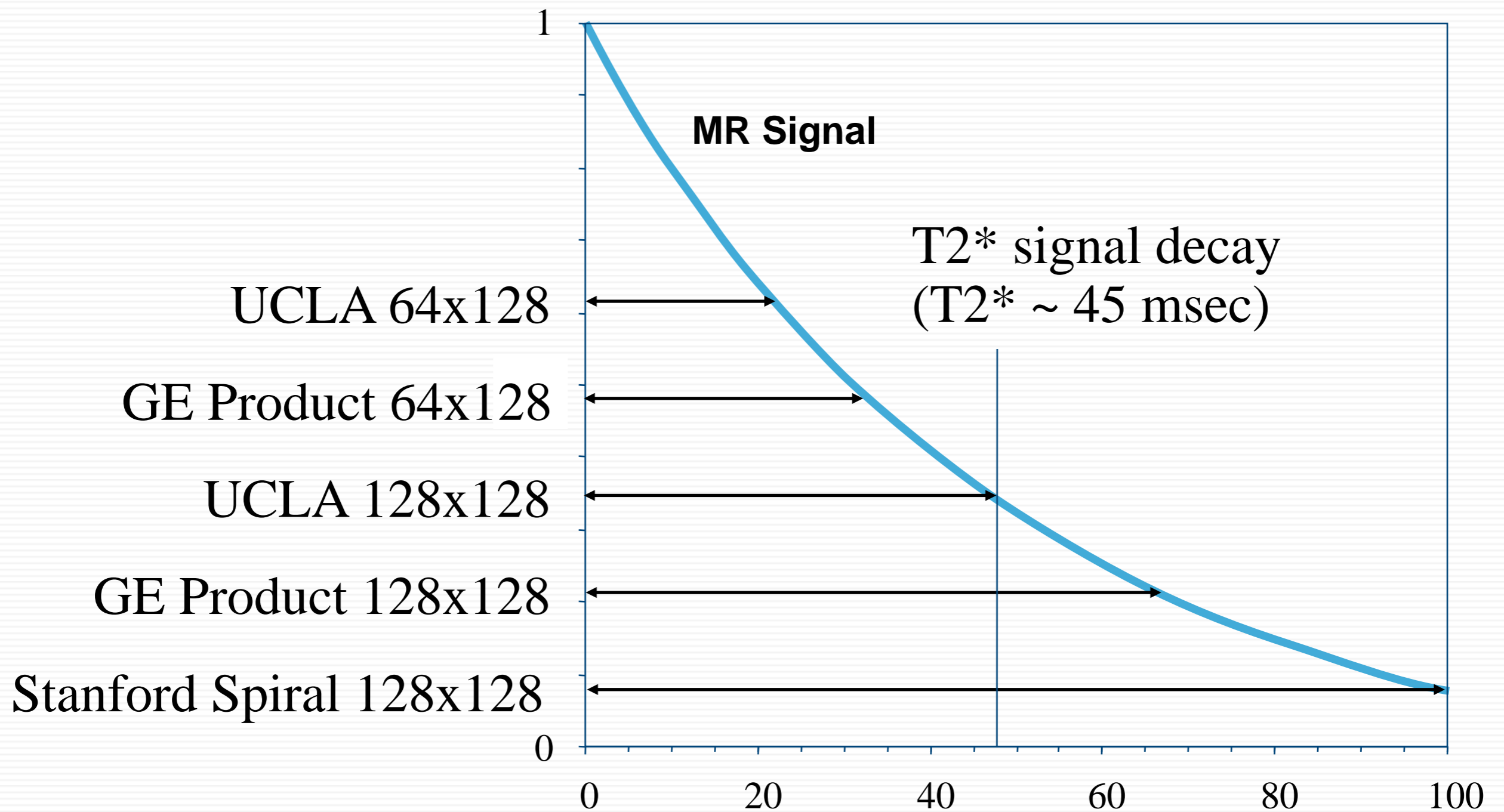
Center for
Cognitive Neuroscience



Apodization from Long Readouts



EPI Readout Durations

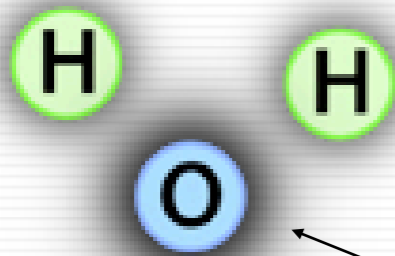


The Origin of Chemical Shift

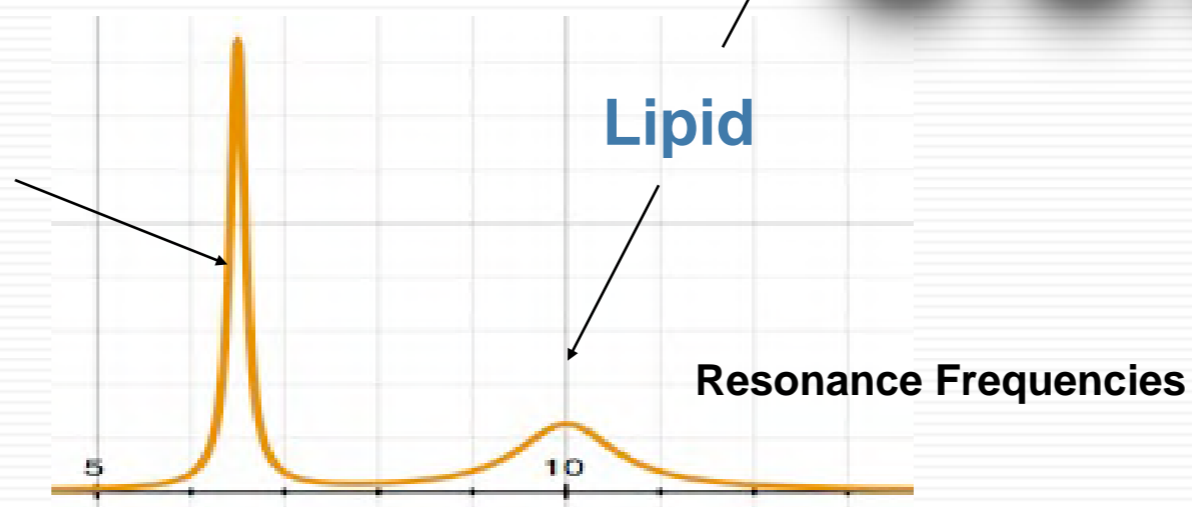
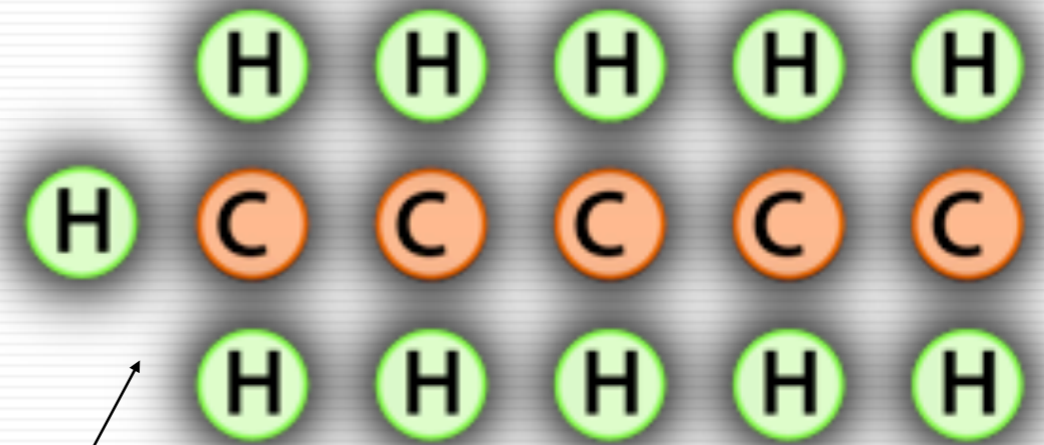
In water, electrons move from Hydrogen towards Oxygen.

This exposes the Proton to a slightly higher magnetic field.

Electrons in lipid are shared equally between Hydrogen and Oxygen



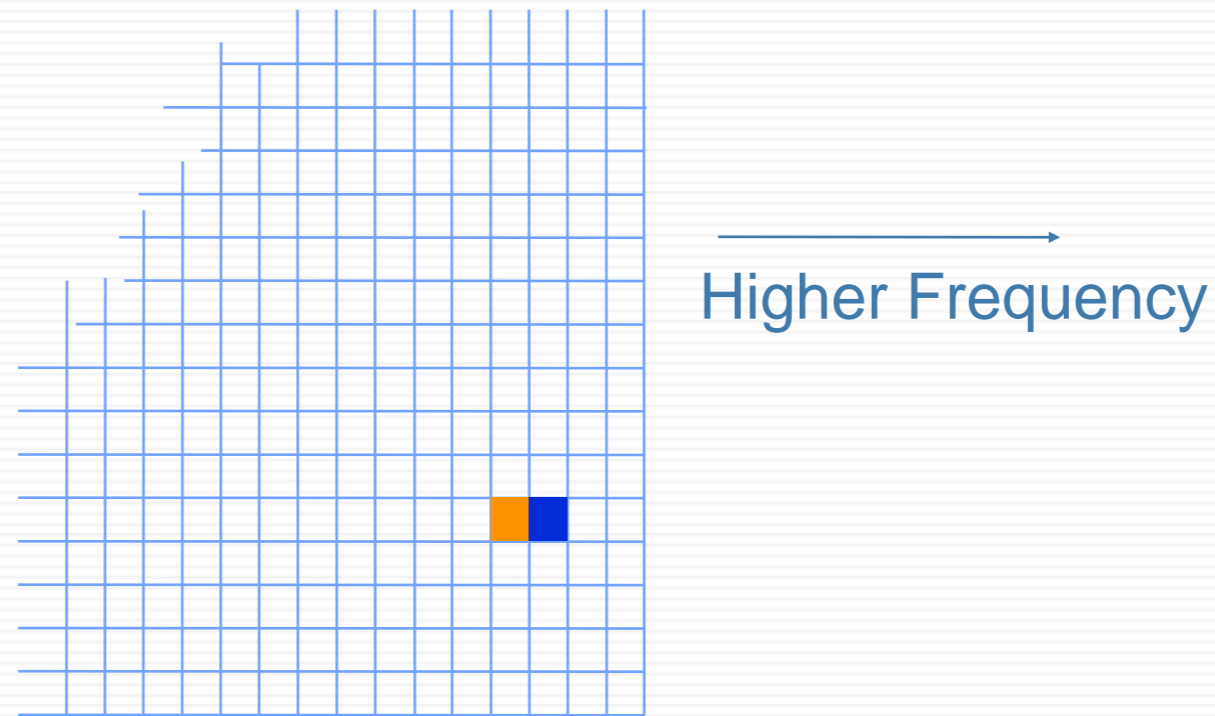
Water



Higher Frequency



Chemical Shift Artifact



If the frequency *width* of each pixel is less than the frequency *difference* between **water** and **lipid**, then **water** and **lipid** will appear in separate pixels



Chemical Shift

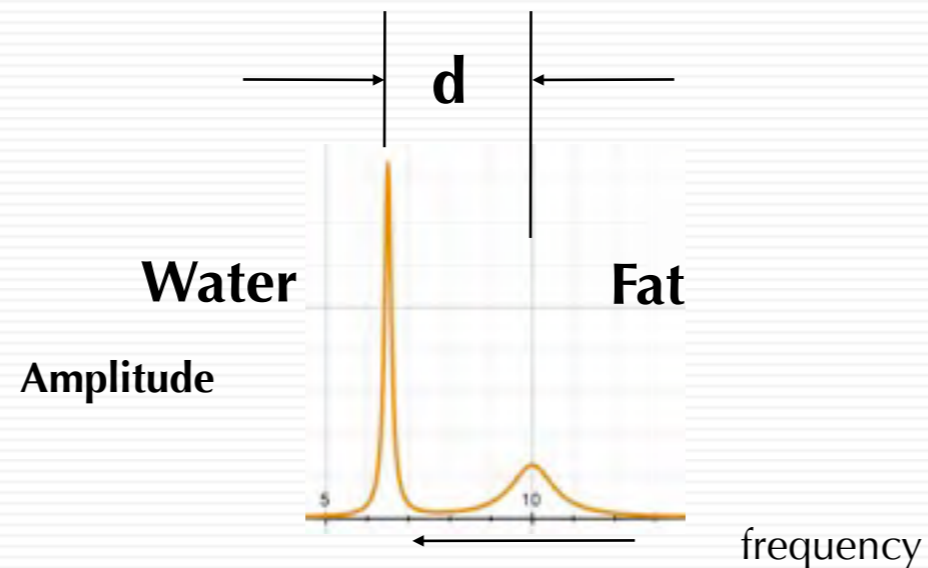
The Fat-Water chemical shift is about 3.5 ppm or:

Which is:

with a 32 kHz readout

75 Hz @ 0.5 Tesla
150 Hz @ 1.0 Tesla
220 Hz @ 1.5 Tesla
440 Hz @ 3.0 Tesla

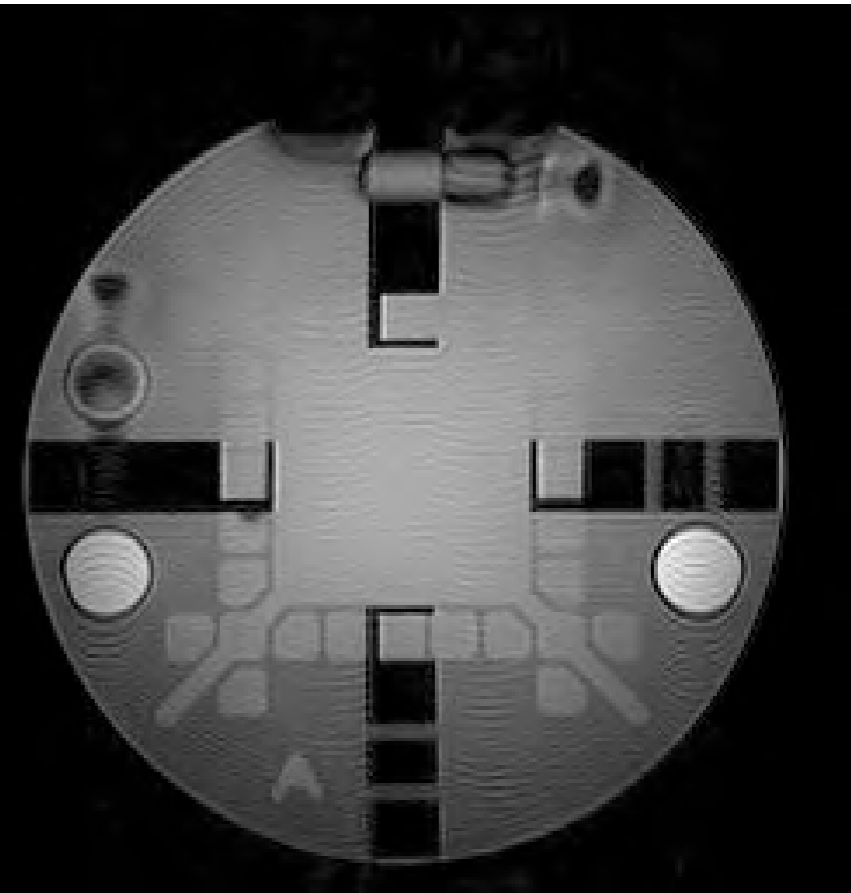
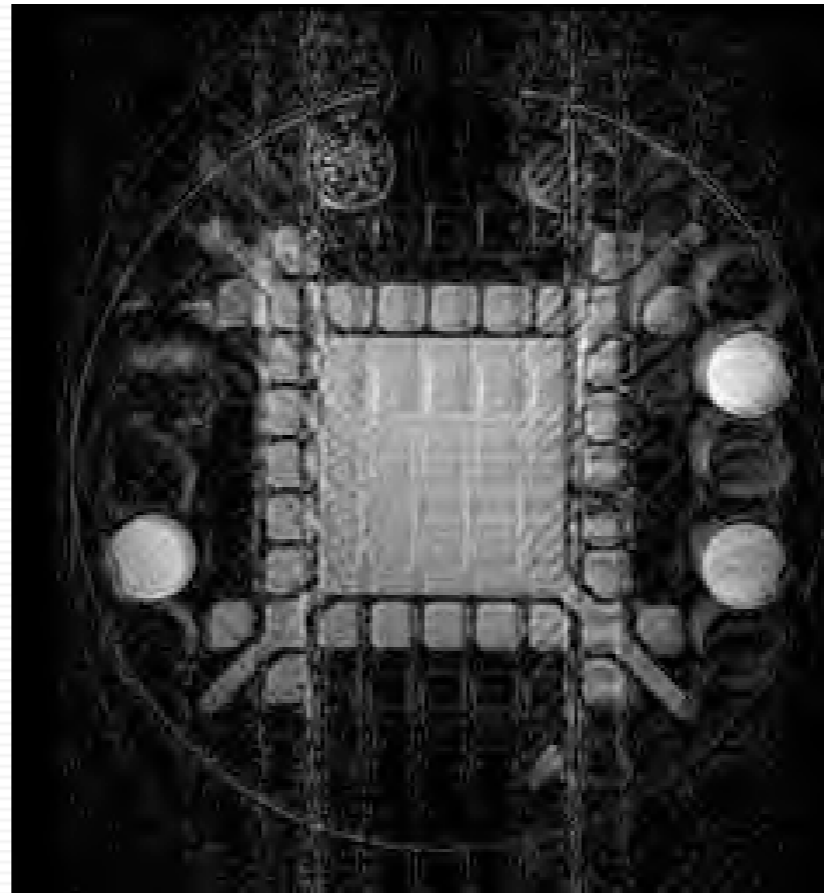
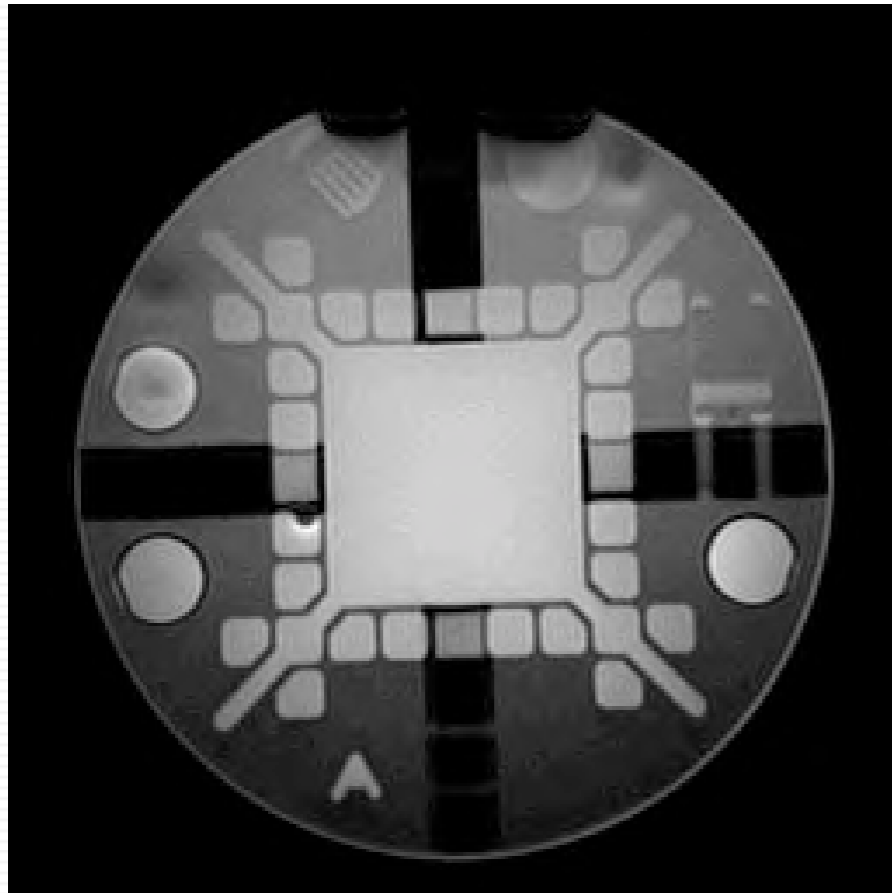
< 1 pixel
 \approx 1 pixel
> 1 pixel
 \approx 3.5 pixels



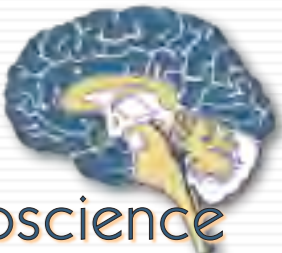
Lowering the Bandwidth/pixel increases the Chemical Shift in pixels



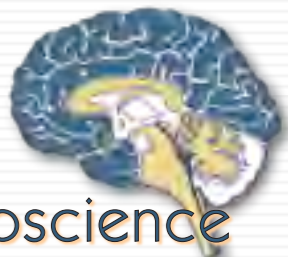
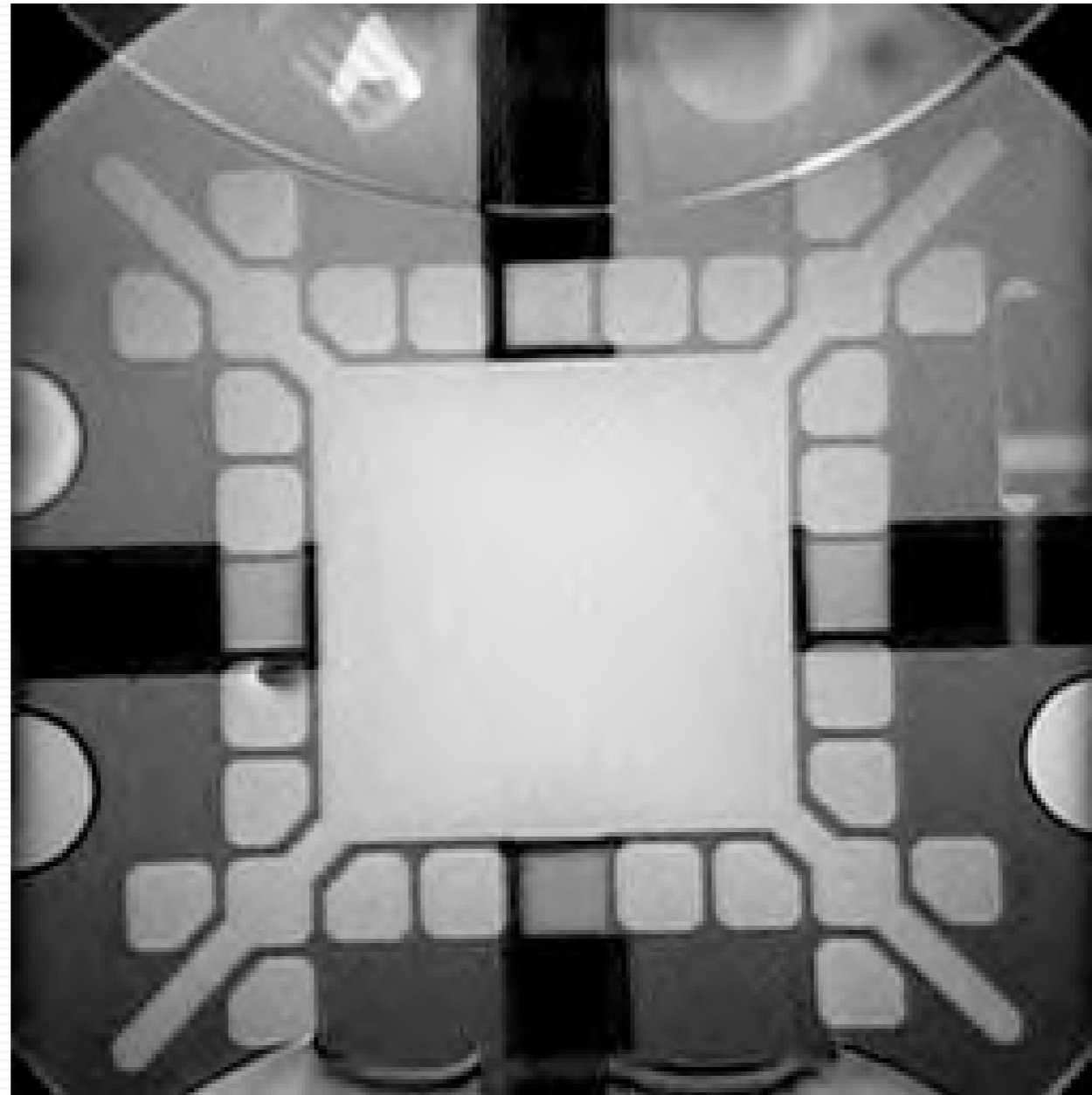
Motion Artifact



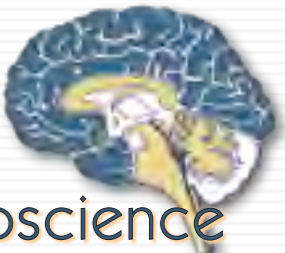
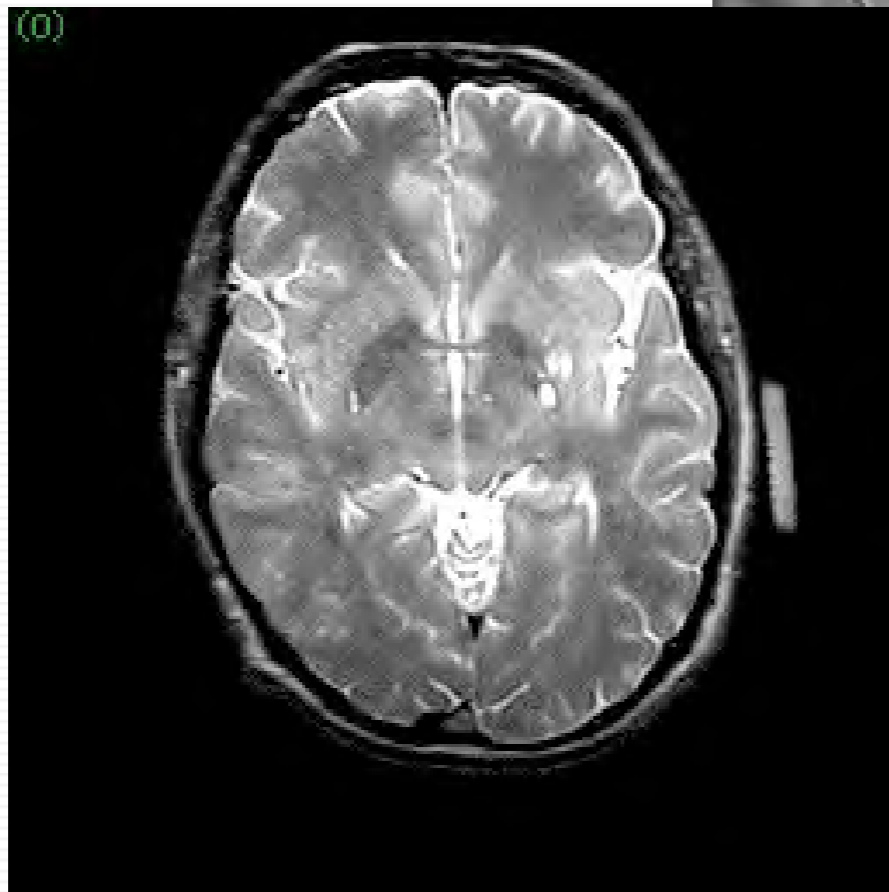
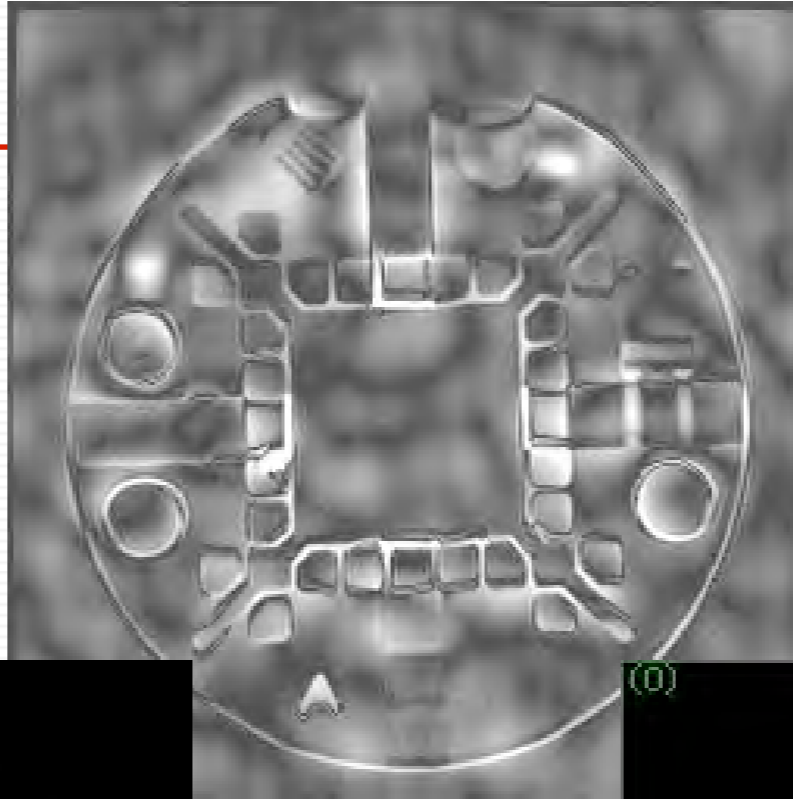
<http://airto.ccn.ucla.edu/BMCweb/SharedCode/MRArtifacts/MRArtifacts.html>



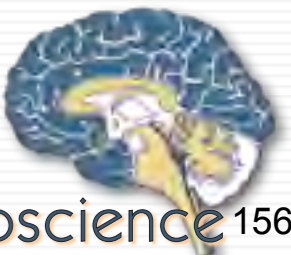
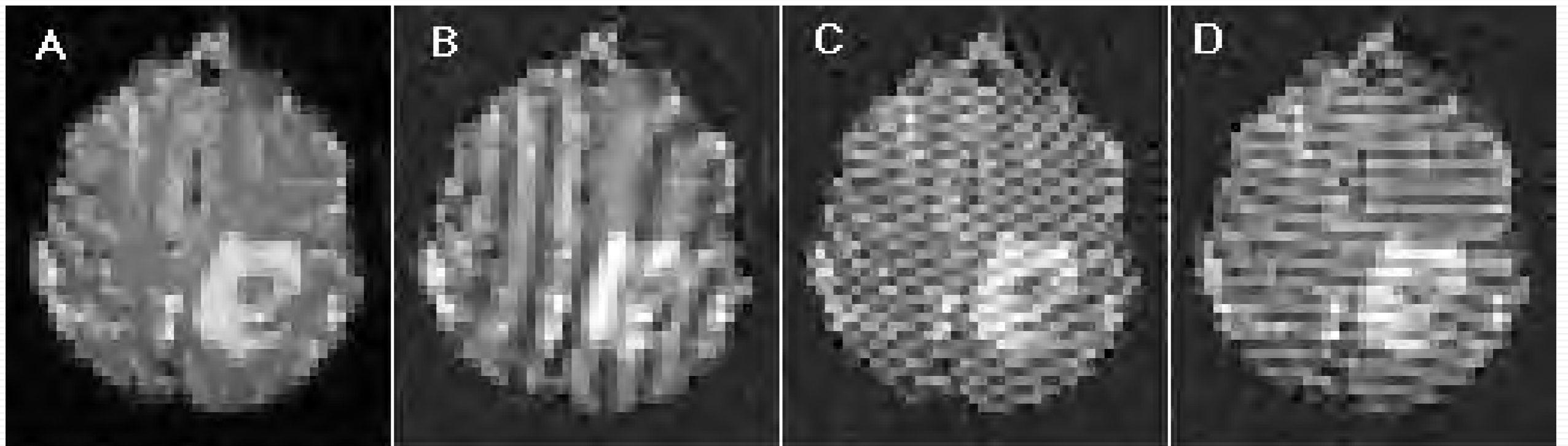
Aliasing



Saturation



Spikes



Spikes

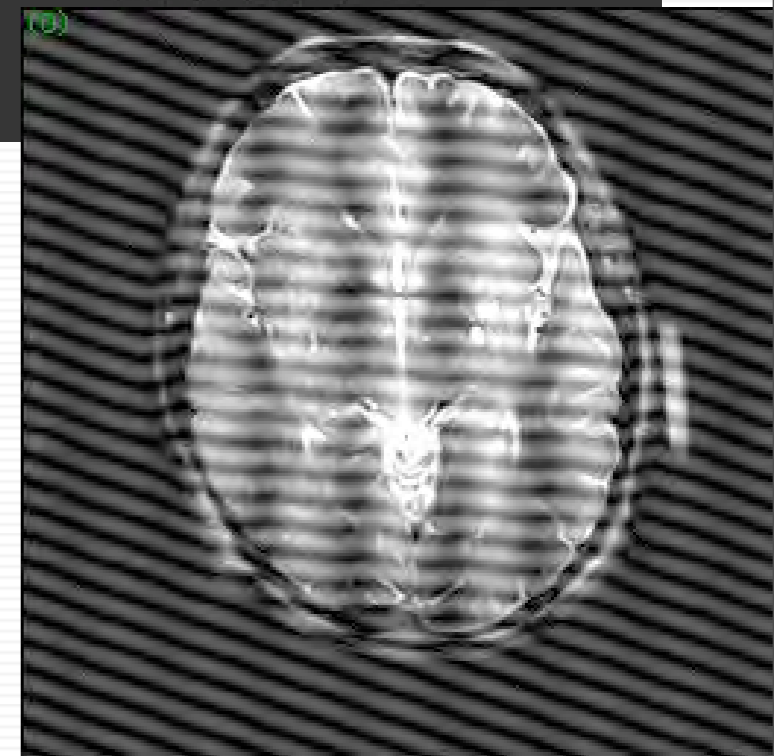
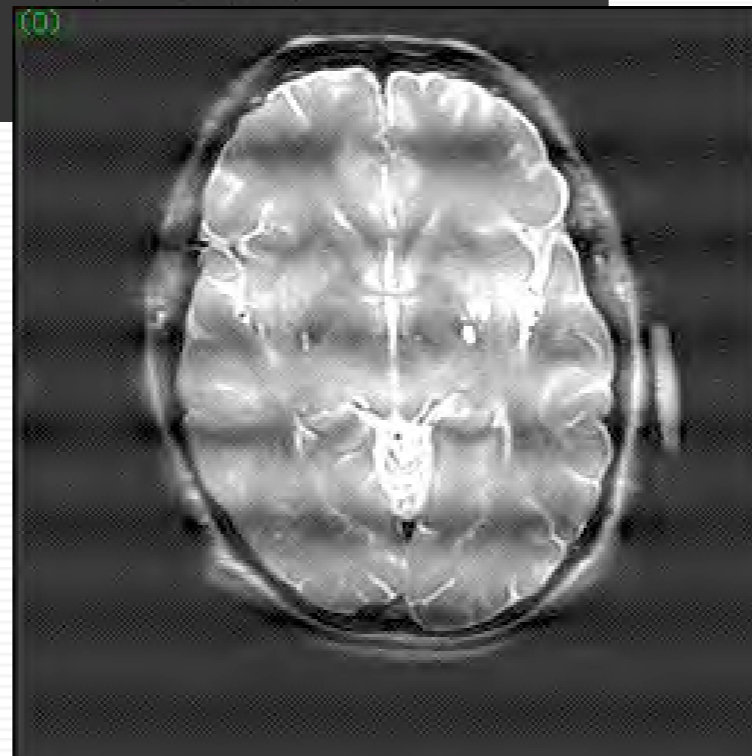
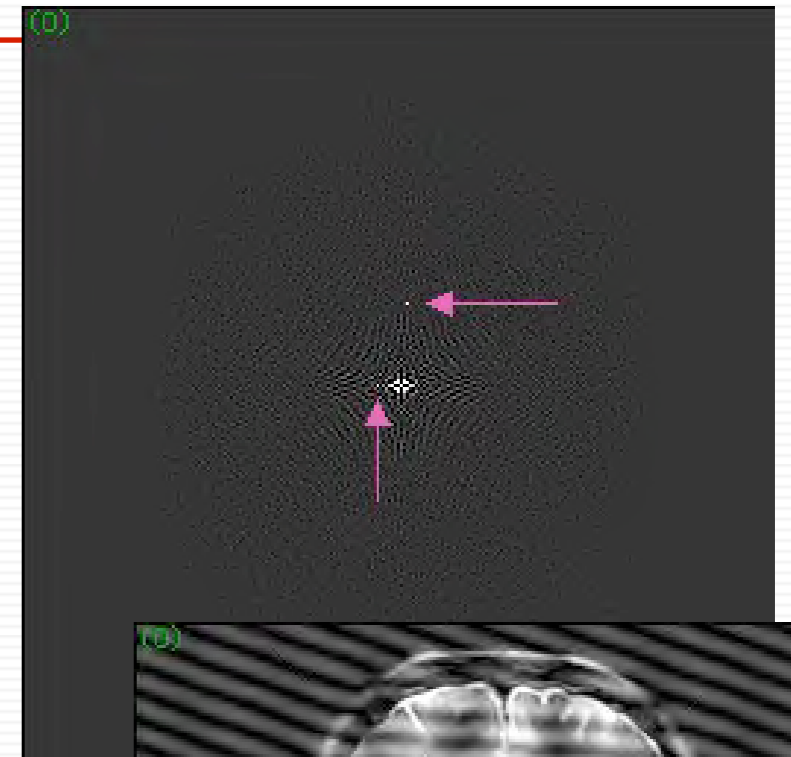
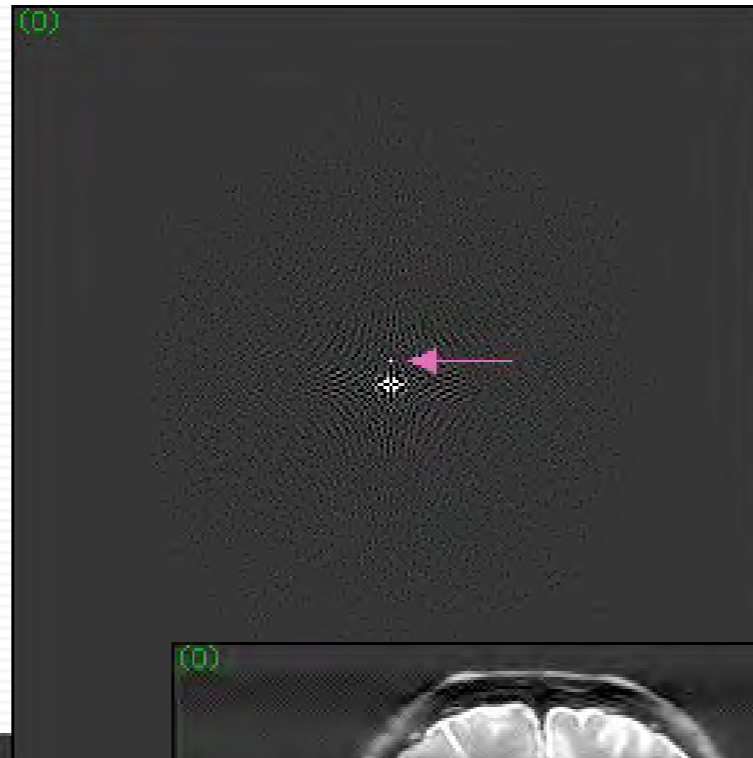
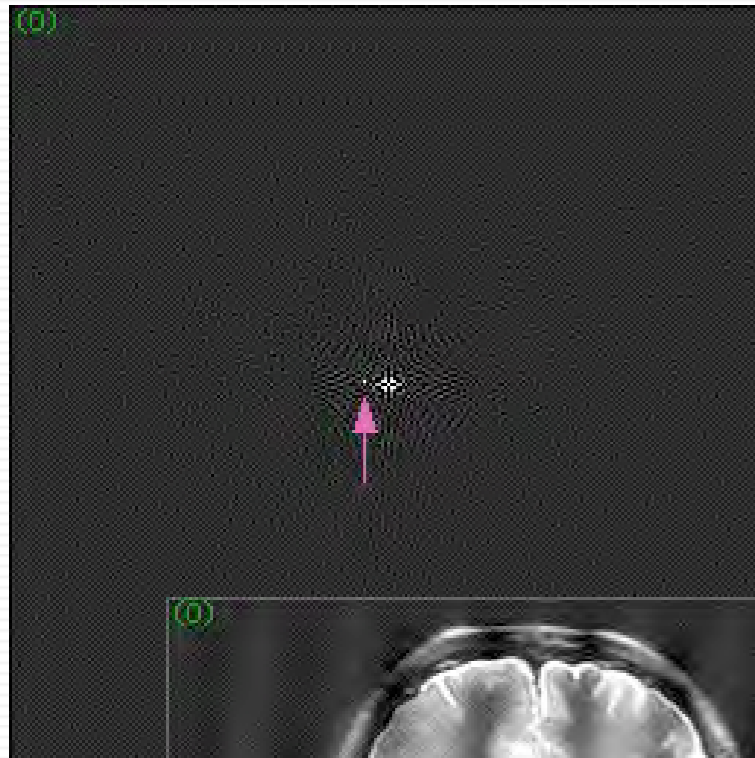


Image Quality

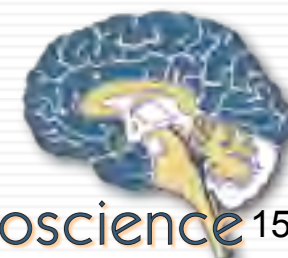


Image Quality

- SNR is Very Limited in MRI

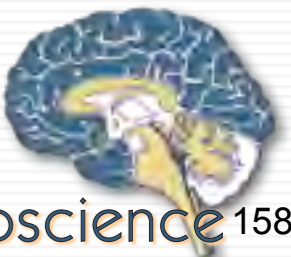


Image Quality

- SNR is Very Limited in MRI
- Feature Detection Falls Rapidly with Loss in Contrast to Noise Ratio

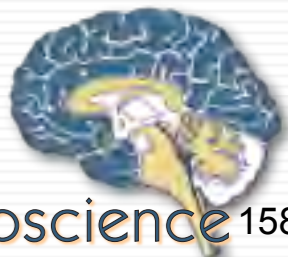


Image Quality

- SNR is Very Limited in MRI
- Feature Detection Falls Rapidly with Loss in Contrast to Noise Ratio
- Usable Resolution is NOT the Same as Voxel Size

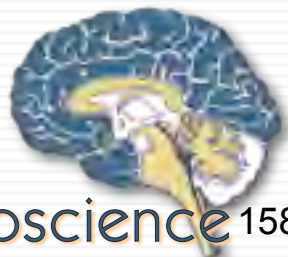


Image Quality

- SNR is Very Limited in MRI
- Feature Detection Falls Rapidly with Loss in Contrast to Noise Ratio
- Usable Resolution is NOT the Same as Voxel Size
- Spatial Encoding Artifacts in MRI May Have Complex Appearance

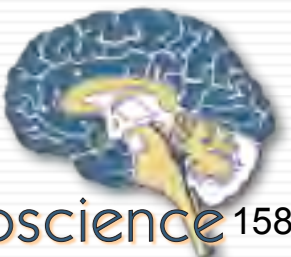
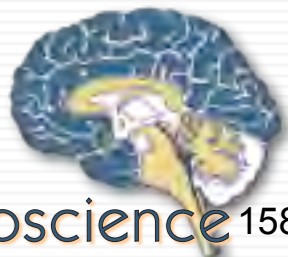


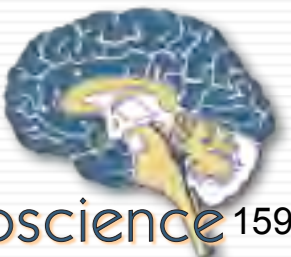
Image Quality

- SNR is Very Limited in MRI
- Feature Detection Falls Rapidly with Loss in Contrast to Noise Ratio
- Usable Resolution is NOT the Same as Voxel Size
- Spatial Encoding Artifacts in MRI May Have Complex Appearance
- Edge Ringing and Blurring are Related to Parameters Such as Contrast



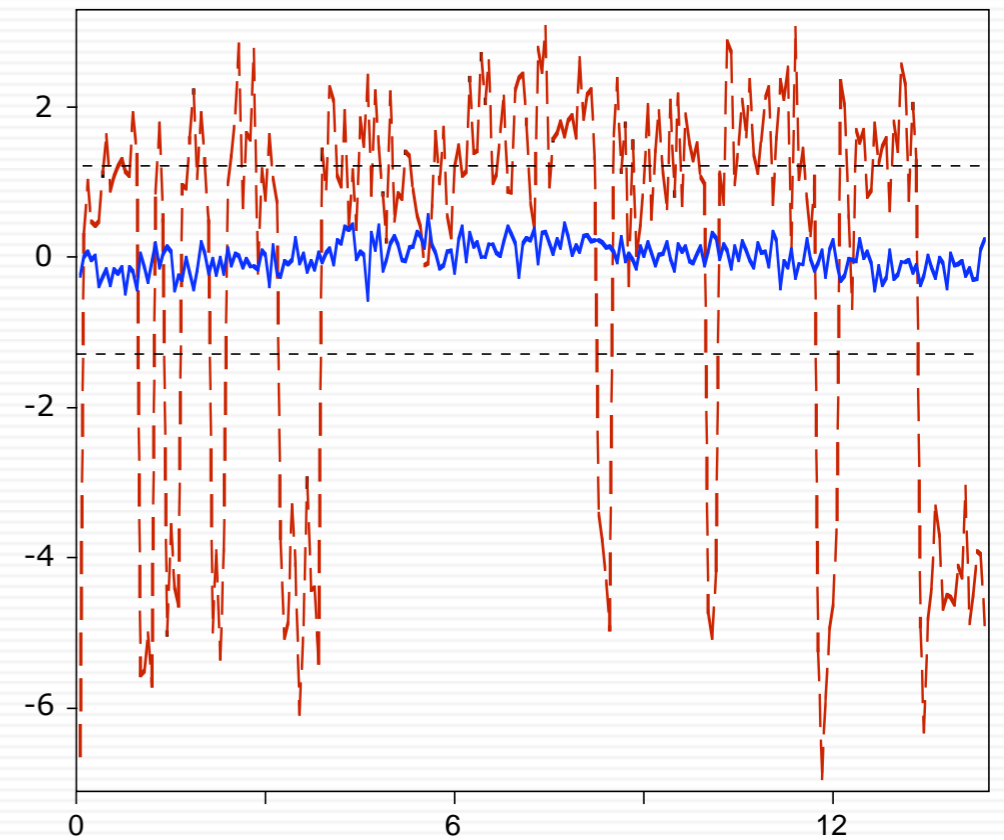
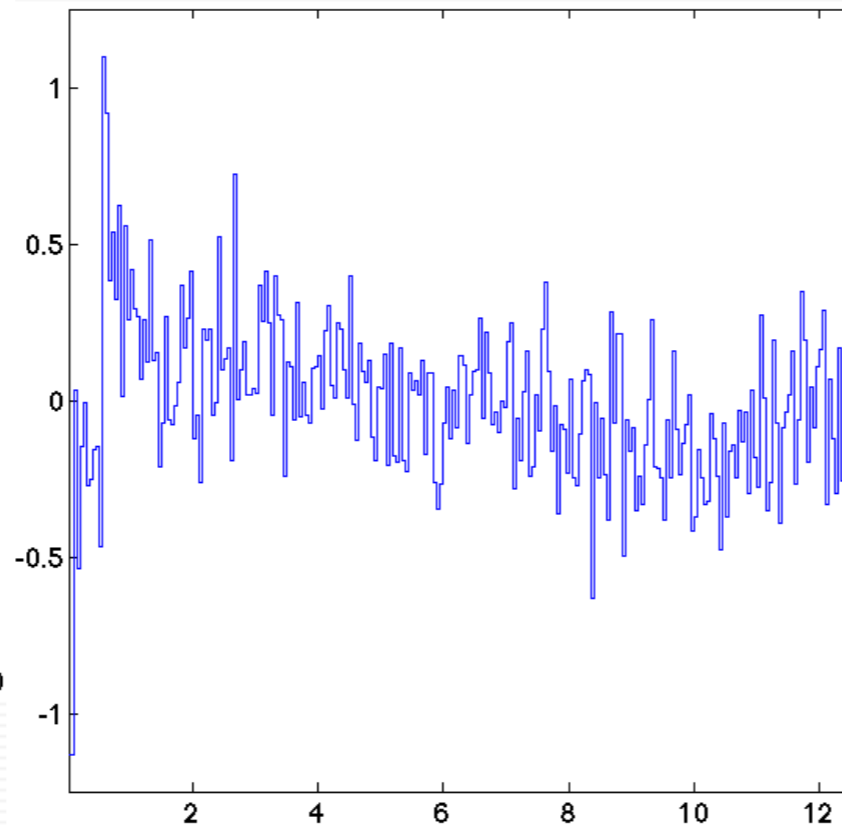
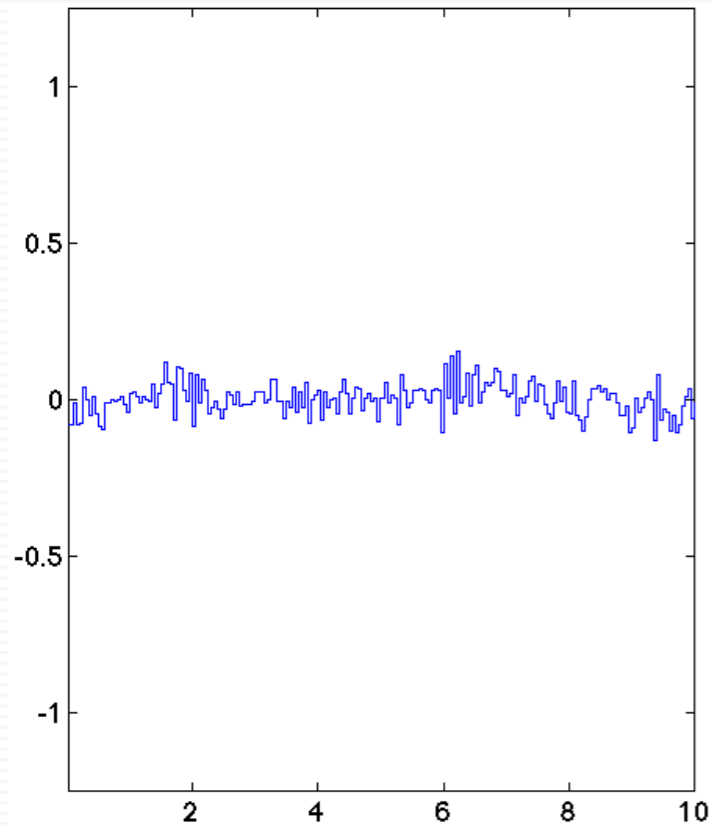
Characterize Your Tools

- Test Statistics are Effect/Variance
- Variance includes:
 - Intrasubject (motion, attention, physiology, fatigue,...)
 - Intersubject variance (position, morphology, performance, pathology, physiology,...)
 - Experimental Variance (uncontrolled variables, stimulation variance,...)
 - Instrument Variance
 - Sitewise Variance
 - True Random Noise

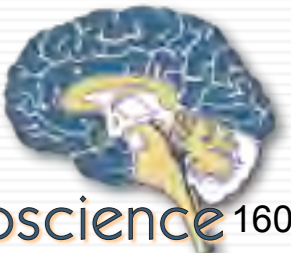


Instrument Variation

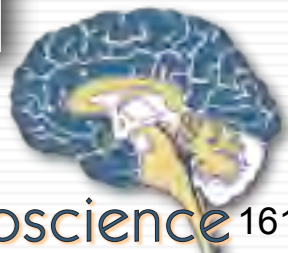
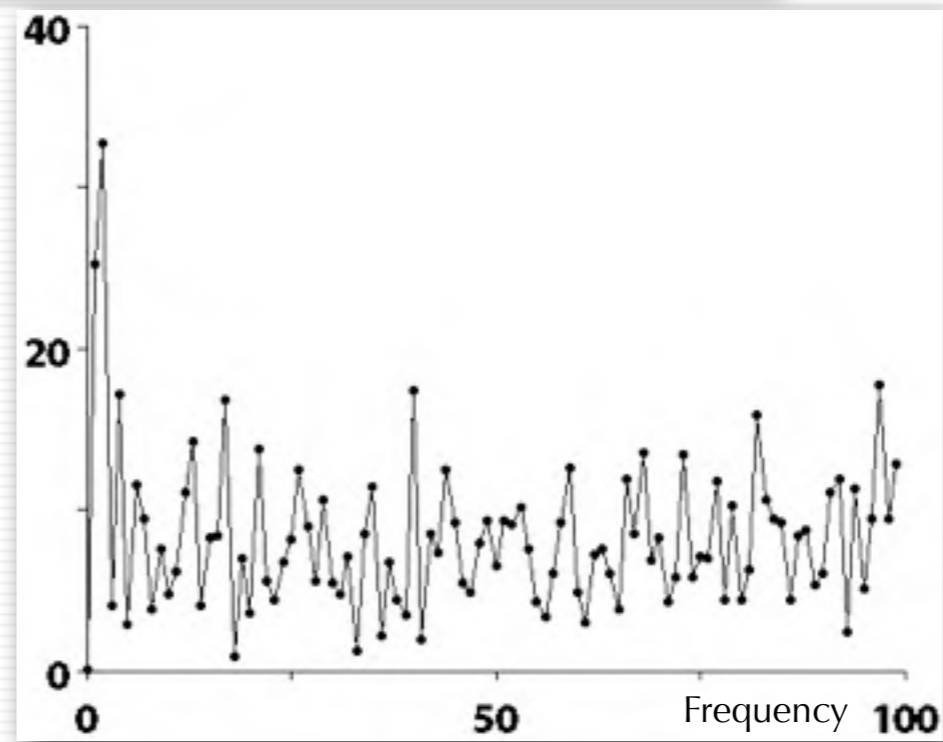
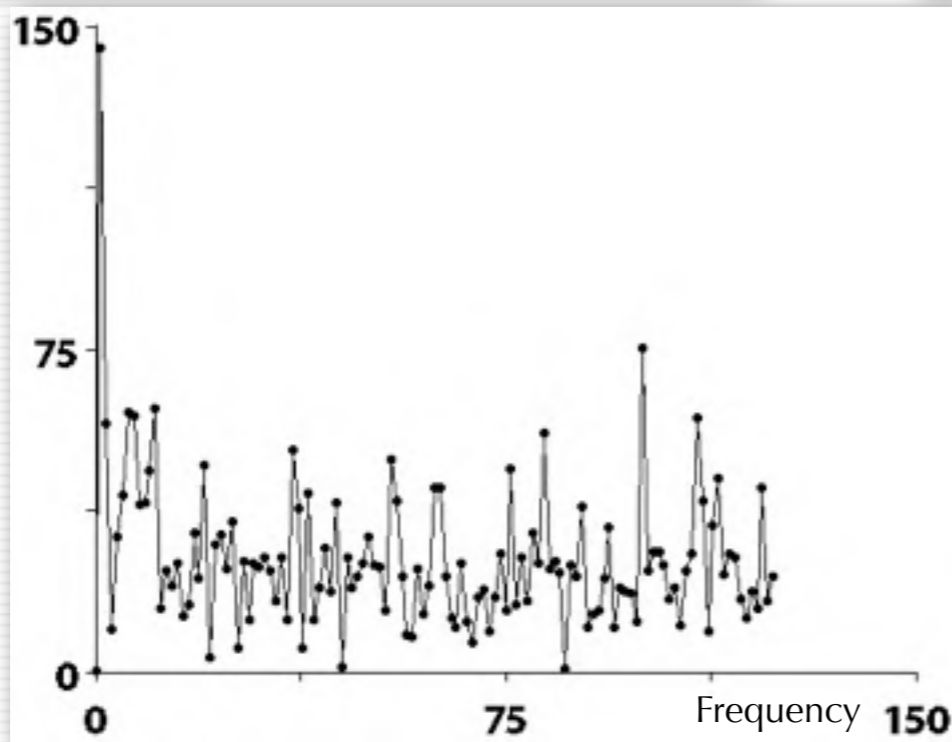
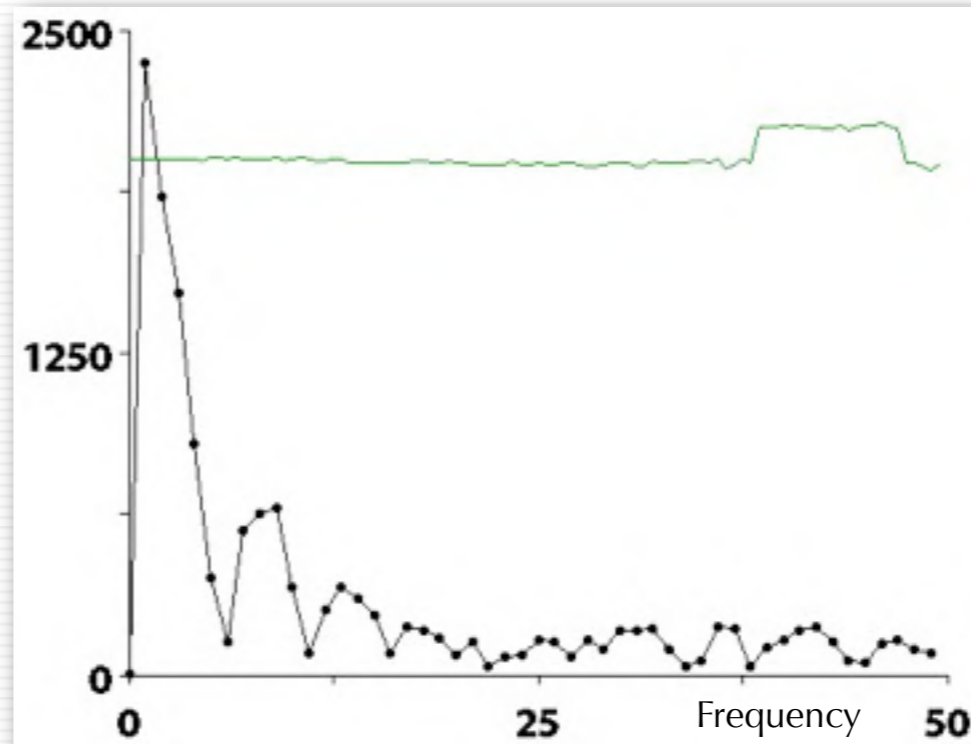
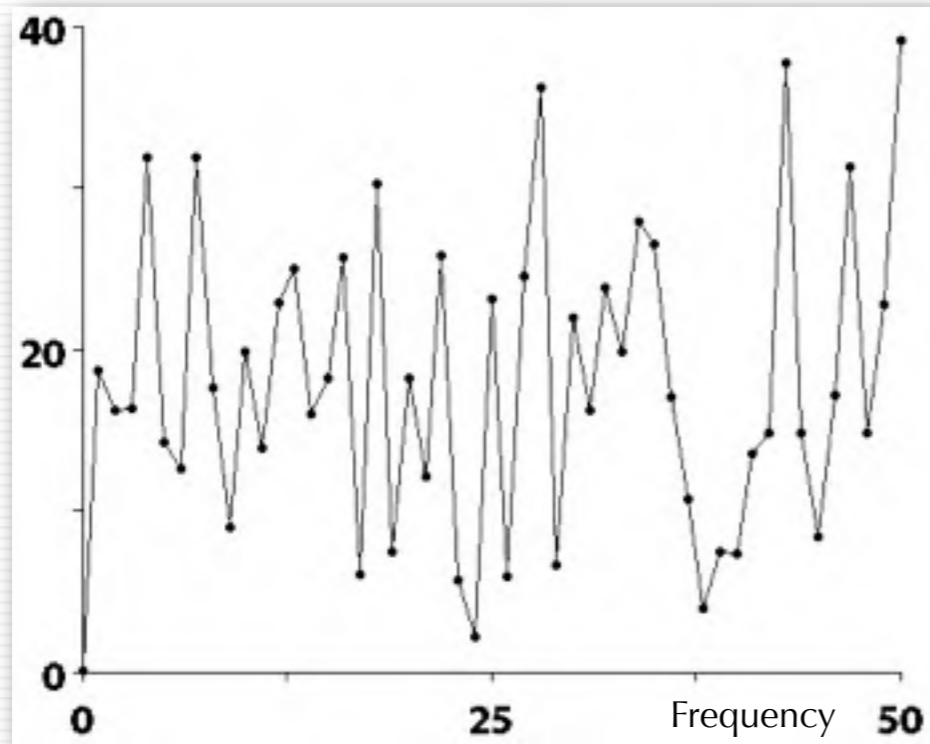
1. System Instability



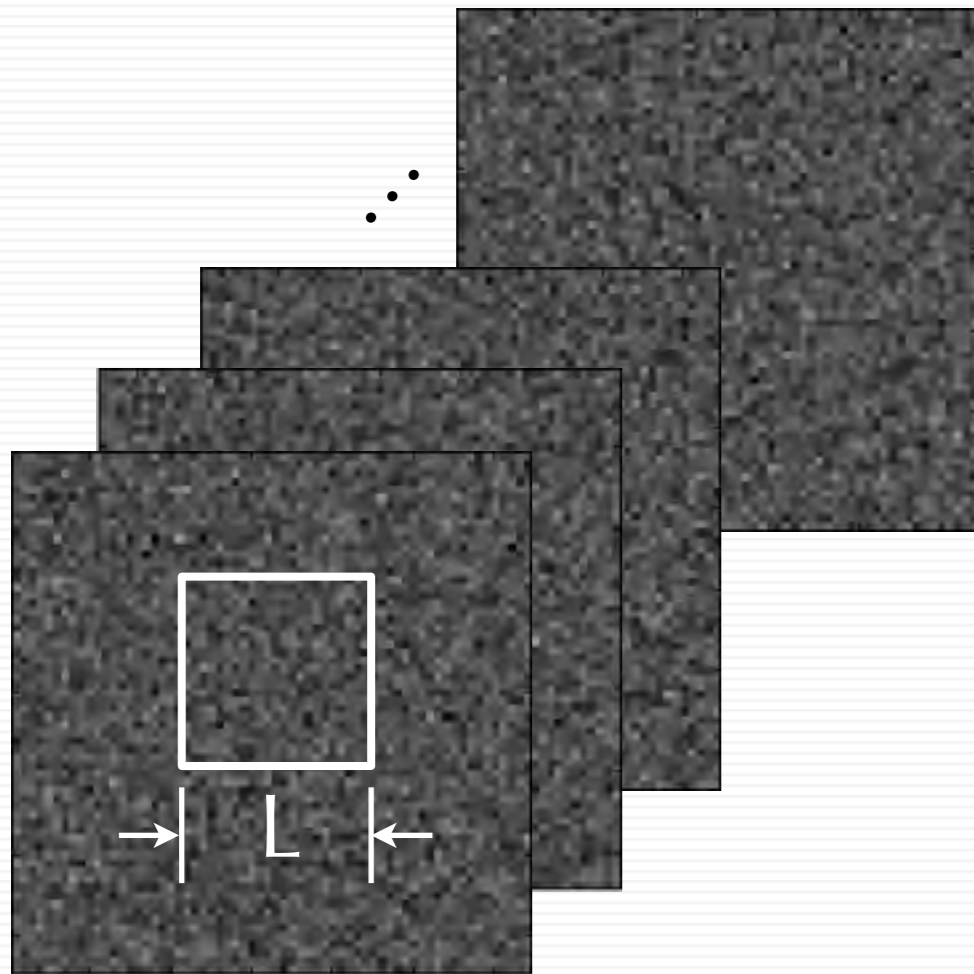
Mean Intensity Variation



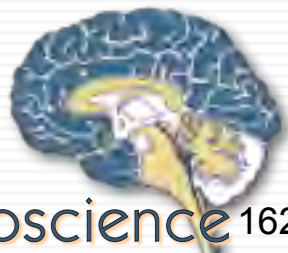
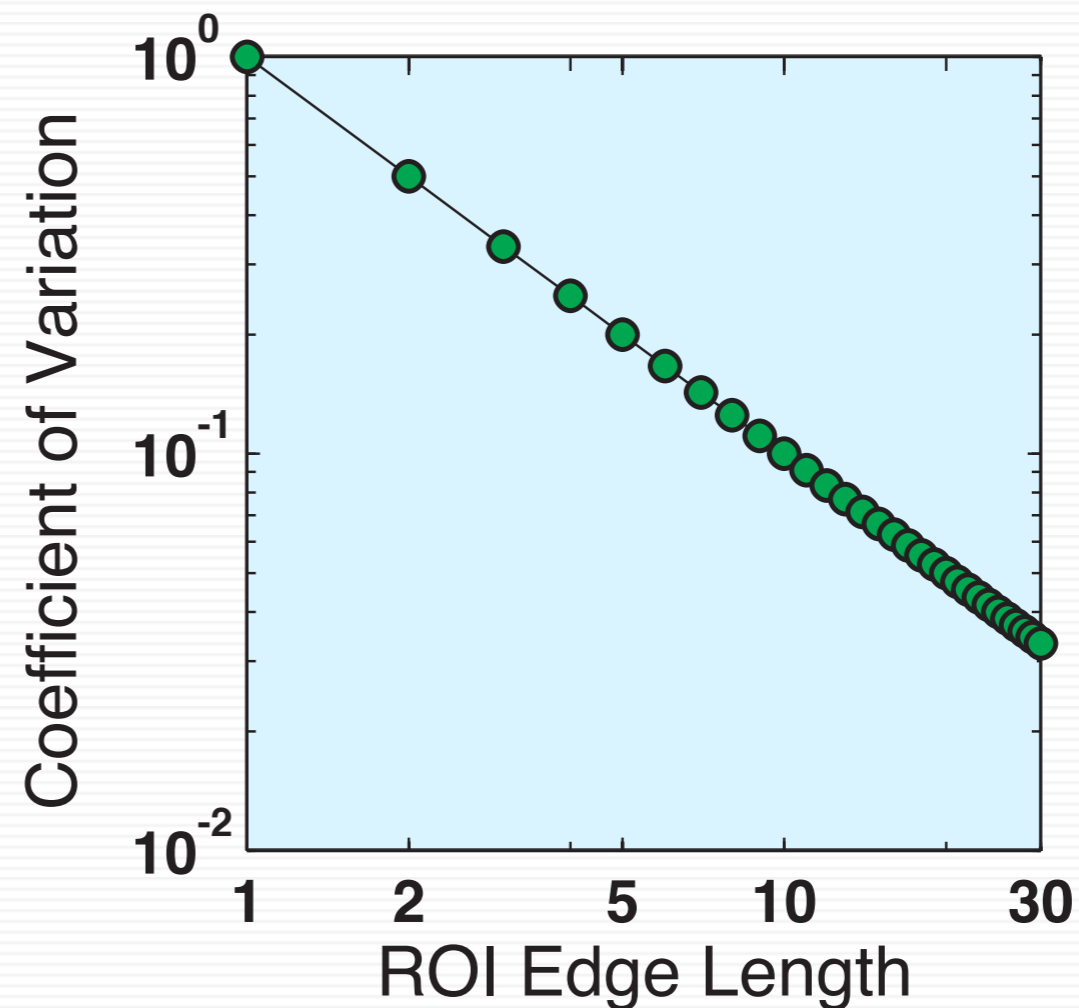
Scanner Autocorrelation



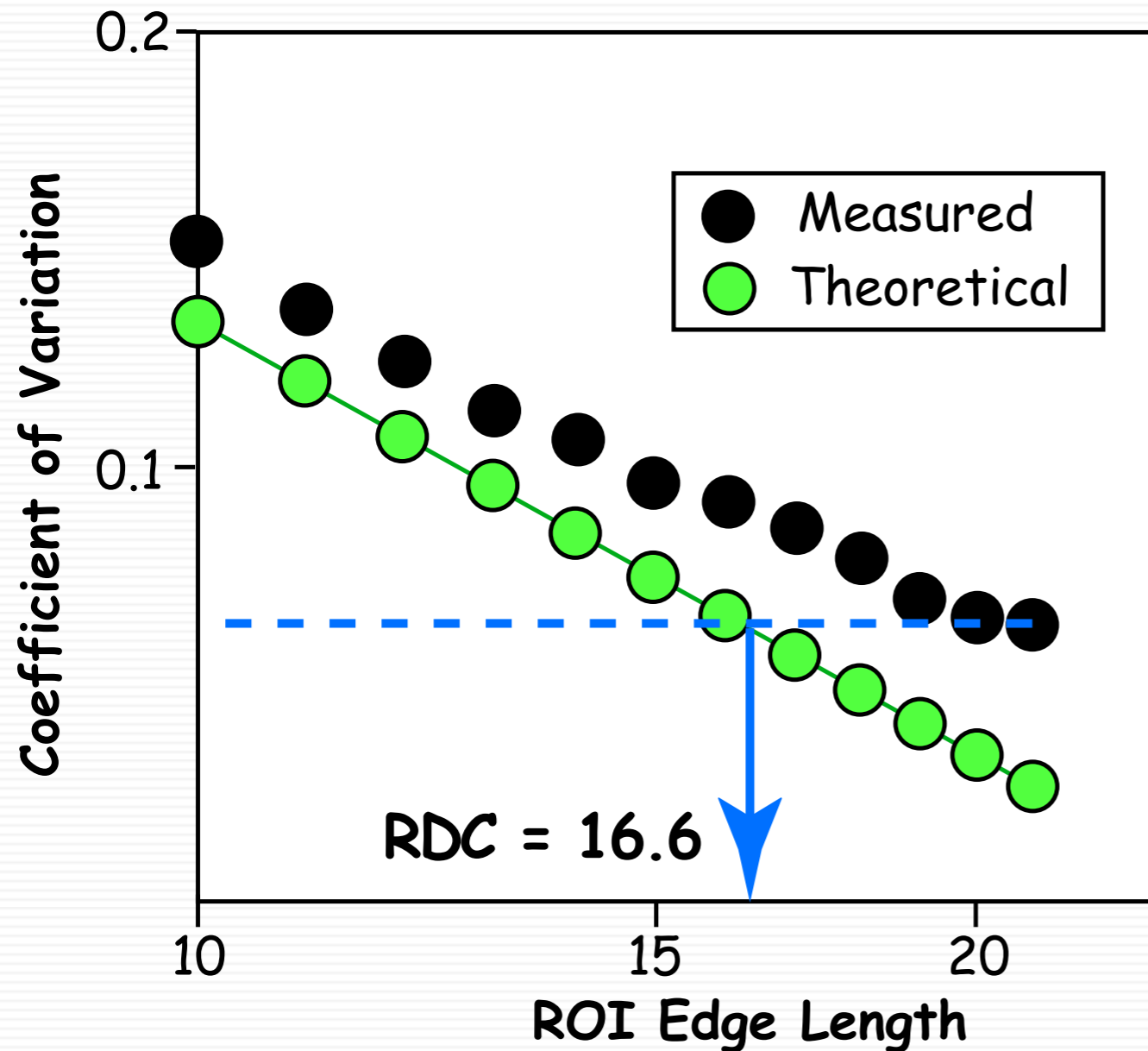
the Weisskoff Plot



The Expected Standard Deviation of the Mean Signal of a Region over Time Falls with the Square Root of the Number of Voxels.

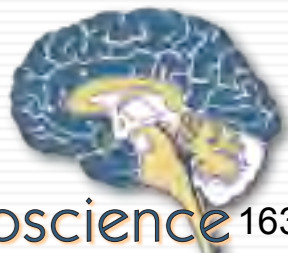


the Weisskoff Plot



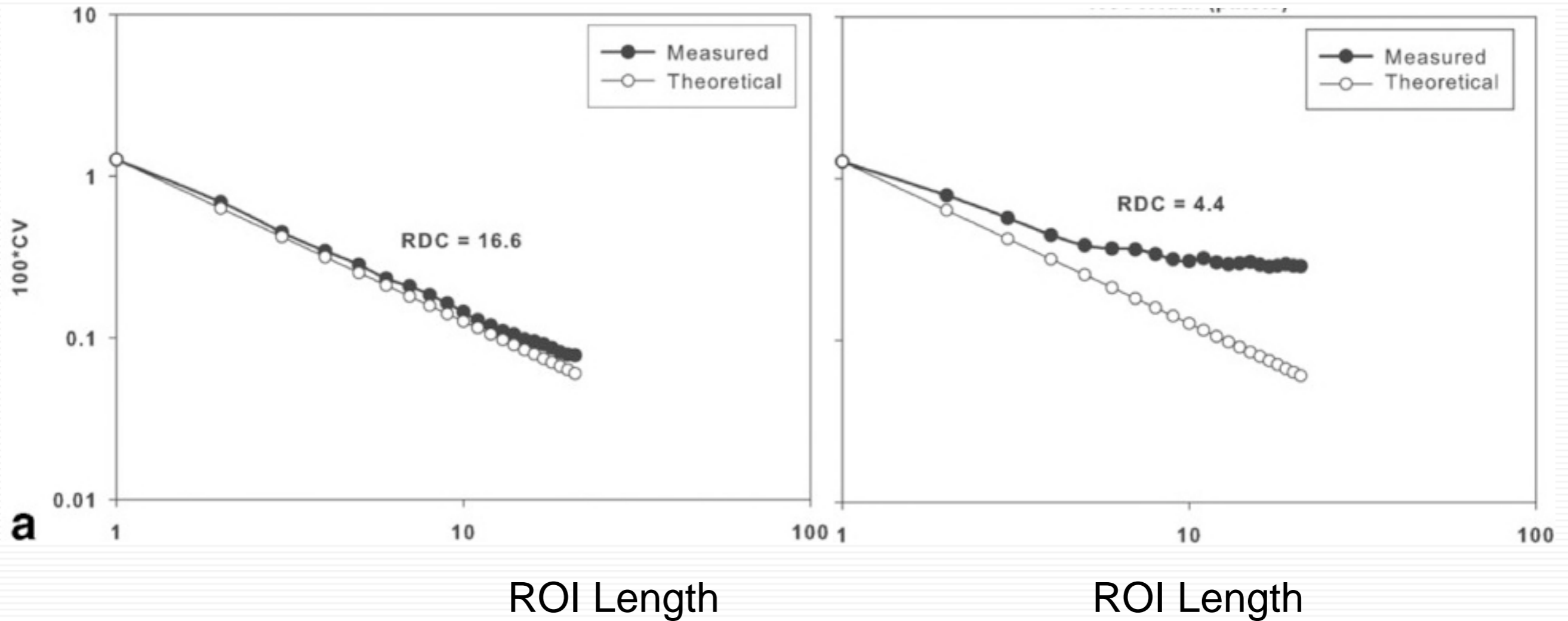
Deviations from the Theoretical Curve are Evidence of Correlated Noise

RDC (*Radius of Decorrelation*) is a Single Point Quantification of the Weisskoff Plot

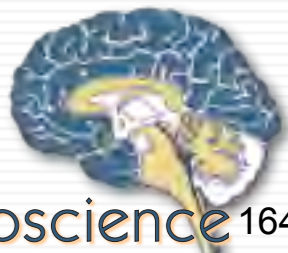


Weisskoff Plot

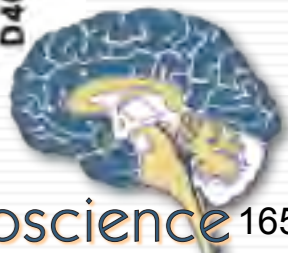
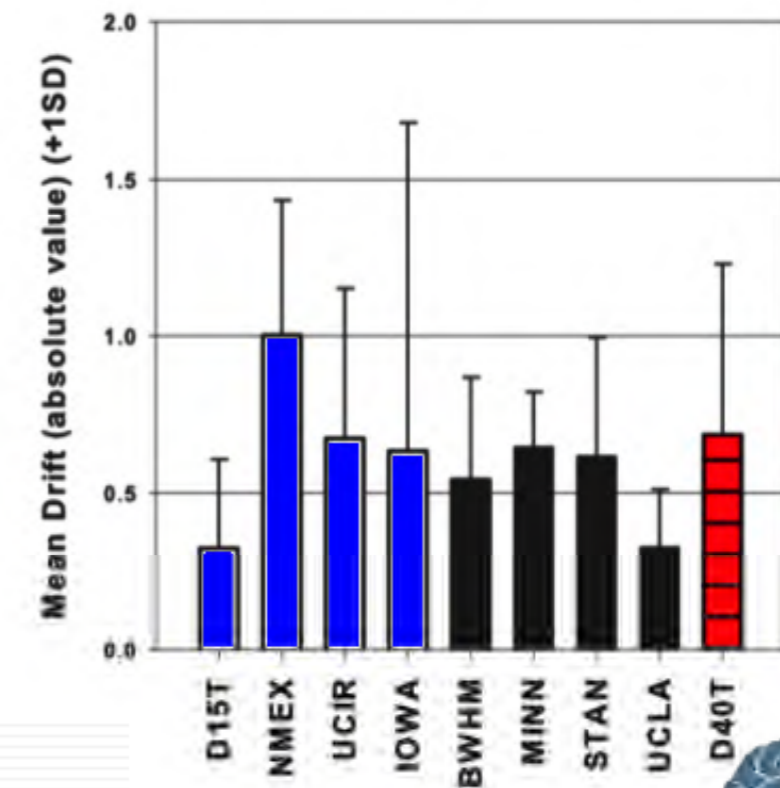
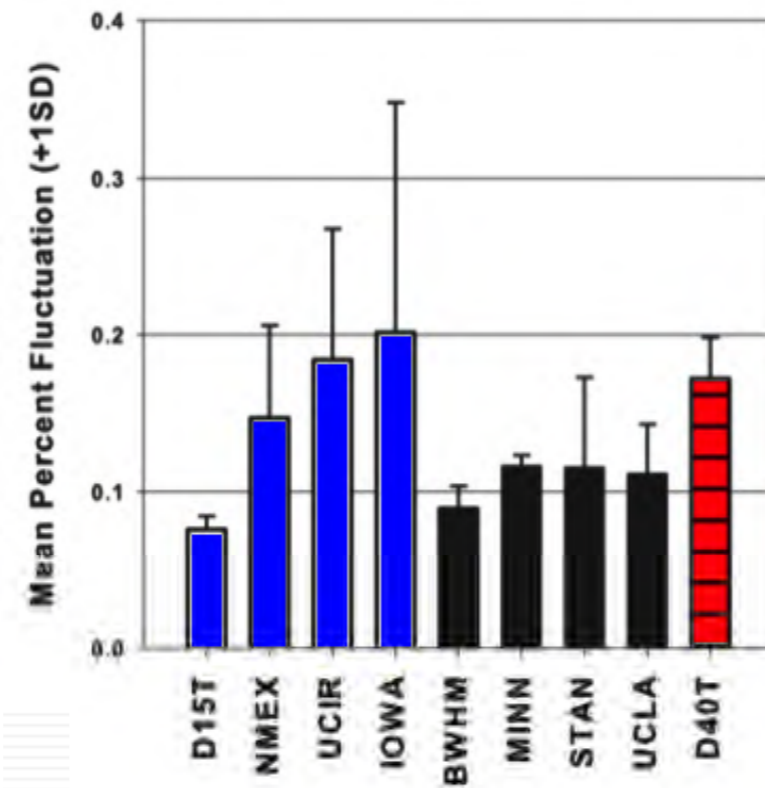
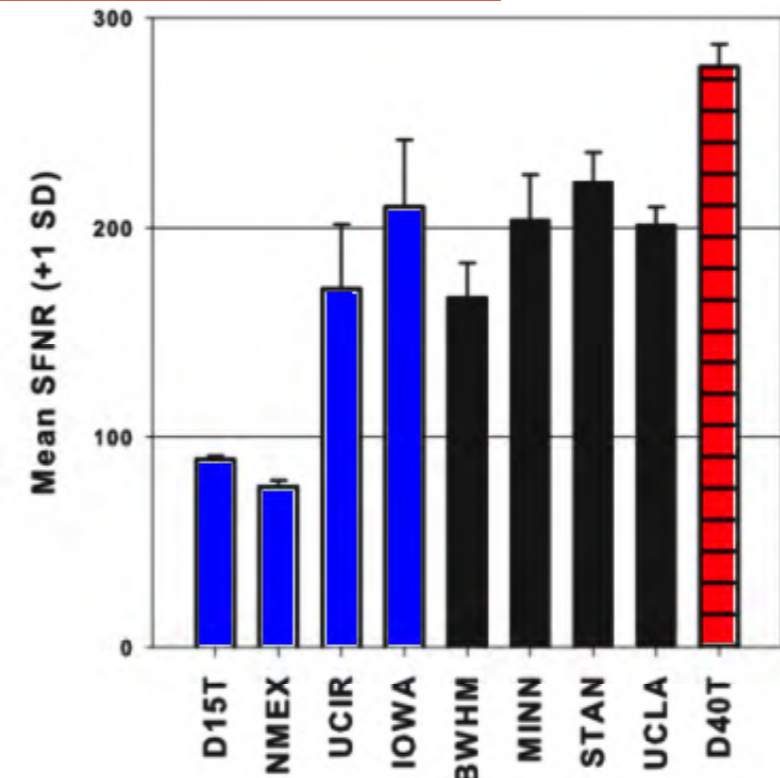
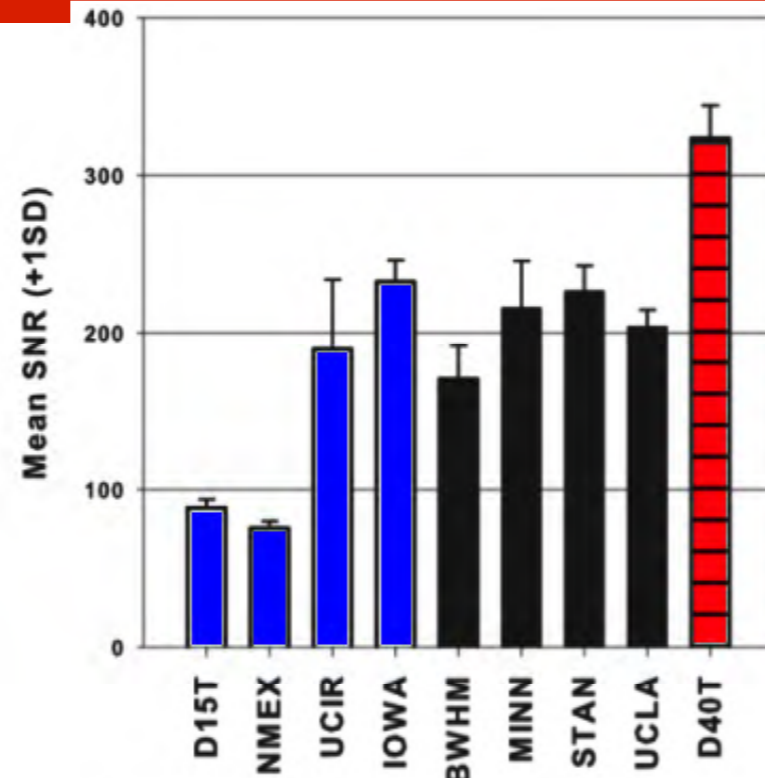
Weisskoff R. Magn Reson Med 36:643



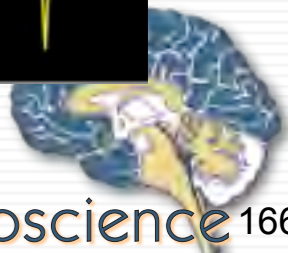
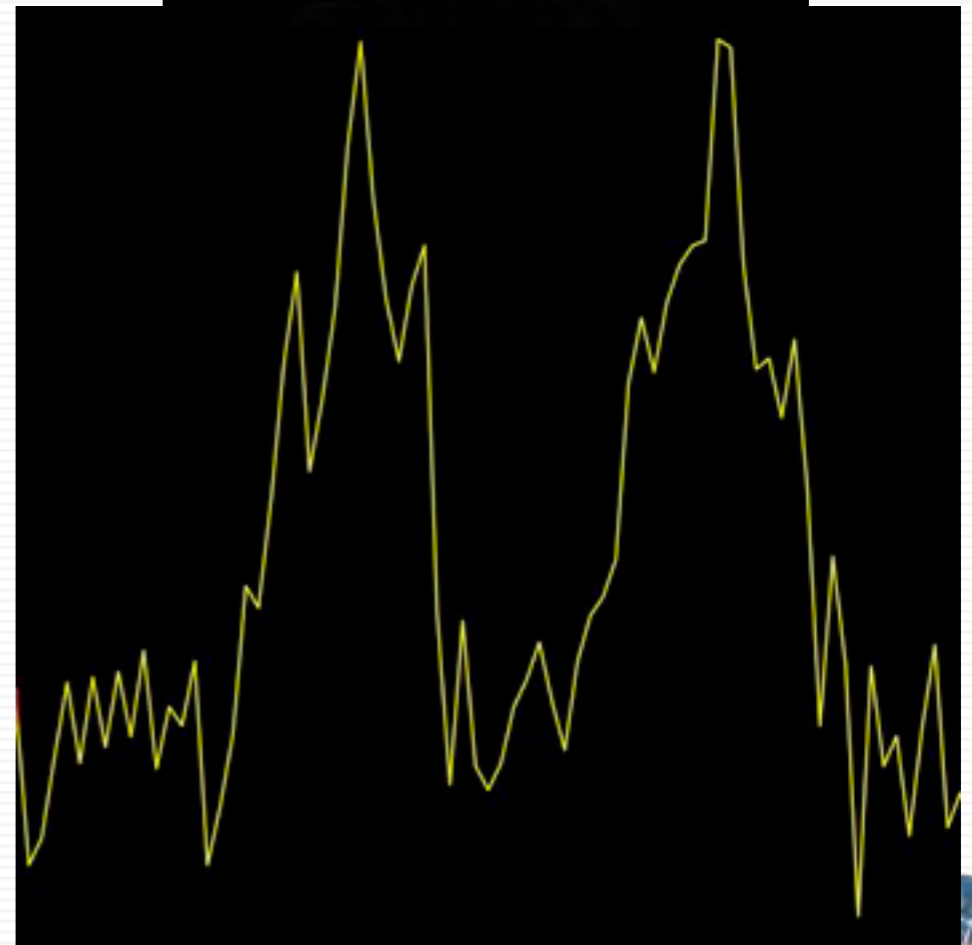
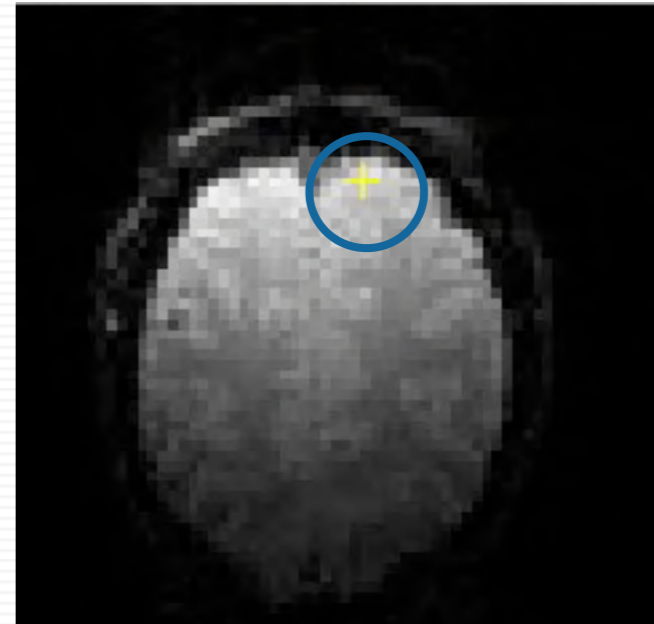
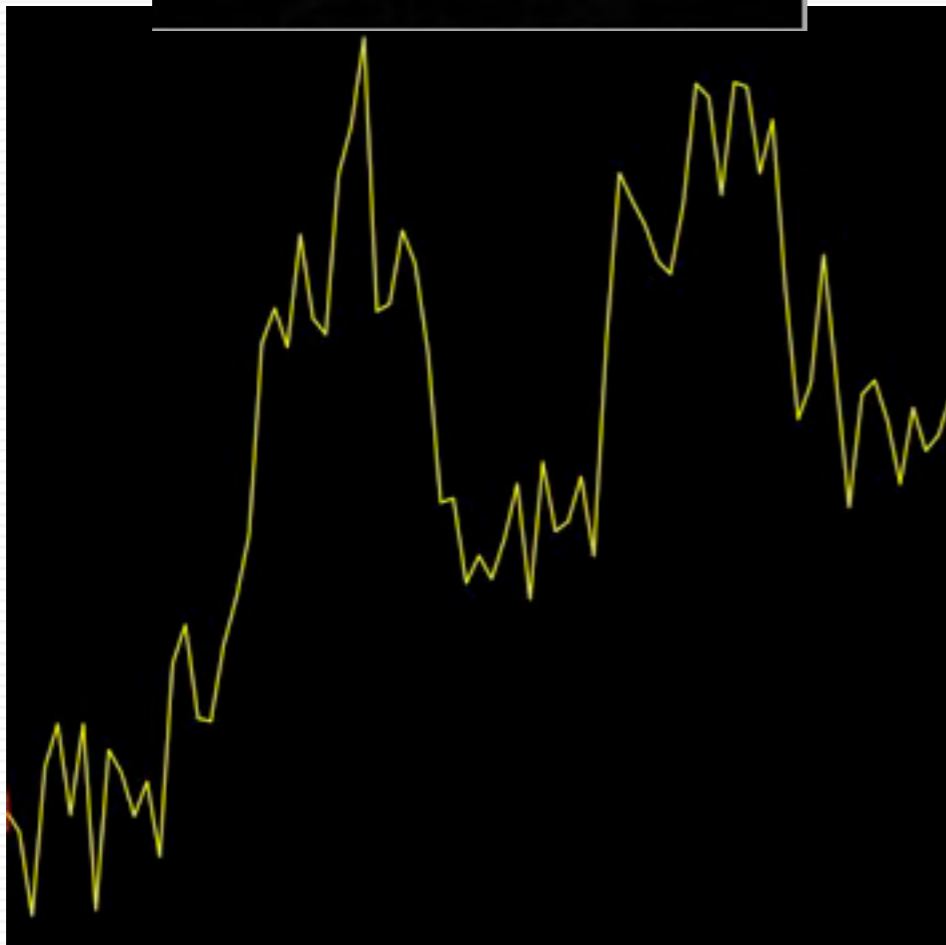
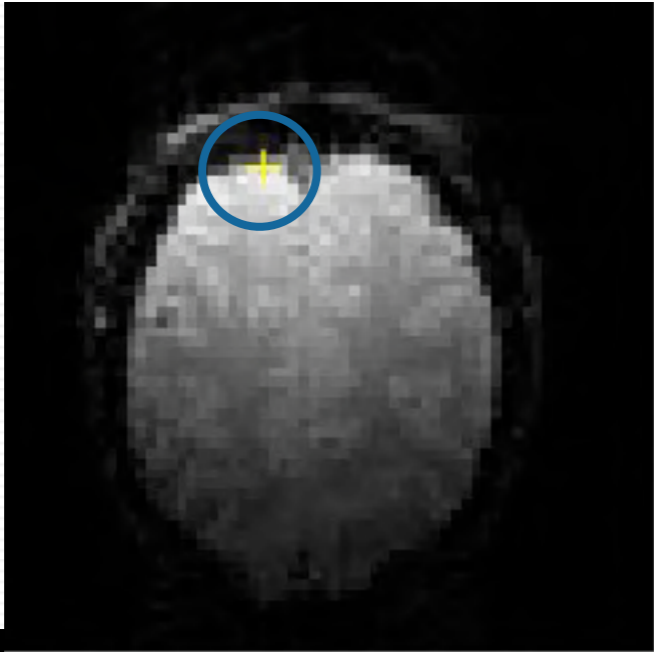
Friedman and Glover, JMRI 23:827



Scanner Comparisons

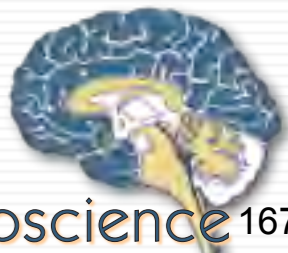
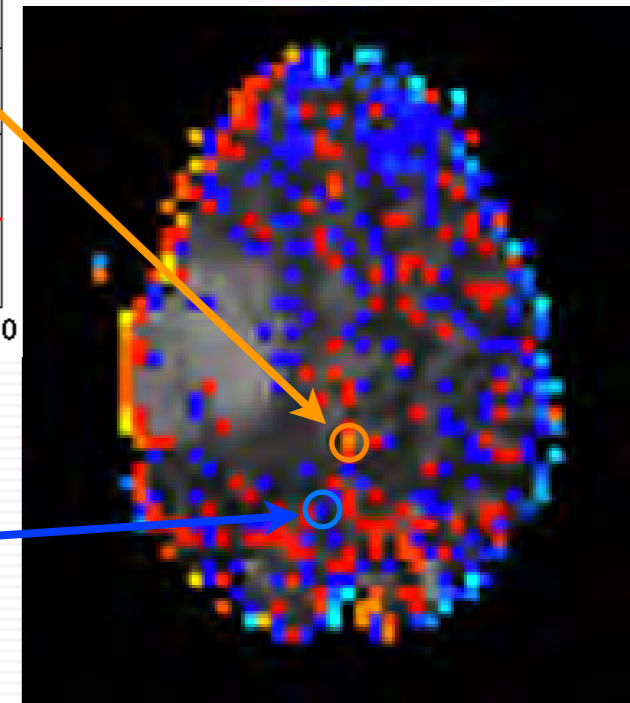
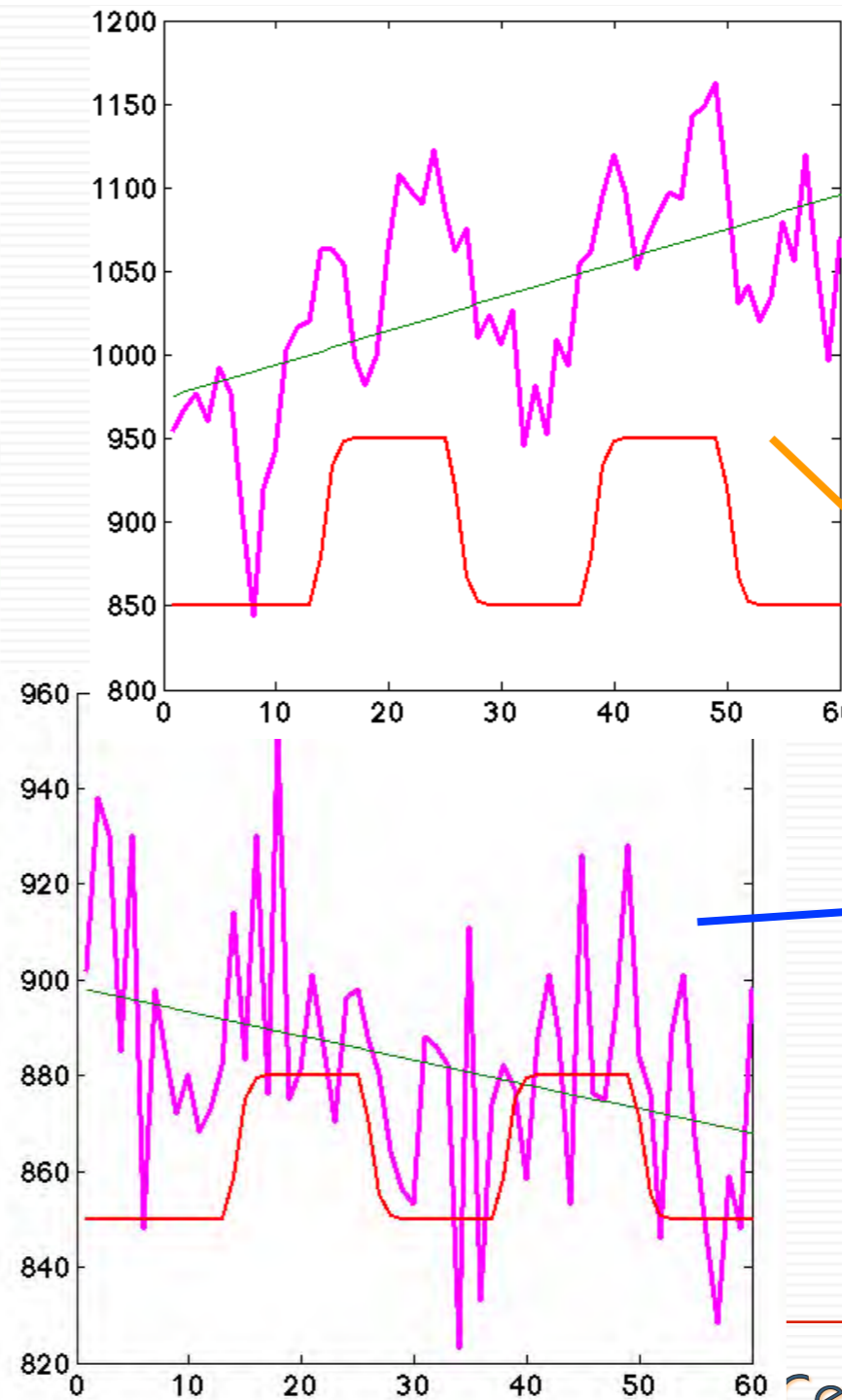
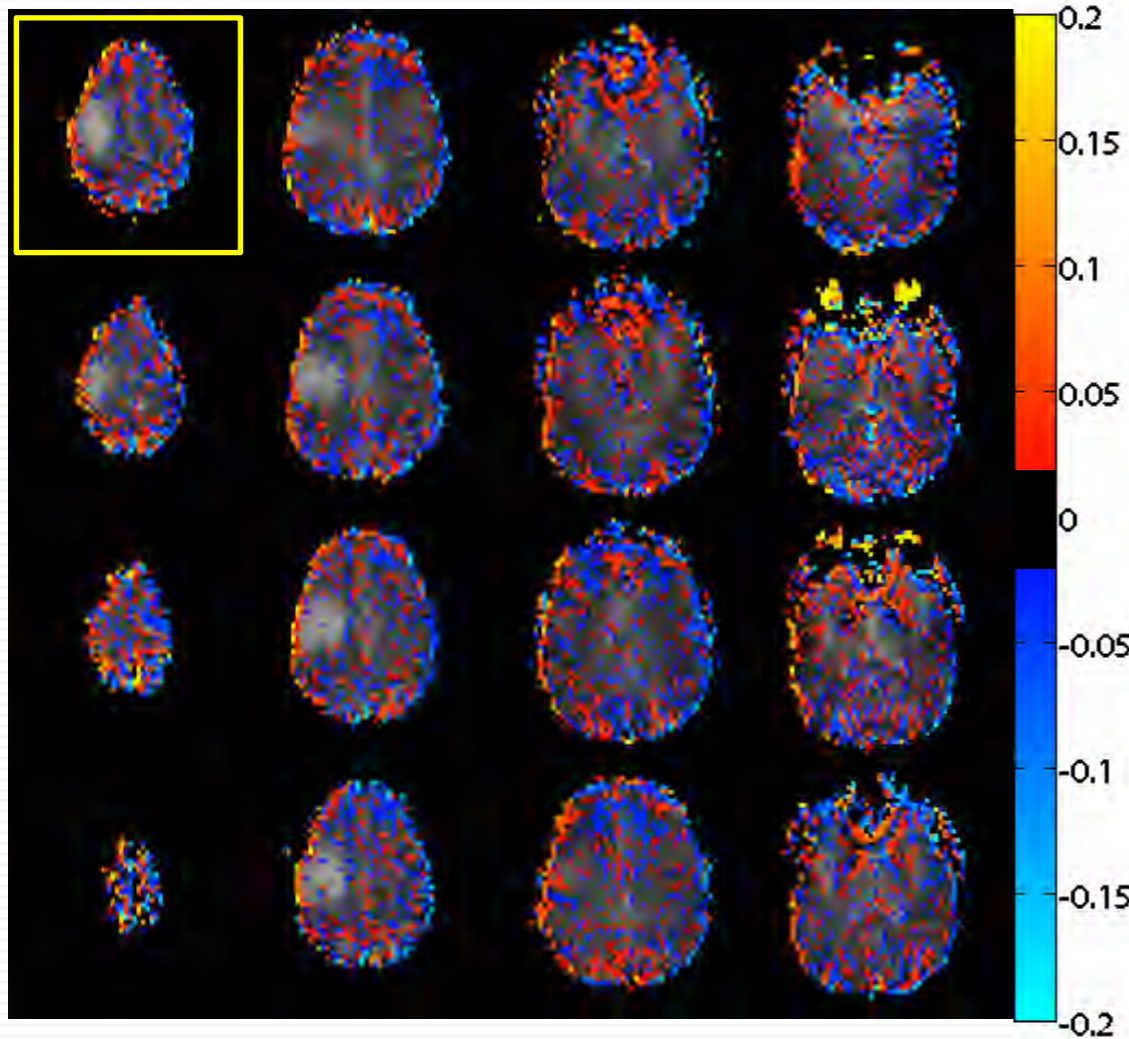


“Drift”

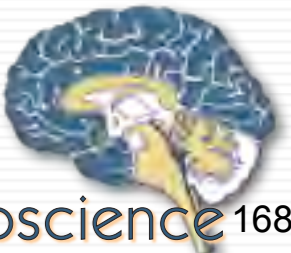
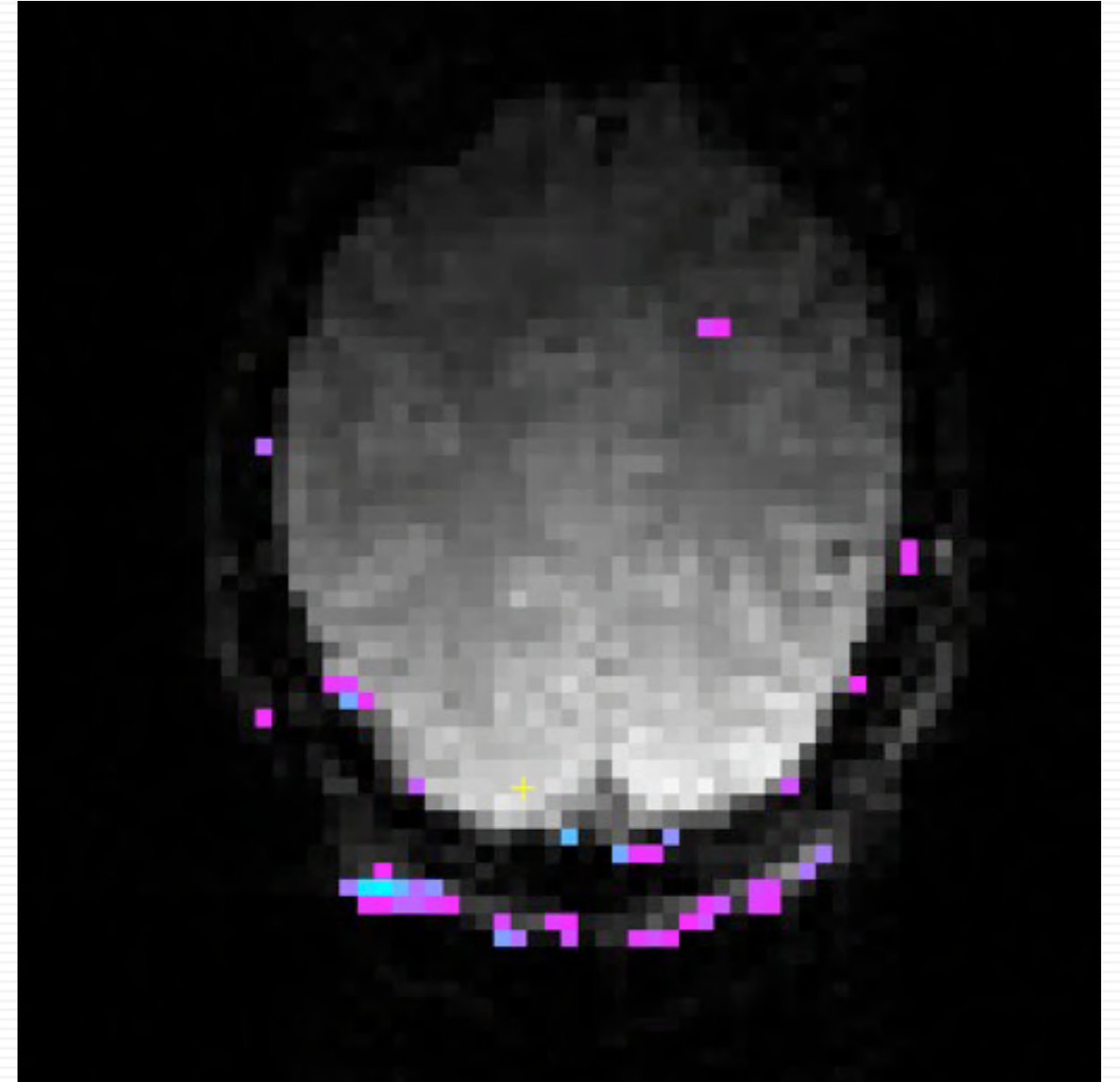
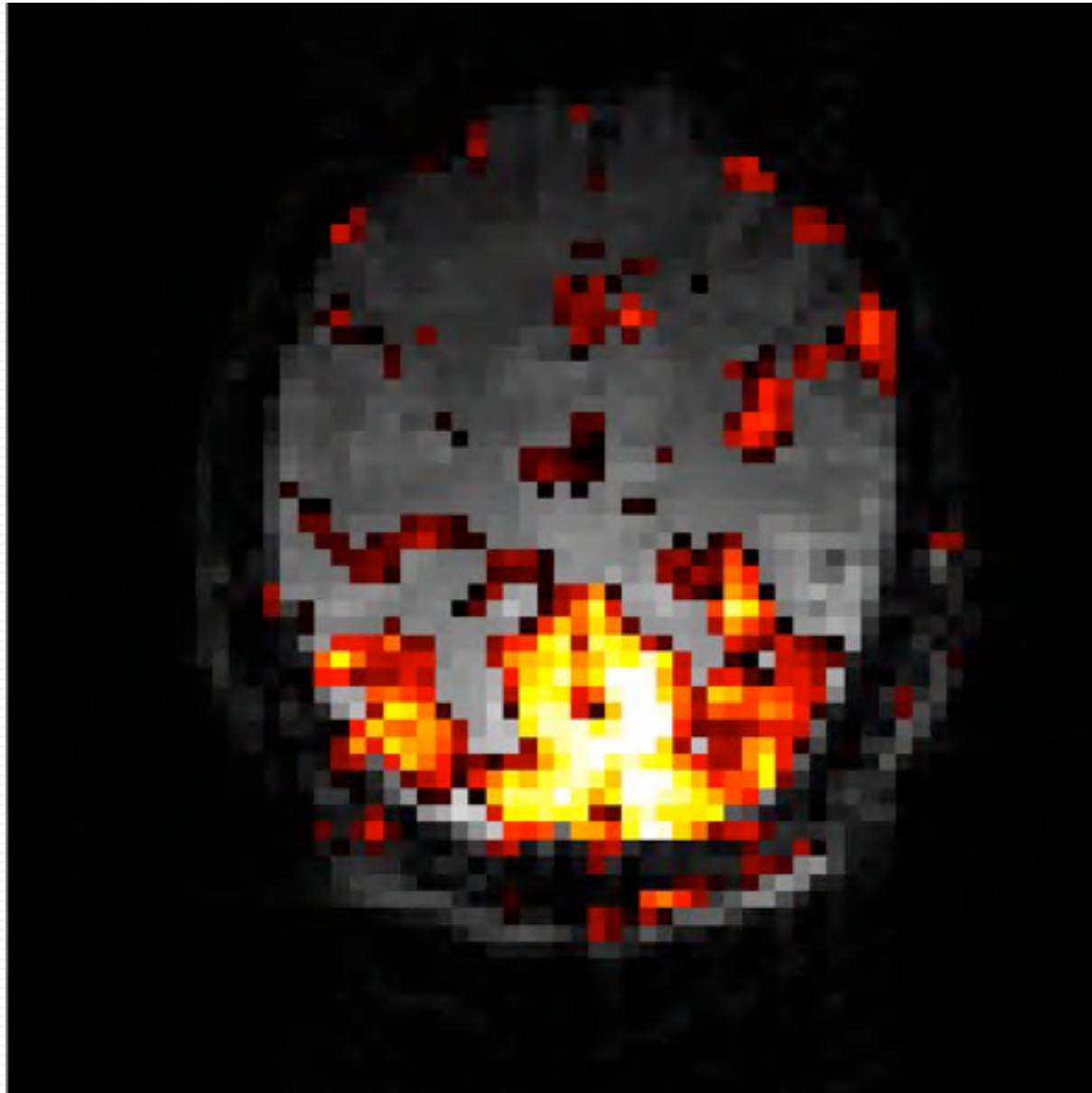


Instrument Variation

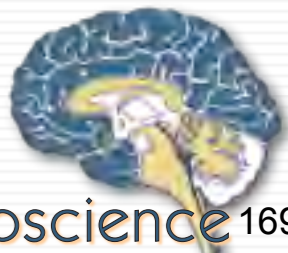
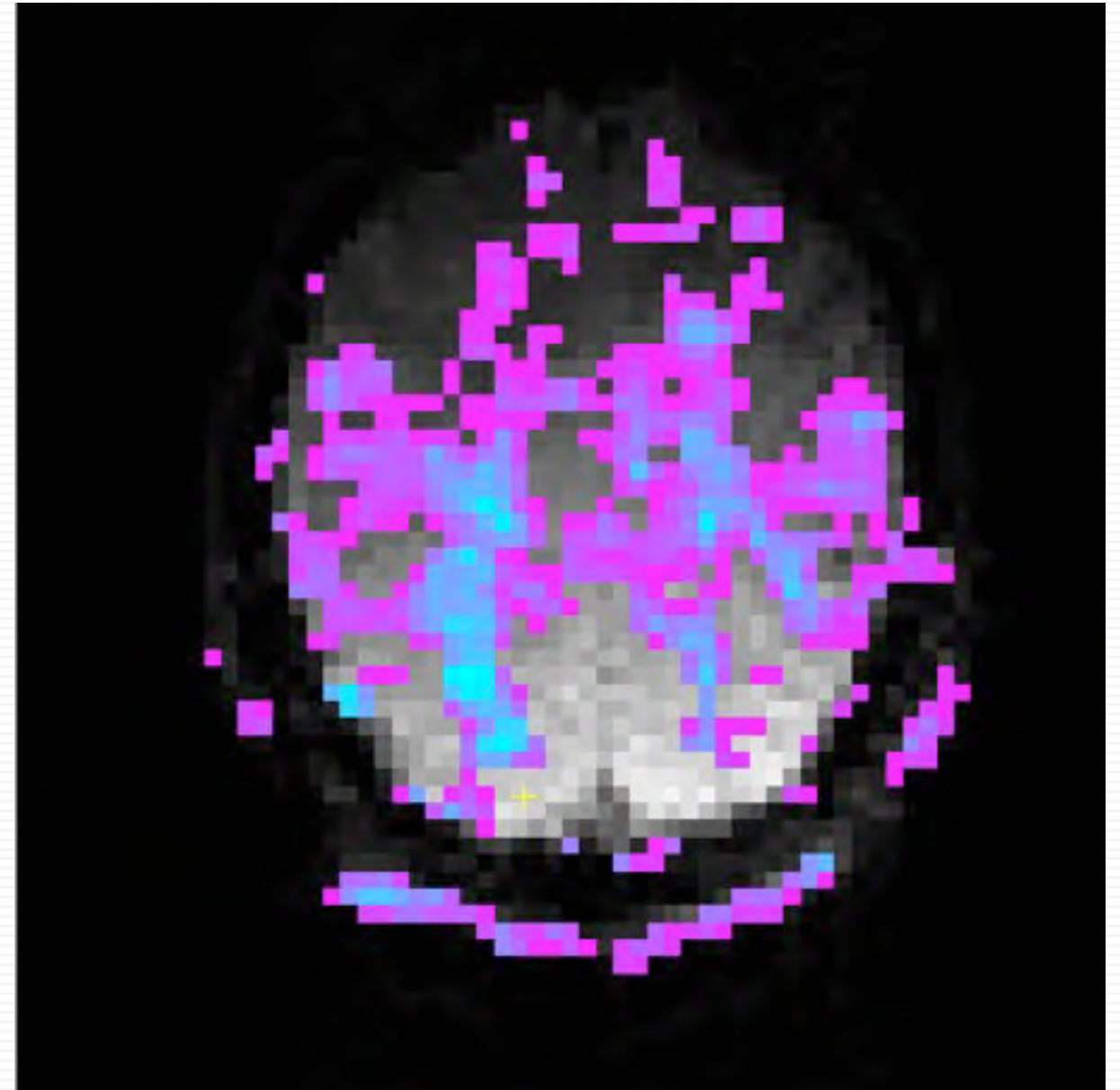
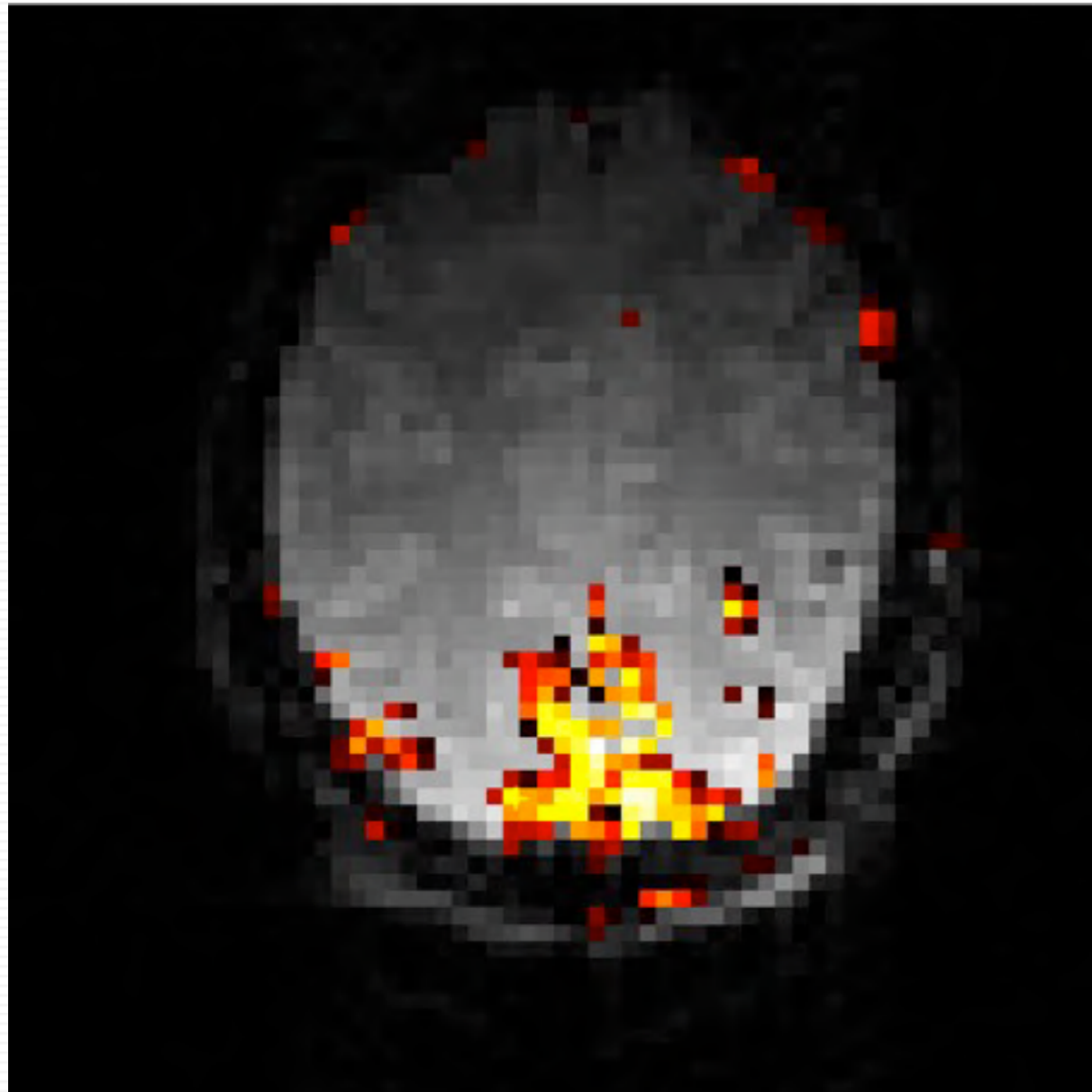
2. The mystery of scanner drift.



Global Mean Scaling - OFF



Global Mean Scaling - ON



Thermal Noise

■ Noise Distribution in MRI is **Rician**

□ $Signal = \sqrt{(\Re + \sigma_1)^2 + (\Im + \sigma_2)^2}$

■ Background should be **Rayleigh** Noise $(\Re = \Im = 0)$

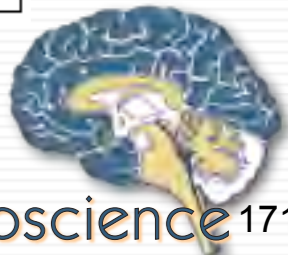
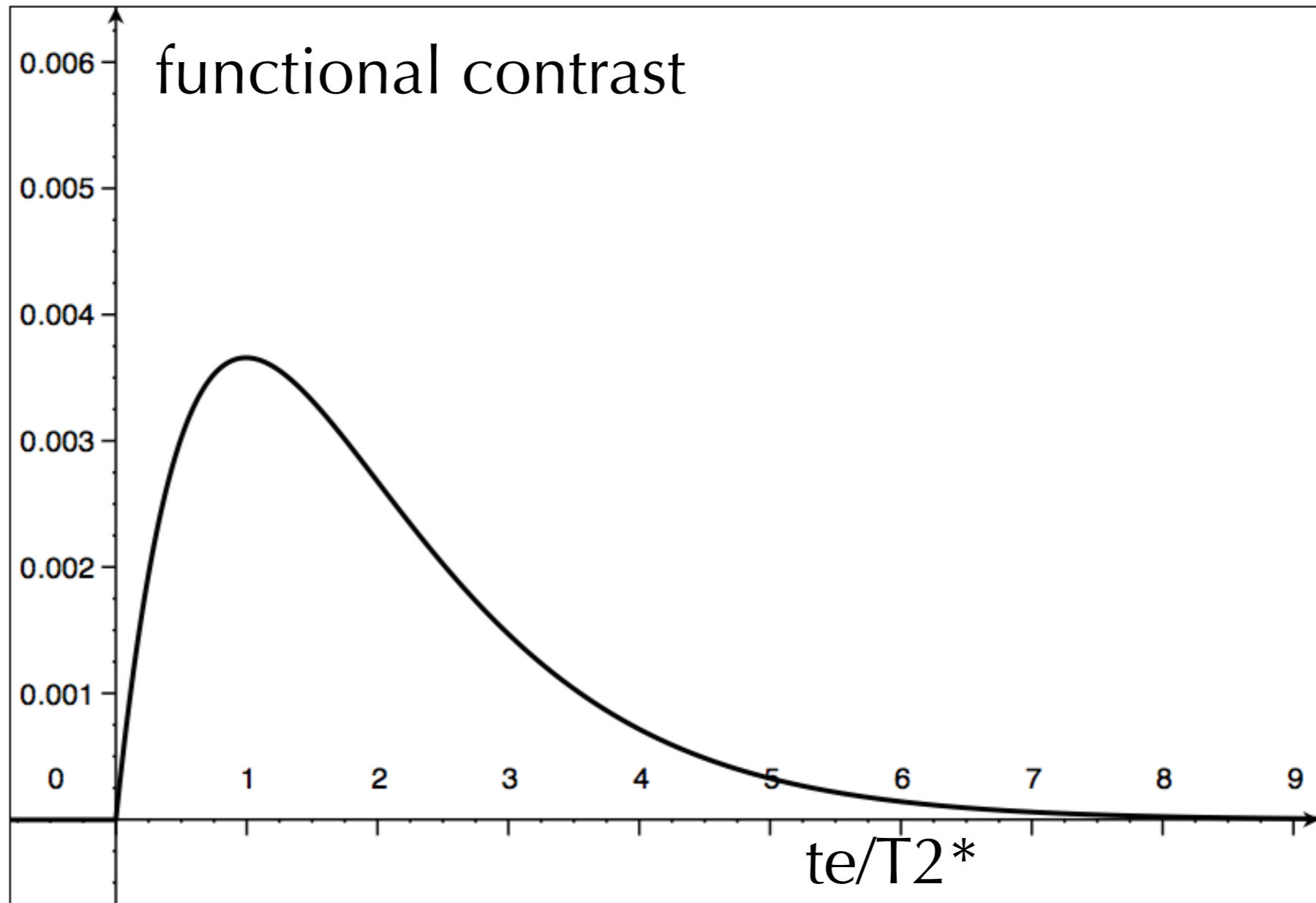
□ Expected μ : $\sigma \sqrt{\frac{\pi}{2}}$ expected variance: $\frac{4 - \pi}{2} \sigma^2$

□ $\left\langle \frac{\mu}{\sqrt{\text{variance}}} \right\rangle = \frac{\sqrt{\pi}}{\sqrt{4 - \mu}}$

■ Deviations from This Model Imply Coherent Artifacts

Parameter Optimization

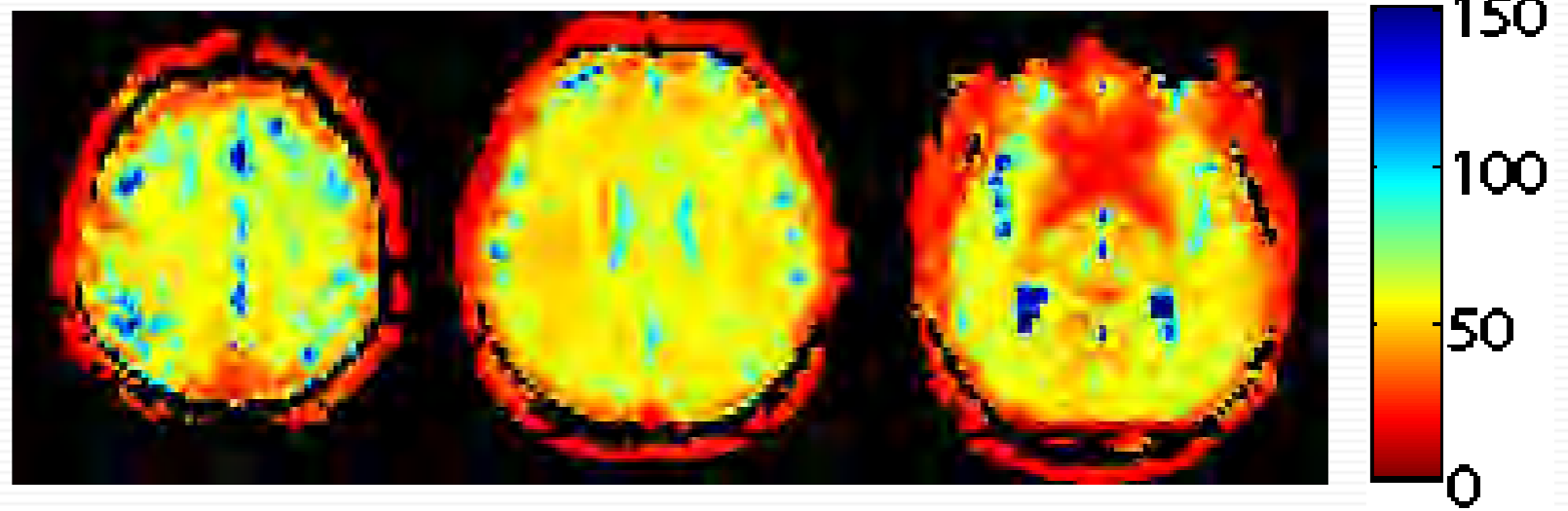
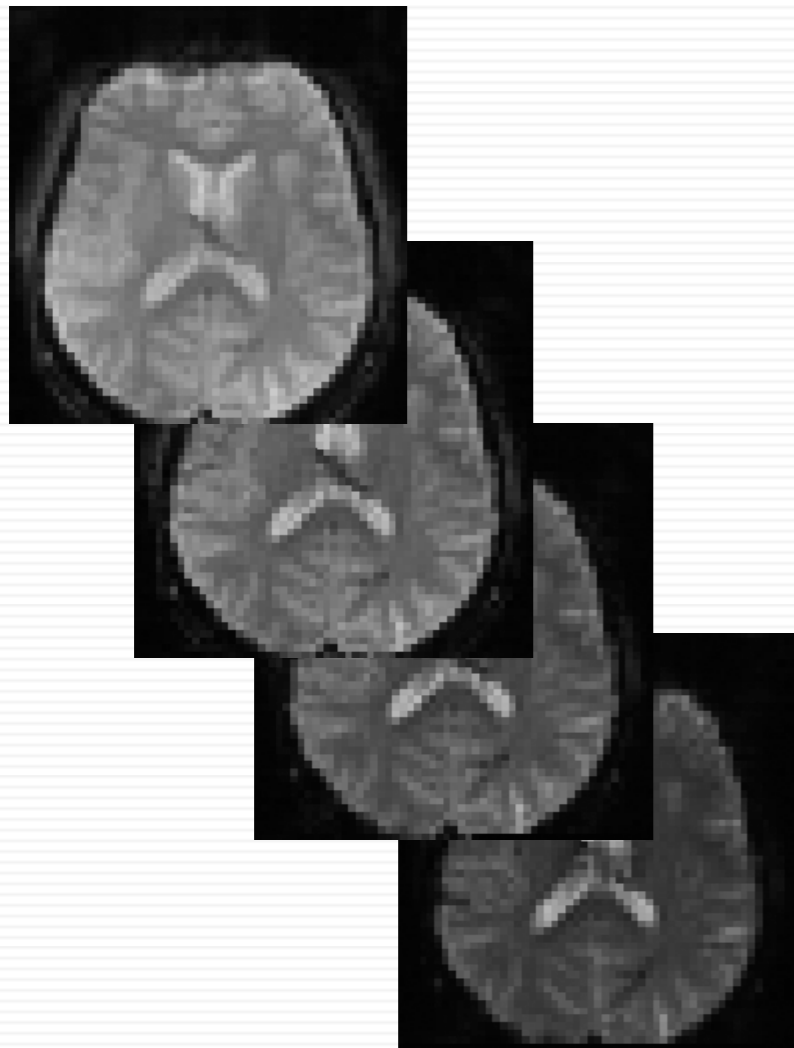
- Best BOLD contrast when $te = T2^*$



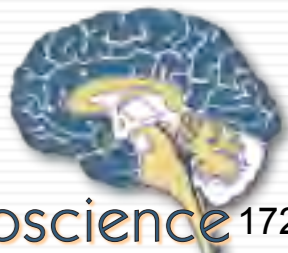
Parameter Optimization

- Best BOLD contrast when $te = T2^*$

- $$\frac{d \ln(\text{Signal})}{d(te)} = \frac{-1}{T2^*}$$

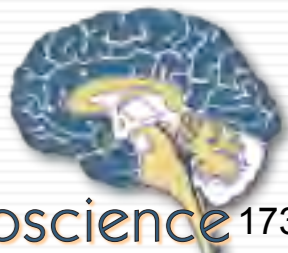
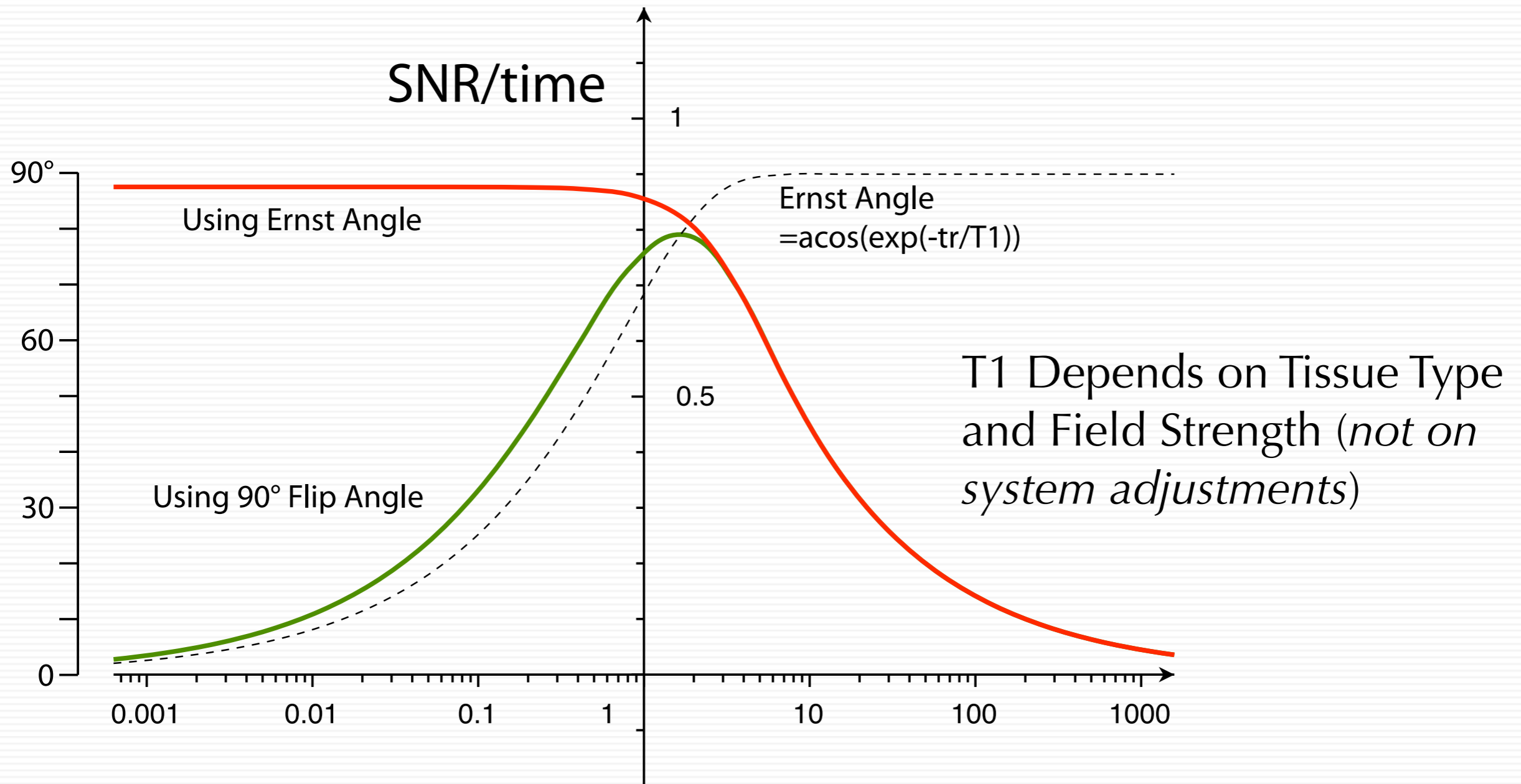


$T2^*$ is both an *Instrument* Parameter and a *Physiological* Parameter



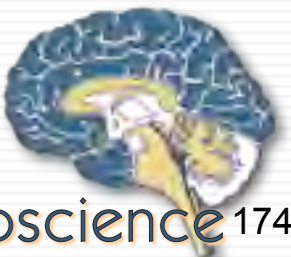
Parameter Optimization - Flip Angle

- SNR per unit time is a *strong* function of $tr/T1$



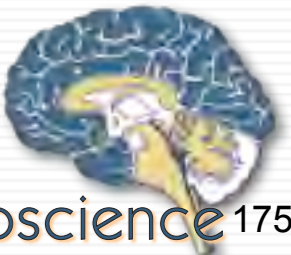
Other Parameters...

- Voxels Should be Large enough that:
 - Thermal Noise \ll Physiological Fluctuations
- For Best Signal with Arbitrary Slice Orientation:
 - Voxels Should be Isotropic
- With Gradient Echo Scans (most BOLD):
 - Signal Falls (much) more than linearly with Slice Thickness
- Do not Confuse Signal to Noise Ratio with Contrast to Noise Ratio!



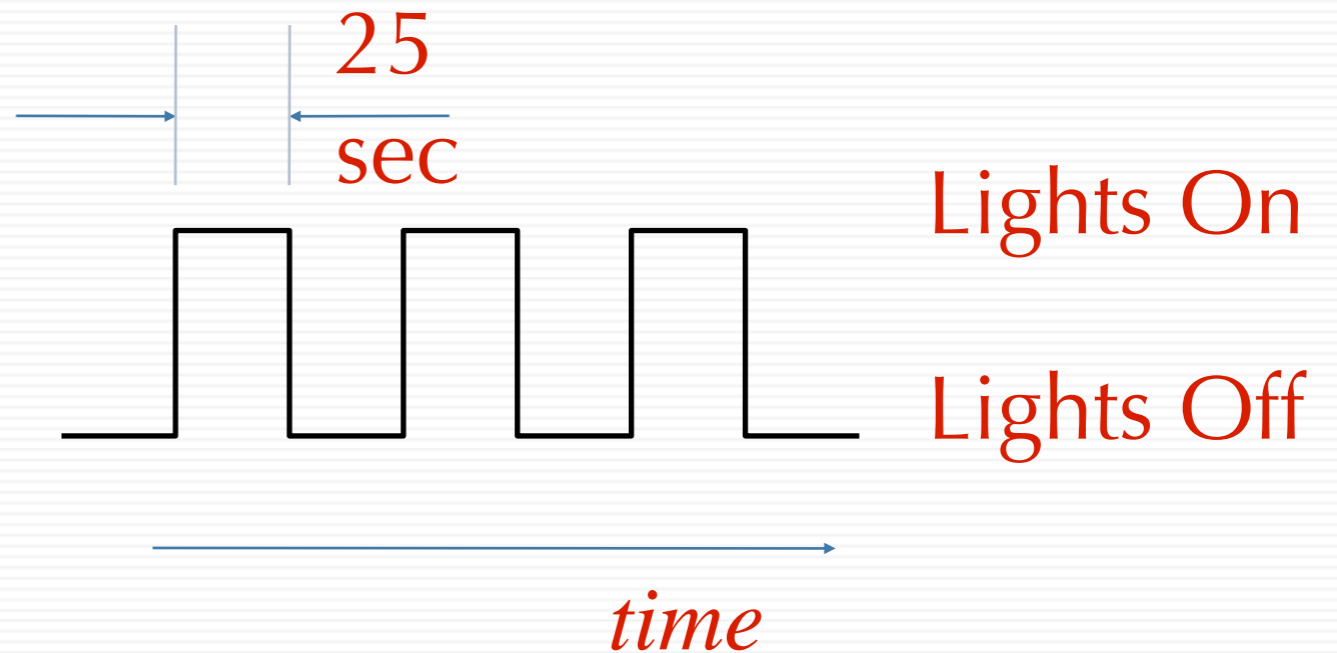
Some Theoretical Considerations

- Study Designs:
 - *Blocked*
 - *Single Trial*
- Predicting Responses
- Sources of Variance
- Resolution Limits:
 - *Temporal*
 - *Spatial*

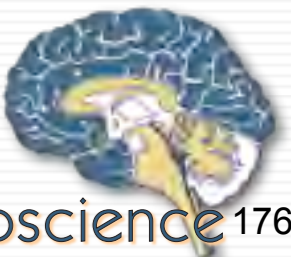
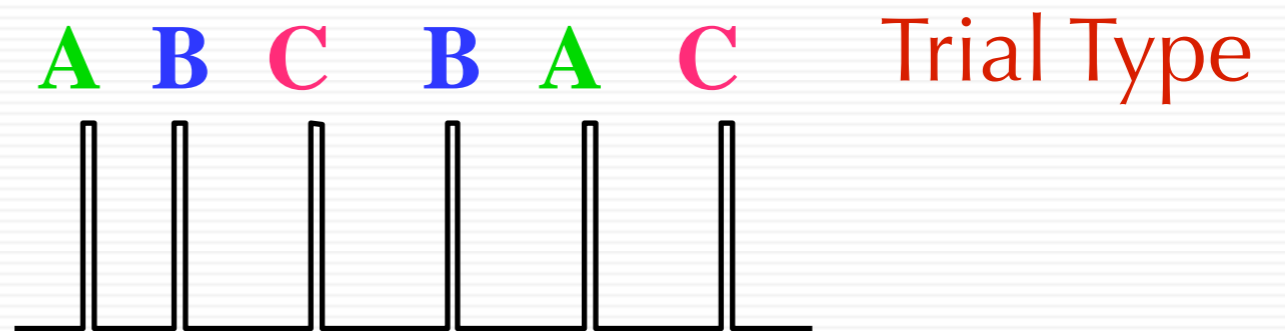


Blocked vs. Single Trial

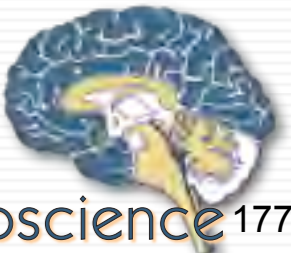
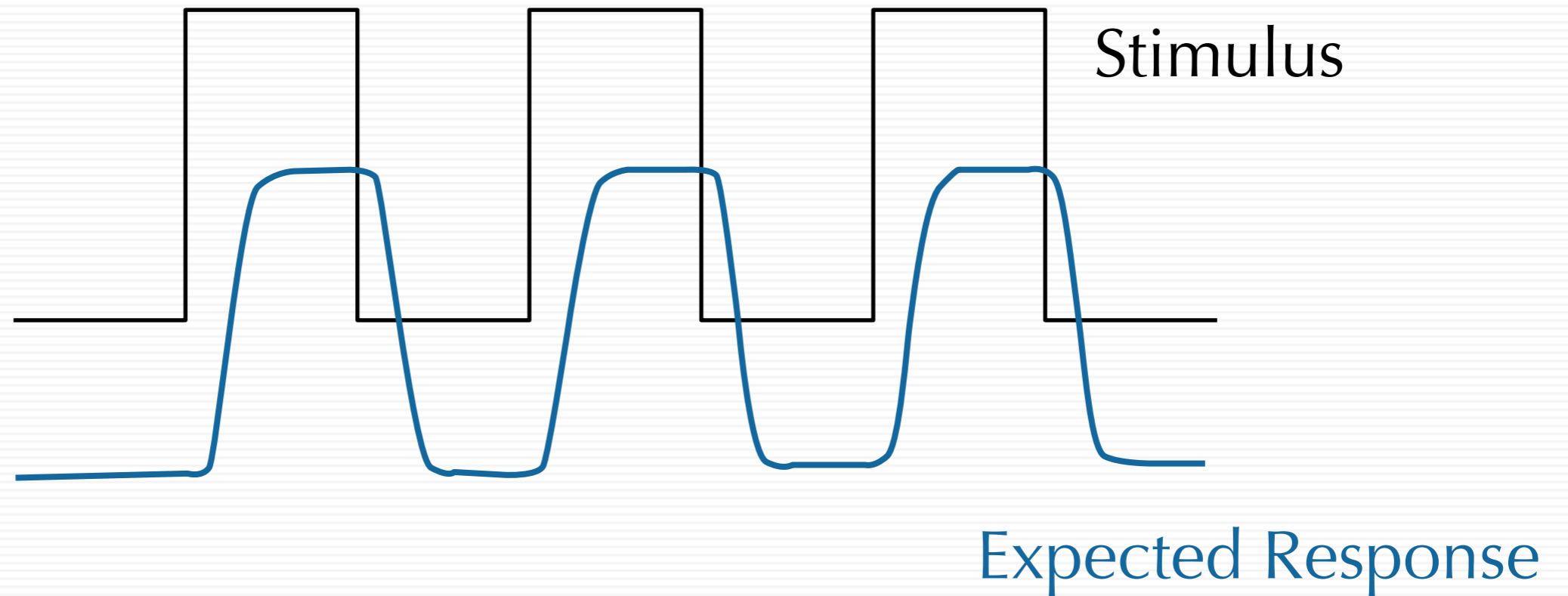
*Typical
Blocked
Design*



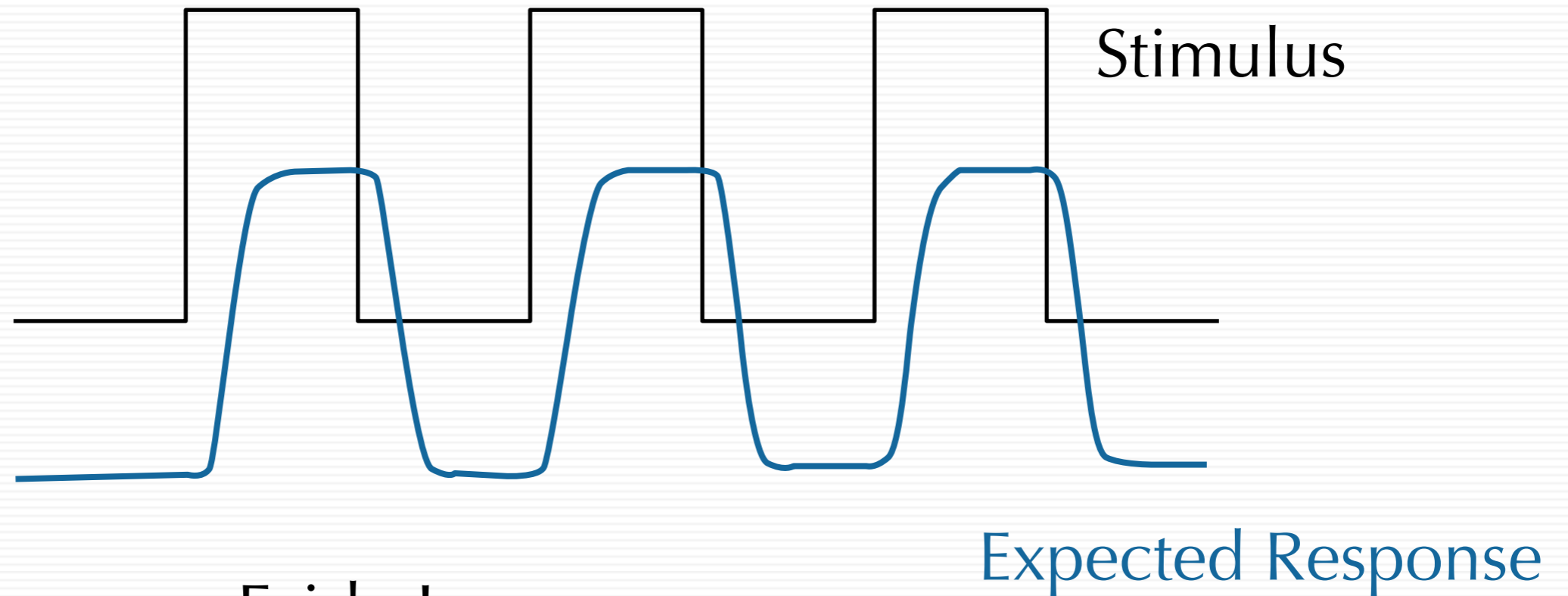
*Typical Single
Trial Design*



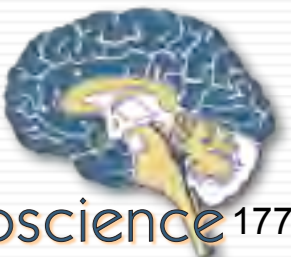
Blocked Experiments



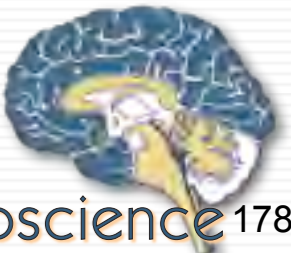
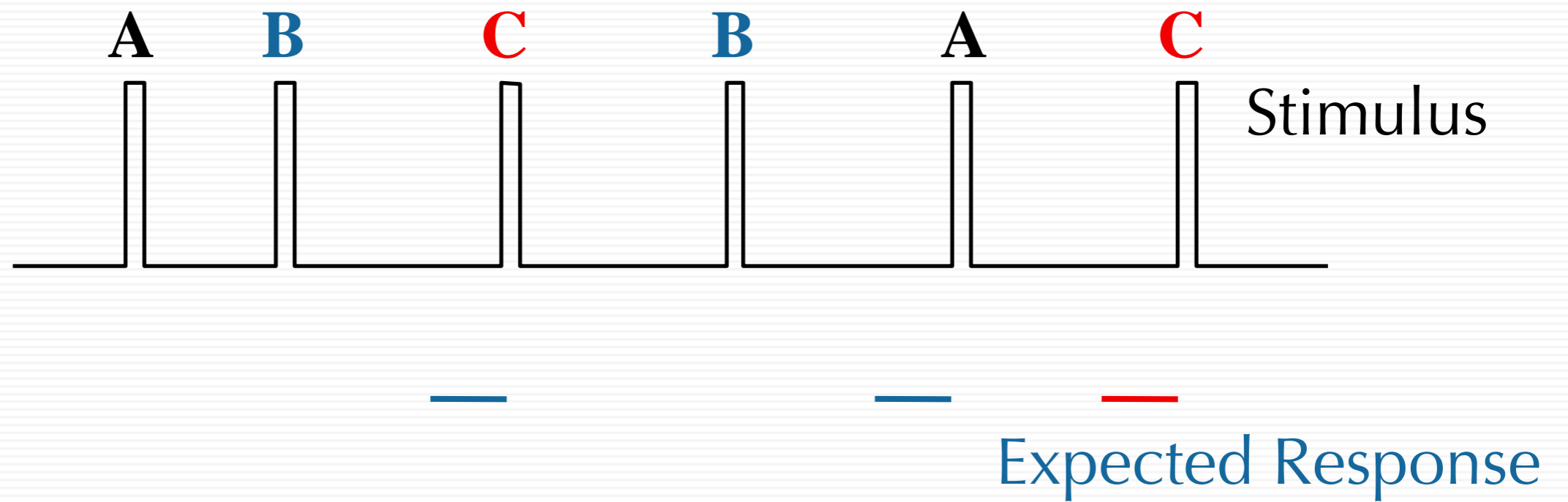
Blocked Experiments



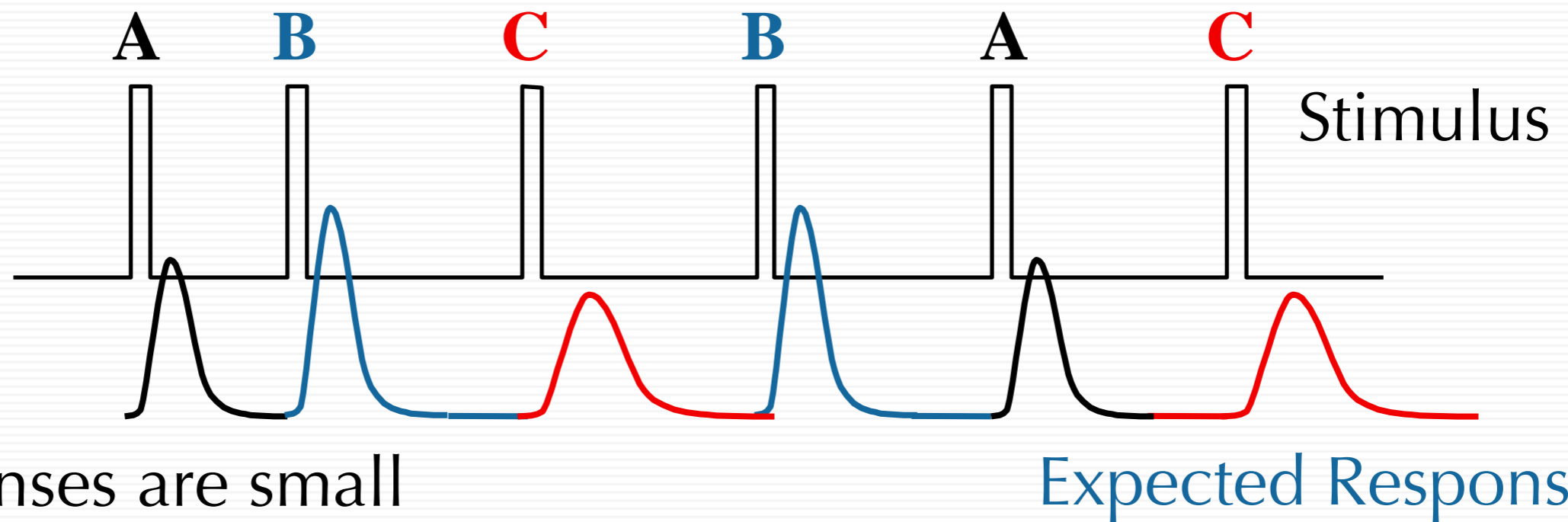
- Responses are Fairly Large
- Data are Easy to Analyze
- With Long Blocks, Time course can be Ignored
- All trials within a block are treated as Identical



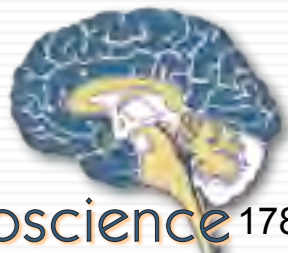
Single Trial Designs



Single Trial Designs

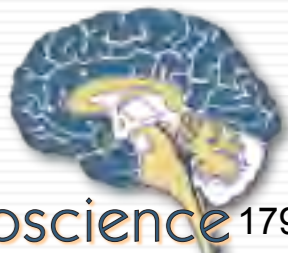
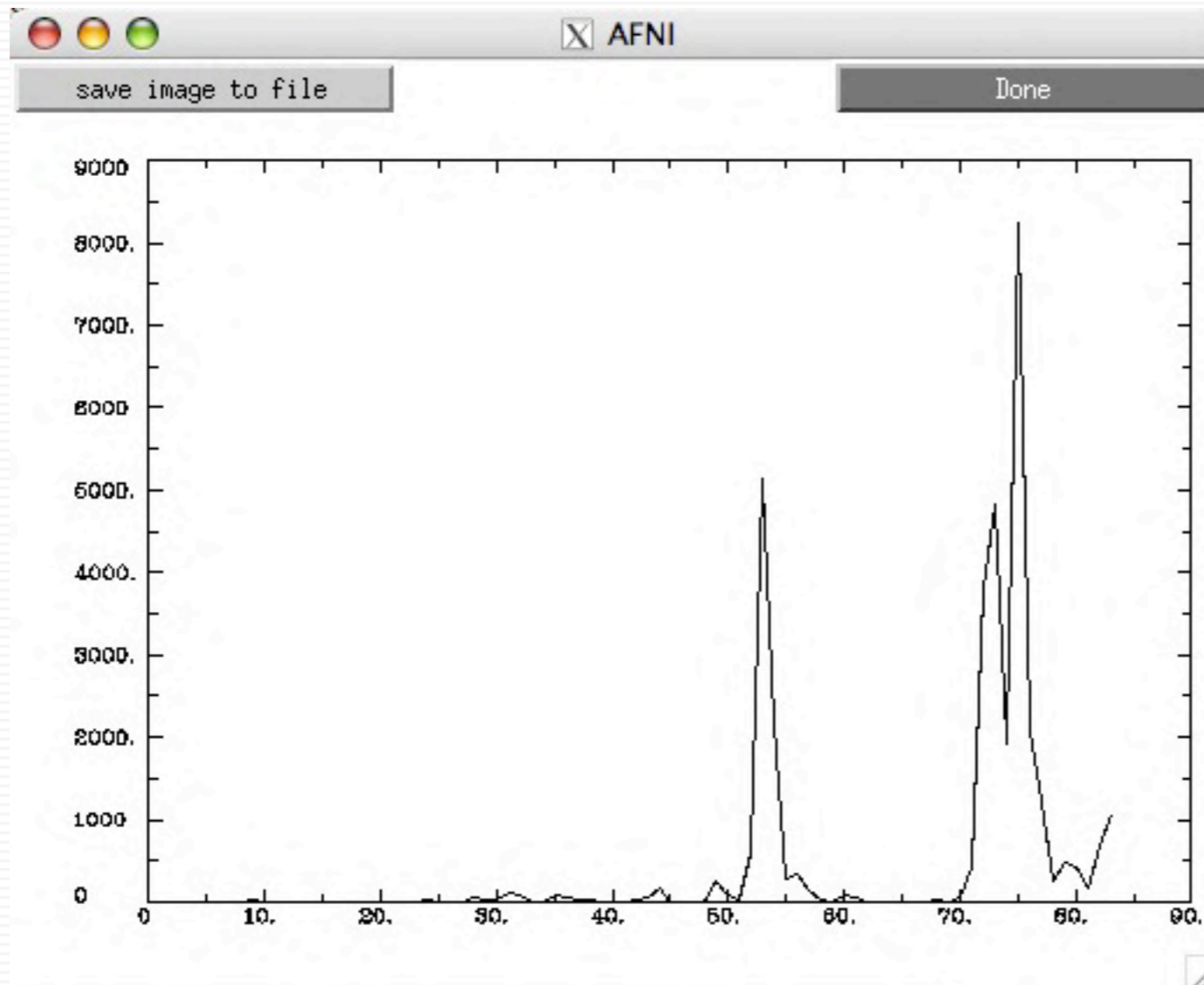


- Responses are small
- Useful contrast/noise is low
- Data are more Challenging to Analyze
- Exact Time course is Modeled or a Dependent Variable
- Suitable for Randomized Stimulus Designs

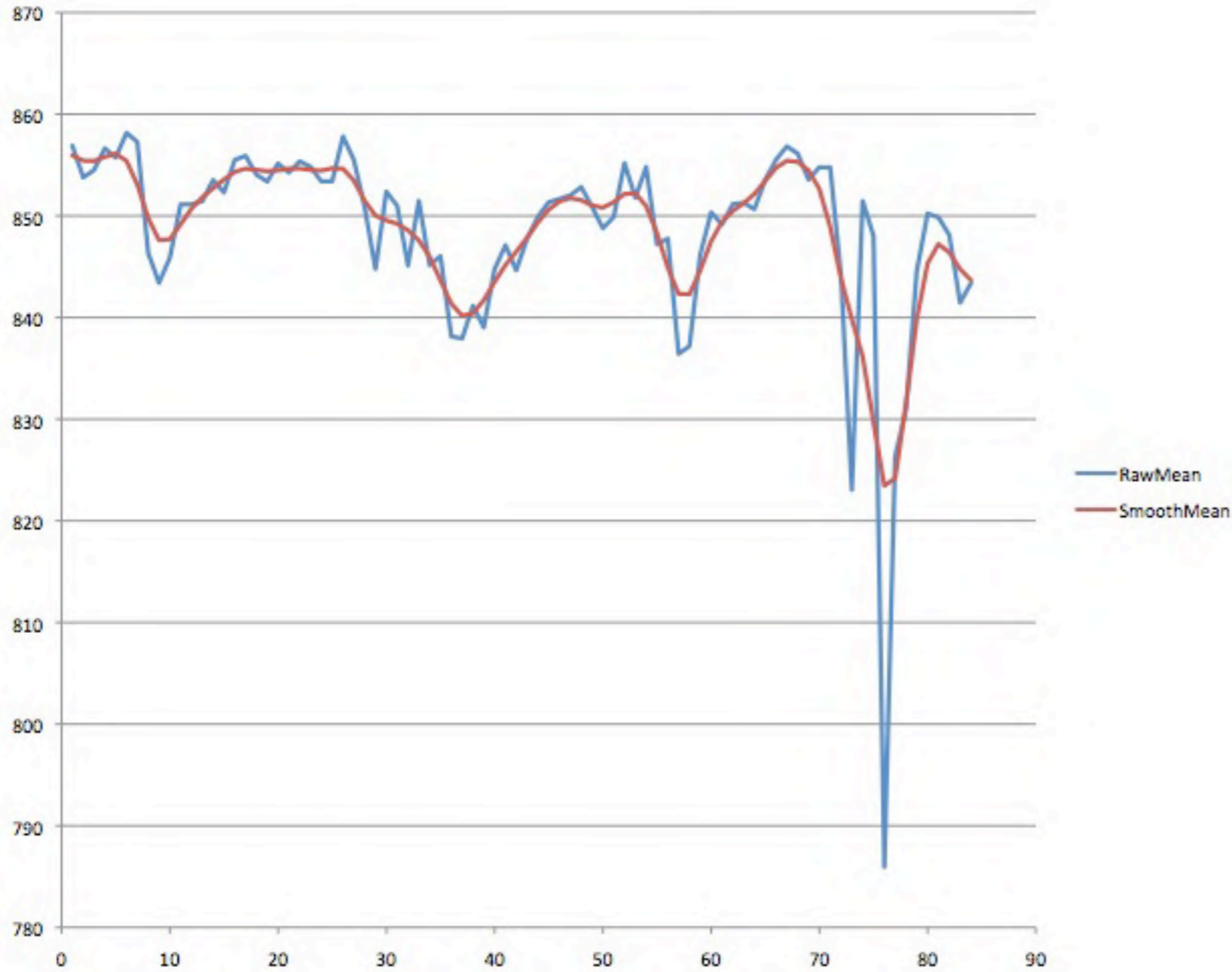


AFNI 3dToutcount

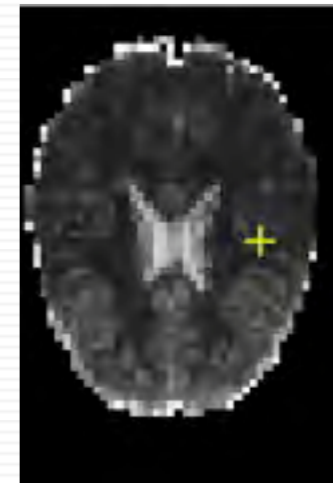
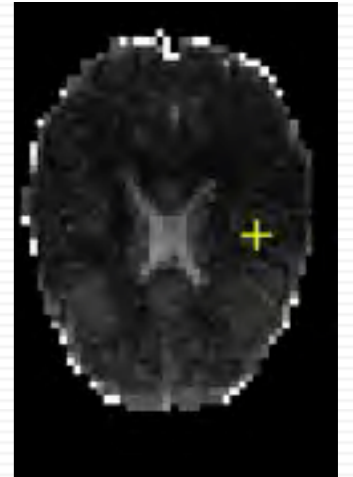
```
3dToutcount -automask KidAsImg.hdr | 1dplot -stdin
```



P2P

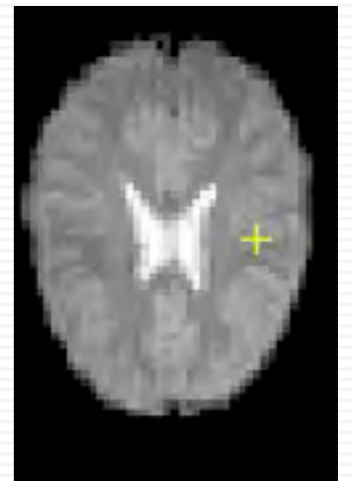


Peak-to peak

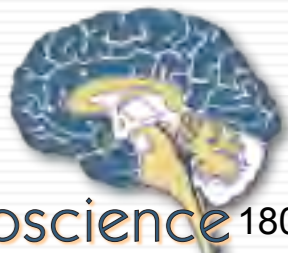
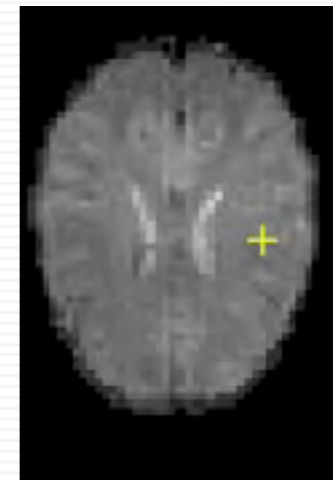


Std Dev

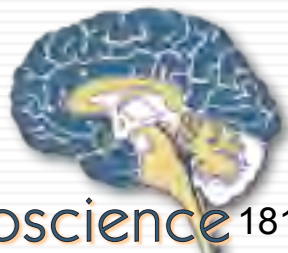
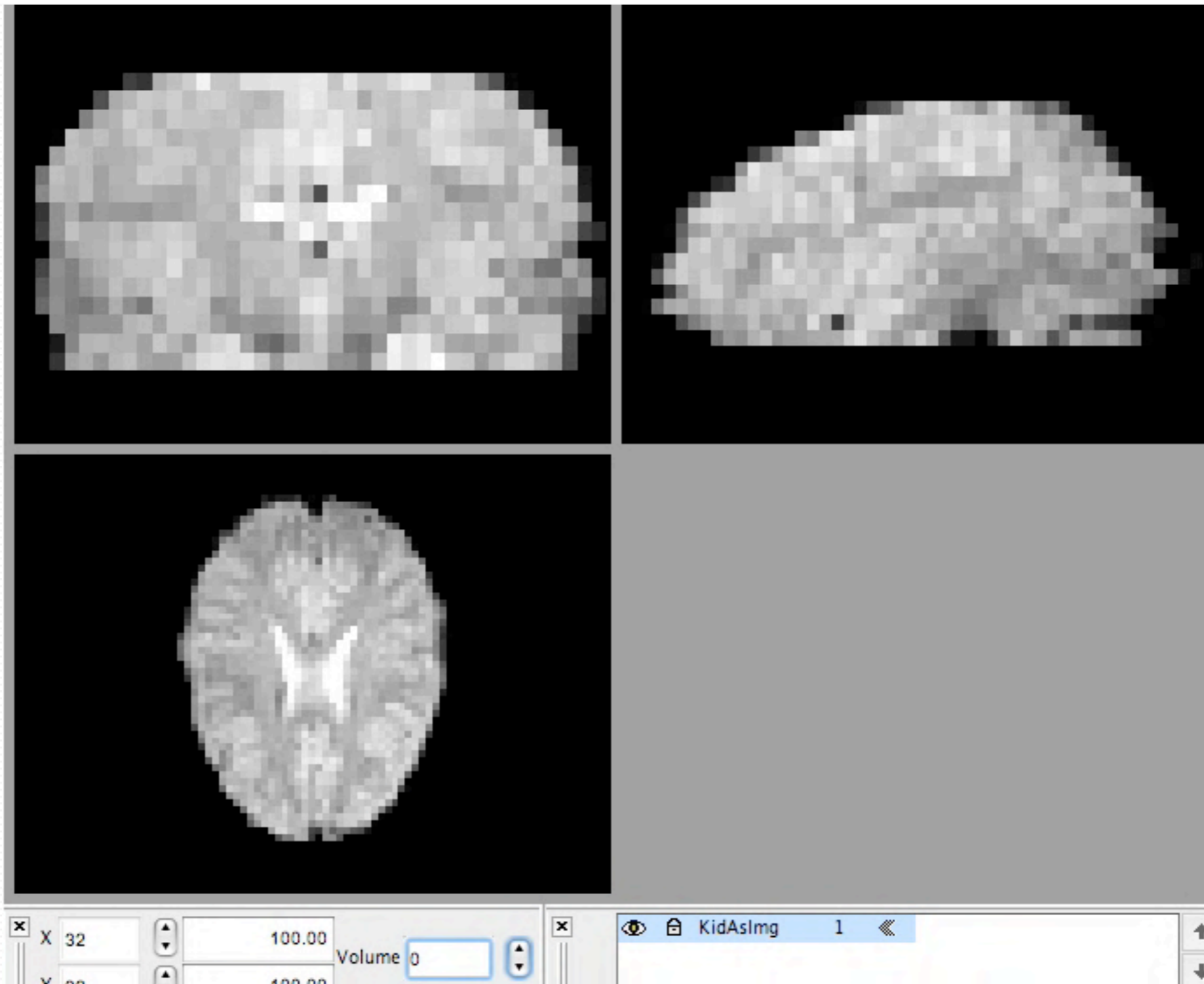
Max



Min



What really happened?



-
- HP filtering consequences
 - FT of scanner drift
 - Anti-alias at $2 \cdot tr$
 - linear regression for DCT gives fit values for the “nuisance” variables. Maps?
 - Gaussian smoother is a low pass filter
 - De-Meaning Figure

